Lecture: Interconnection Networks

- Topics: topologies, deadlock, pipelines, switches, metrics
Consistency Model Recap

**Sequential Consistency Model**
Programmer view                   Hardware view

**Relaxed Consistency Model**
Programmer view                   Hardware view
Network Topology Examples

Grid

Torus

Hypercube
Routing

- Deterministic routing: given the source and destination, there exists a unique route.

- Adaptive routing: a switch may alter the route in order to deal with unexpected events (faults, congestion) – more complexity in the router vs. potentially better performance.

- Example of deterministic routing: dimension order routing: send packet along first dimension until destination co-ord (in that dimension) is reached, then next dimension, etc.
Deadlock

- Deadlock happens when there is a cycle of resource dependencies – a process holds on to a resource (A) and attempts to acquire another resource (B) – A is not relinquished until B is acquired
Each message is attempting to make a left turn – it must acquire an output port, while still holding on to a series of input and output ports.
Deadlock-Free Proofs

- Number edges and show that all routes will traverse edges in increasing (or decreasing) order – therefore, it will be impossible to have cyclic dependencies

- Example: k-ary 2-d array with dimension routing: first route along x-dimension, then along y
Breaking Deadlock

- Consider the eight possible turns in a 2-d array (note that turns lead to cycles)
- By preventing just two turns, cycles can be eliminated
- Dimension-order routing disallows four turns
- Helps avoid deadlock even in adaptive routing

West-First  North-Last  Negative-First  Can allow deadlocks
Packets/Flits

- A message is broken into multiple packets (each packet has header information that allows the receiver to re-construct the original message)

- A packet may itself be broken into flits – flits do not contain additional headers

- Two packets can follow different paths to the destination. Flits are always ordered and follow the same path

- Such an architecture allows the use of a large packet size (low header overhead) and yet allows fine-grained resource allocation on a per-flit basis
Flow Control

• The routing of a message requires allocation of various resources: the channel (or link), buffers, control state

• Bufferless: flits are dropped if there is contention for a link, NACKs are sent back, and the original sender has to re-transmit the packet

• Circuit switching: a request is first sent to reserve the channels, the request may be held at an intermediate router until the channel is available (hence, not truly bufferless), ACKs are sent back, and subsequent packets/flits are routed with little effort (good for bulk transfers)
Virtual Channels

Flits do not carry headers. Once a packet starts going over a channel, another packet cannot cut in (else, the receiving buffer will confuse the flits of the two packets). If the packet is stalled, other packets can’t use the channel.

With virtual channels, the flit can be received into one of N buffers. This allows N packets to be in transit over a given physical channel. The packet must carry an ID to indicate its virtual channel.
Virtual Channel Flow Control

- Incoming flits are placed in buffers

- For this flit to jump to the next router, it must acquire three resources:
  - A free virtual channel on its intended hop
    - We know that a virtual channel is free when the tail flit goes through
  - Free buffer entries for that virtual channel
    - This is determined with credit or on/off management
  - A free cycle on the physical channel
    - Competition among the packets that share a physical channel
Deadlock Avoidance with VCs

- VCs provide another way to number the links such that a route always uses ascending link numbers

- Alternatively, use West-first routing on the 1st plane and cross over to the 2nd plane in case you need to go West again (the 2nd plane uses North-last, for example)
Router Functions

- Crossbar, buffer, arbiter, VC state and allocation, buffer management, ALUs, control logic, routing

- Typical on-chip network power breakdown:
  - 30% link
  - 30% buffers
  - 30% crossbar
Router Pipeline

• Four typical stages:
  ▪ RC routing computation: the head flit indicates the VC that it belongs to, the VC state is updated, the headers are examined and the next output channel is computed (note: this is done for all the head flits arriving on various input channels)
  ▪ VA virtual-channel allocation: the head flits compete for the available virtual channels on their computed output channels
  ▪ SA switch allocation: a flit competes for access to its output physical channel
  ▪ ST switch traversal: the flit is transmitted on the output channel

A head flit goes through all four stages, the other flits do nothing in the first two stages (this is an in-order pipeline and flits can not jump ahead), a tail flit also de-allocates the VC
Router Pipeline

• Four typical stages:
  - RC routing computation: compute the output channel
  - VA virtual-channel allocation: allocate VC for the head flit
  - SA switch allocation: compete for output physical channel
  - ST switch traversal: transfer data on output physical channel

<table>
<thead>
<tr>
<th>Cycle</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
</tr>
</thead>
<tbody>
<tr>
<td>Head flit</td>
<td>RC</td>
<td>VA</td>
<td>SA</td>
<td>ST</td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>Body flit 1</td>
<td>--</td>
<td>--</td>
<td>SA</td>
<td>ST</td>
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<td></td>
<td></td>
</tr>
<tr>
<td>Body flit 2</td>
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<td>--</td>
<td>SA</td>
<td>ST</td>
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<tr>
<td>Tail flit</td>
<td>--</td>
<td>--</td>
<td>SA</td>
<td>ST</td>
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</table>

STALL
Trends

- Growing interest in eliminating the area/power overheads of router buffers; traffic levels are also relatively low, so virtual-channel buffered routed networks may be overkill

- Option 1: use a bus for short distances (16 cores) and use a hierarchy of buses to travel long distances

- Option 2: hot-potato or bufferless routing
Centralized Crossbar Switch
Crossbar Properties

• Assuming each node has one input and one output, a crossbar can provide maximum bandwidth: N messages can be sent as long as there are N unique sources and N unique destinations.

• Maximum overhead: $WN^2$ internal switches, where $W$ is data width and $N$ is number of nodes.

• To reduce overhead, use smaller switches as building blocks – trade off overhead for lower effective bandwidth.
Switch with Omega Network
Omega Network Properties

- The switch complexity is now $O(N \log N)$

- Contention increases: $P0 \rightarrow P5$ and $P1 \rightarrow P7$ cannot happen concurrently (this was possible in a crossbar)

- To deal with contention, can increase the number of levels (redundant paths) – by mirroring the network, we can route from $P0$ to $P5$ via $N$ intermediate nodes, while increasing complexity by a factor of 2
Tree Network

- Complexity is $O(N)$
- Can yield low latencies when communicating with neighbors
- Can build a fat tree by having multiple incoming and outgoing links
Bisection Bandwidth

• Split N nodes into two groups of N/2 nodes such that the bandwidth between these two groups is minimum: that is the bisection bandwidth

• Why is it relevant: if traffic is completely random, the probability of a message going across the two halves is $\frac{1}{2}$ – if all nodes send a message, the bisection bandwidth will have to be N/2

• The concept of bisection bandwidth confirms that the tree network is not suited for random traffic patterns, but for localized traffic patterns
## Topology Examples

### Grid

<table>
<thead>
<tr>
<th>Criteria</th>
<th>Bus</th>
<th>Ring</th>
<th>2Dtorus</th>
<th>Hypercube</th>
<th>Fully connected</th>
</tr>
</thead>
<tbody>
<tr>
<td>64 nodes</td>
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<td></td>
<td></td>
<td></td>
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<tr>
<td>Performance</td>
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</tr>
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<td>Bisection bandwidth</td>
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<td>Cost</td>
<td></td>
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<tr>
<td>Diameter</td>
<td>1</td>
<td>32</td>
<td>8</td>
<td>6</td>
<td>1</td>
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<tr>
<td>Bisection BW</td>
<td>1</td>
<td>2</td>
<td>16</td>
<td>32</td>
<td>1024</td>
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k-ary d-cube

- Consider a k-ary d-cube: a d-dimension array with k elements in each dimension, there are links between elements that differ in one dimension by 1 (mod k)

- Number of nodes $N = k^d$

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<th>Avg. routing distance:</th>
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<td>Switch degree</td>
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<td>Bisection bandwidth</td>
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Should we minimize or maximize dimension?
k-ary d-Cube

- Consider a k-ary d-cube: a d-dimension array with k elements in each dimension, there are links between elements that differ in one dimension by 1 (mod k)

- Number of nodes $N = k^d$

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<th>Number of switches</th>
<th>$N$</th>
<th>Avg. routing distance: $d(k-1)/4$</th>
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<tr>
<td>Switch degree</td>
<td>$2d + 1$</td>
<td>Diameter</td>
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<td>Number of links</td>
<td>$Nd$</td>
<td>Bisection bandwidth</td>
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<td>$2wd$</td>
<td>Switch complexity</td>
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The switch degree, num links, pins per node, bisection bw for a hypercube are half of what is listed above (diam and avg routing distance are twice, switch complexity is $(d + 1)^2$) because unlike the other cases, a hypercube does not have right and left neighbors.

Should we minimize or maximize dimension?

27