

CS 6530: Advanced Database Systems Fall 2023

Lecture 10

Write-Optimized Indexes

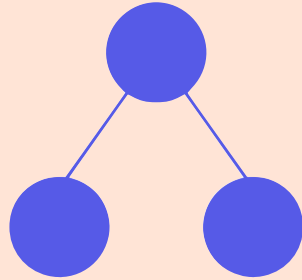
Prashant Pandey

prashant.pandey@utah.edu

Slides taken from Prof. Alex Conway, Cornell Tech

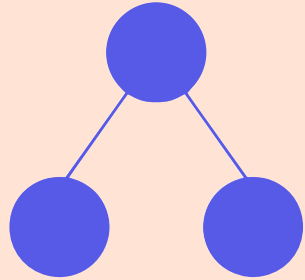
The Story of SplinterDB

Model the problem:
external memory dictionary



The Story of SplinterDB

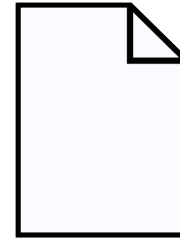
Model the problem:
external memory dictionary



48 B



4 KiB



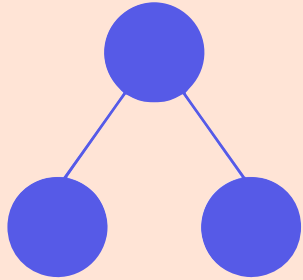
IO 4 KiB



Metadata is fine-grained

The Story of SplinterDB

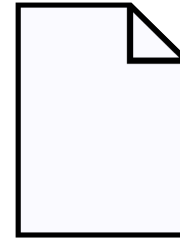
Model the problem:
external memory dictionary



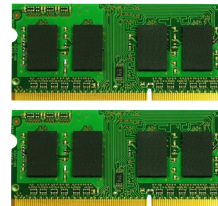
48 B



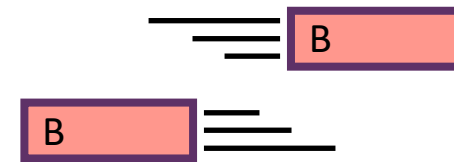
4 KiB



IO 4 KiB



Internal
Memory of size
M



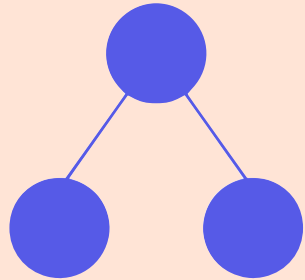
A B-sized block can be read or
written in 1 IO



External Memory Model

The Story of SplinterDB

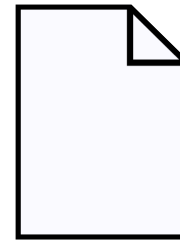
Model the problem:
external memory dictionary



48 B



4 KiB

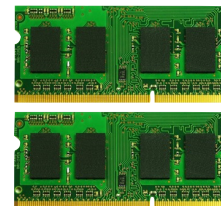


IO 4 KiB

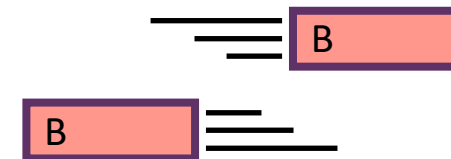


Here B is the number of
items in an IO:
 $B = 4 \text{ KiB} / 48 \text{ B}$

If the items were larger, the model
wouldn't be as good



Internal
Memory of size
M



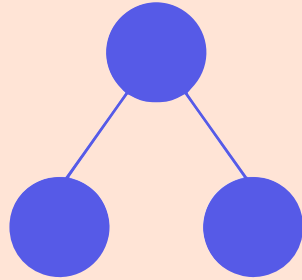
A B-sized block can be read or
written in 1 IO



External Memory Model

The Story of SplinterDB

Model the problem:
external memory dictionary



Two Flavors of
External-Memory Dictionary

Different lower bounds
(performance limits)

Comparison-Based Dictionaries

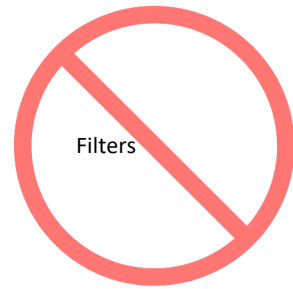
Comparison External Memory Model

user024299 <
= user082587
>

Comparison-Based Dictionaries

Comparison External Memory Model

user024299 < user082587
=>



Comparison-Based Dictionaries

Comparison External Memory Model

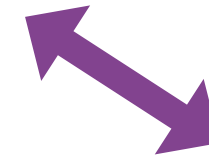
Brodal-Fagerberg Lower Bound

user024299 < user082587
= >



Insertions in

$$O\left(\frac{\lambda}{B} \log_{\lambda} N\right)$$



Lookups in

$$\Omega(\log_{\lambda} N)$$

where λ is a tuning parameter

Lower bounds for external memory dictionaries,
Brodal, G., Fagerberg, R. SODA '03

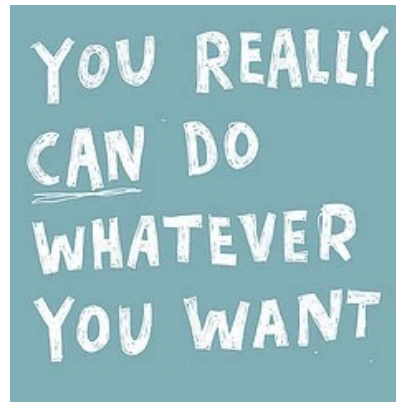
General Dictionaries

External Memory Model

General Dictionaries

External Memory Model

user024299



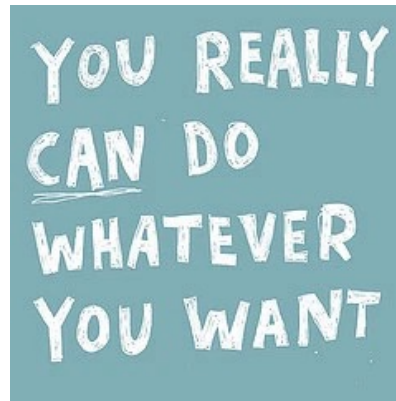
General Dictionaries

External Memory Model

user024299

Hashing

XXH(user024299)



General Dictionaries

External Memory Model

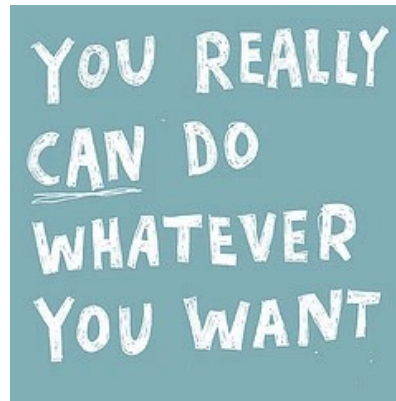
user024299

Hashing

XXH(user024299)

Filters

qf_insert(user024299)



General Dictionaries

External Memory Model

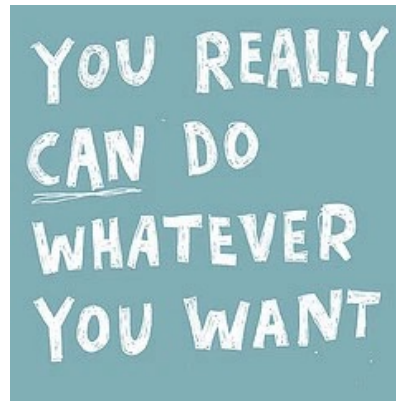
user024299

Hashing

XXH(user024299)

Filters

qf_insert(user024299)

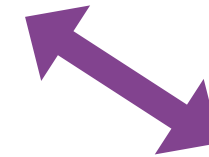


Using hashing to solve the dictionary problem (in external memory),
Iacono, J., Pătrașcu, M. SODA '12

Iacono-Pătrașcu Lower Bound

Insertions in

$$O\left(\frac{\lambda}{B} \log_{\lambda} N\right)$$



Lookups in

$$\Omega(\log_{\lambda} N)$$

where λ is a tuning parameter

Lower Bounds

Brodal-Fagerberg Lower Bound

Insertions in

$$O\left(\frac{\lambda}{B} \log_{\lambda} N\right)$$



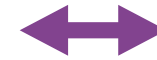
Lookups in

$$\Omega(\log_{\lambda} N)$$

Iacono-Pătraşcu Lower Bound

Insertions in

$$O\left(\frac{\lambda}{B}\right)$$



Lookups in

$$\Omega(\log_{\lambda} N)$$

Comparison External Memory Model

General External Memory Model

Lower Bounds

Brodal-Fagerberg Lower Bound

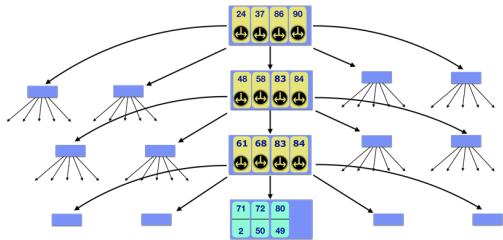
Insertions in

$$O\left(\frac{\lambda}{B} \log_{\lambda} N\right)$$



Lookups in

$$\Omega(\log_{\lambda} N)$$



B-Trees

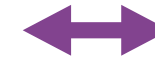
$$(\lambda = B)$$

Comparison External Memory Model

Iacono-Pătraşcu Lower Bound

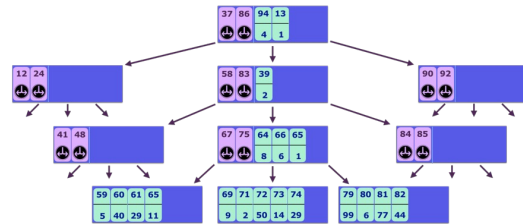
Insertions in

$$O\left(\frac{\lambda}{B}\right)$$



Lookups in

$$\Omega(\log_{\lambda} N)$$



B^ε-Trees

$$(\lambda = B^{\epsilon})$$

General External Memory Model

Lower Bounds

Brodal-Fagerberg Lower Bound

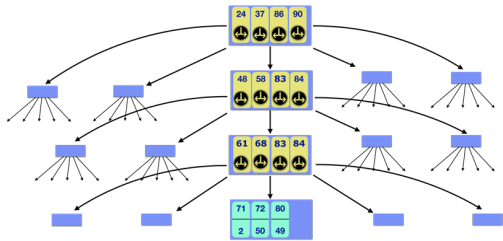
Insertions in

$$O\left(\frac{\lambda}{B} \log_{\lambda} N\right)$$



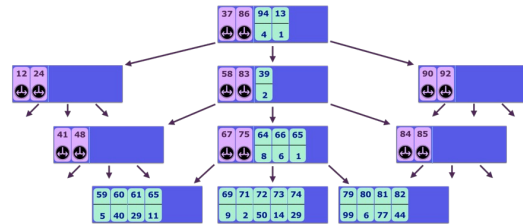
Lookups in

$$\Omega(\log_{\lambda} N)$$



B-Trees

$$(\lambda = B)$$



B^ε-Trees

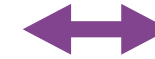
$$(\lambda = B^{\epsilon})$$

Comparison External Memory Model

Iacono-Pătraşcu Lower Bound

Insertions in

$$O\left(\frac{\lambda}{B}\right)$$



Lookups in

$$\Omega(\log_{\lambda} N)$$

Iacono-Patrascu Hash Table

BoA/BoT Hash Table

General External Memory Model

Lower Bounds

Brodal-Fagerberg Lower Bound

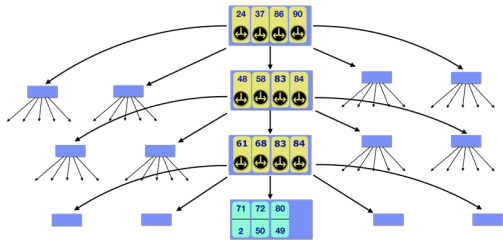
Insertions in

$$O\left(\frac{\lambda}{B} \log_{\lambda} N\right)$$



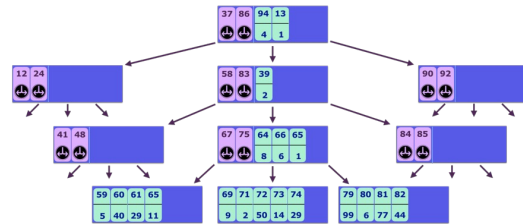
Lookups in

$$\Omega(\log_{\lambda} N)$$



B-Trees

$$(\lambda = B)$$



B^{ϵ} -Trees

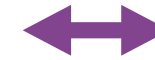
$$(\lambda = B^{\epsilon})$$

Comparison External Memory Model

Iacono-Pătraşcu Lower Bound

Insertions in

$$O\left(\frac{\lambda}{B}\right)$$



Lookups in

$$\Omega(\log_{\lambda} N)$$

Iacono-Patrascu Hash Table

BoA/BoT
Hash Table

Optimal Hashing in External Memory, Conway, Farach-Colton, Shillane, ICALP 2018

Lower Bounds

Brodal-Fagerberg Lower Bound

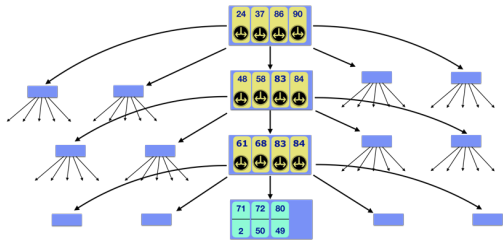
Insertions in

$$O\left(\frac{\lambda}{B} \log_{\lambda} N\right)$$



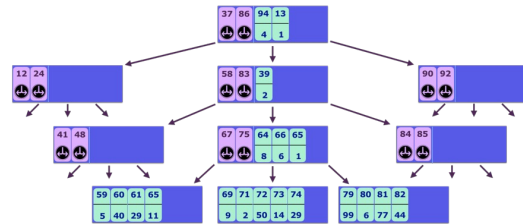
Lookups in

$$\Omega(\log_{\lambda} N)$$



B-Trees

$$(\lambda = B)$$



B^ε-Trees

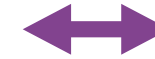
$$(\lambda = B^{\epsilon})$$

Comparison External Memory Model

Iacono-Pătraşcu Lower Bound

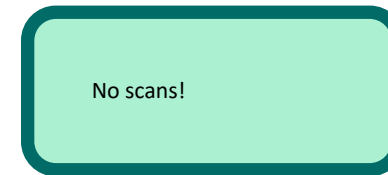
Insertions in

$$O\left(\frac{\lambda}{B}\right)$$



Lookups in

$$\Omega(\log_{\lambda} N)$$



Iacono-Patrascu Hash Table



BoA/BoT Hash Table



General External Memory Model

Lower Bounds

Brodal-Fagerberg Lower Bound

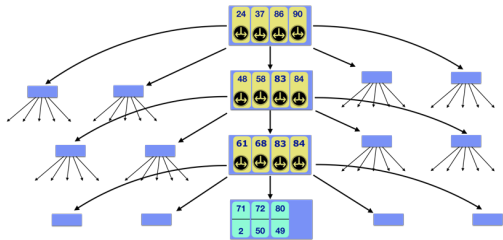
Insertions in

$$O\left(\frac{\lambda}{B} \log_{\lambda} N\right)$$



Lookups in

$$\Omega(\log_{\lambda} N)$$



B-Trees

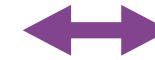
$$(\lambda = B)$$

Comparison External Memory Model

Iacono-Pătraşcu Lower Bound

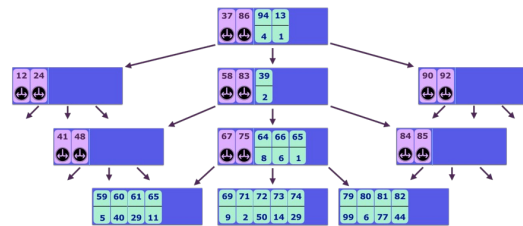
Insertions in

$$O\left(\frac{\lambda}{B}\right)$$



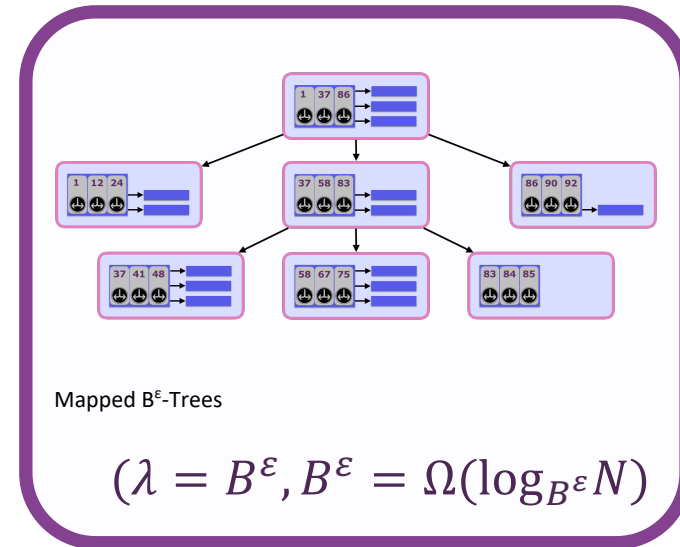
Lookups in

$$\Omega(\log_{\lambda} N)$$



B^{ϵ} -Trees

$$(\lambda = B^{\epsilon})$$



Mapped B^{ϵ} -Trees

$$(\lambda = B^{\epsilon}, B^{\epsilon} = \Omega(\log_{B^{\epsilon}} N))$$

General External Memory Model

Iacono-Patrascu Hash Table

BoA/BoT Hash Table

Lower Bounds

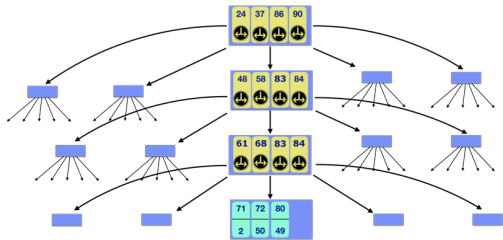
Brodal-Fagerberg Lower Bound

Insertions in

$$O\left(\frac{\lambda}{B} \log_{\lambda} N\right)$$

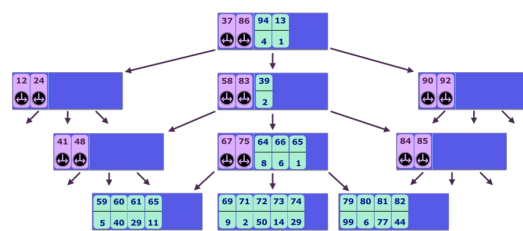
Lookups in

$$\Omega(\log_{\lambda} N)$$



B-Trees

$$(\lambda = B)$$



B^{ϵ} -Trees

$$(\lambda = B^{\epsilon})$$

Comparison External Memory Model

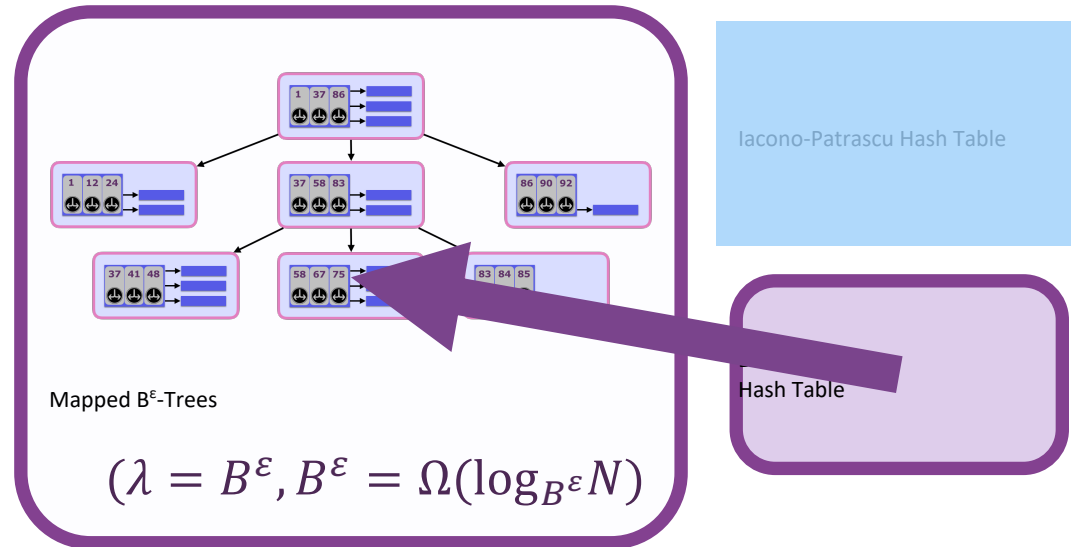
Iacono-Pătraşcu Lower Bound

Insertions in

$$O\left(\frac{\lambda}{B}\right)$$

Lookups in

$$\Omega(\log_{\lambda} N)$$



General External Memory Model

I/O Amplification

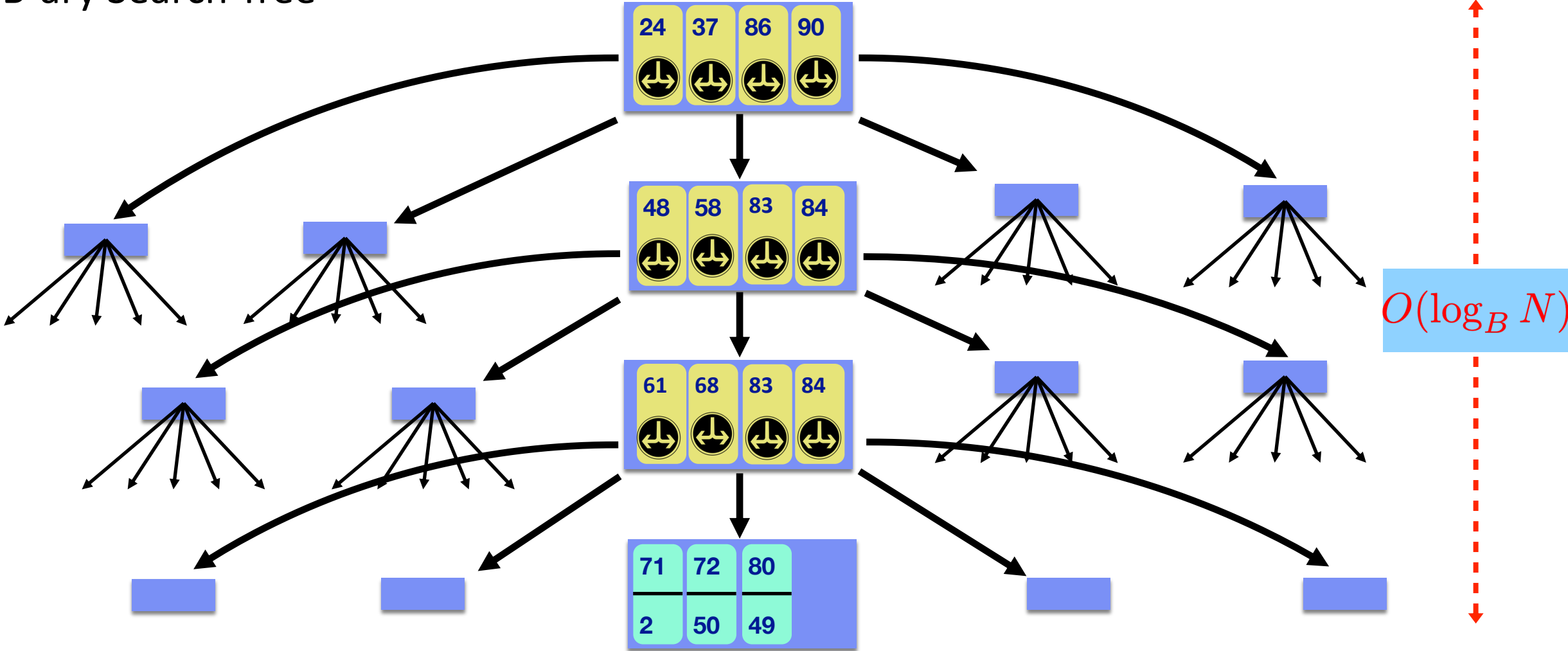
Read amplification is the ratio of the number of blocks read from the disk versus the number of blocks required to read the key-value pair.

Write amplification is the ratio of the number of blocks written to the disk versus the number of blocks required to write the key-value pair.

B-Trees

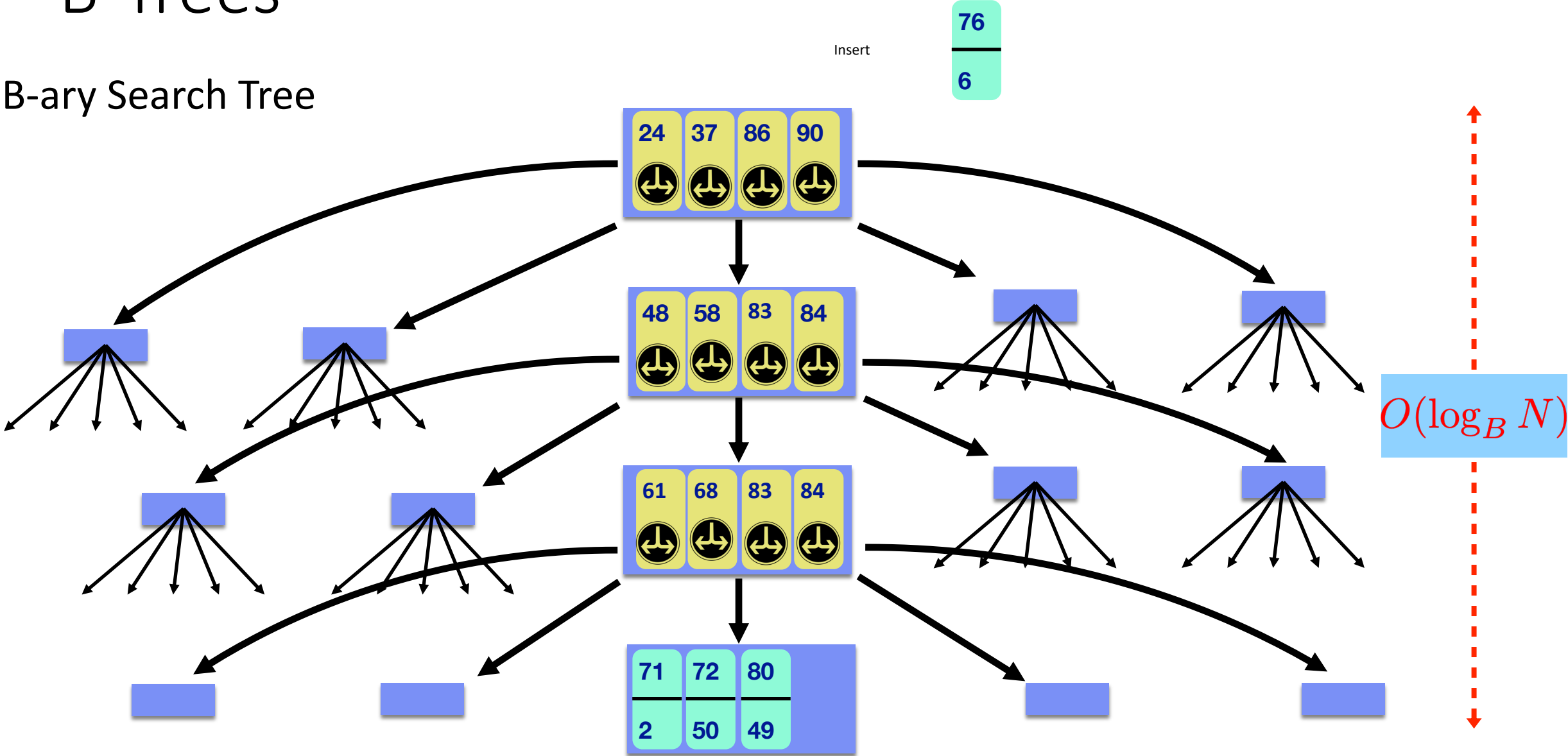
B-Trees

B-ary Search Tree



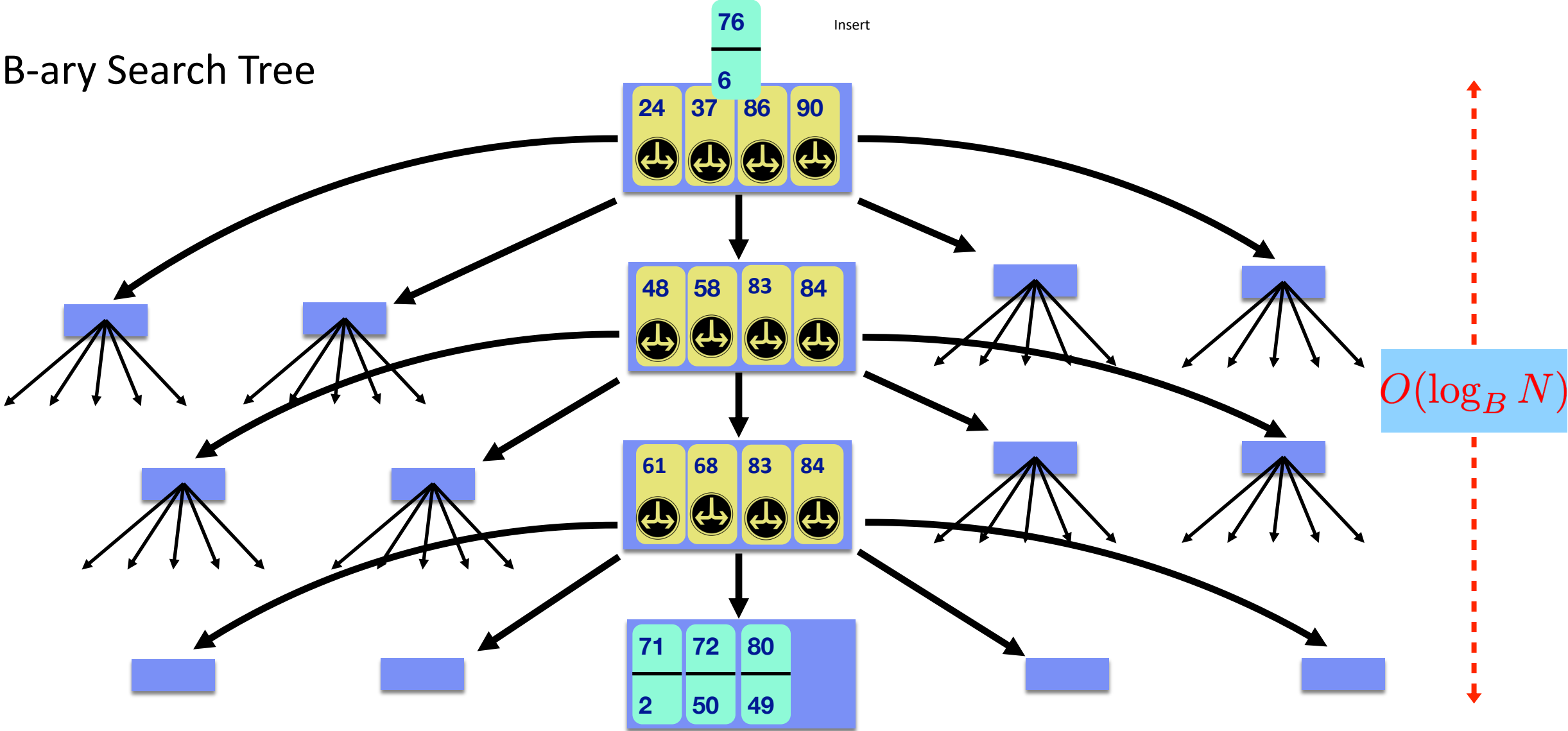
B-Trees

B-ary Search Tree



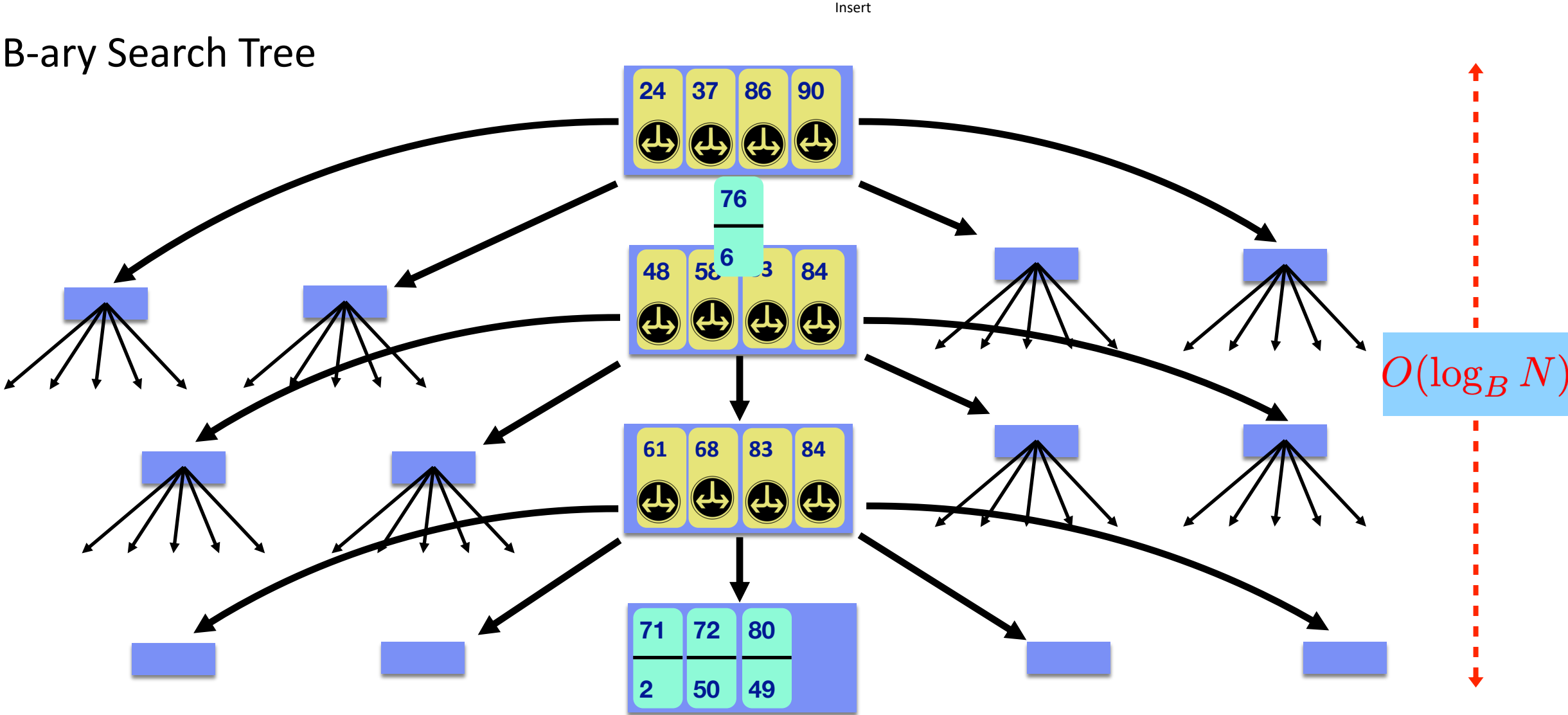
B-Trees

B-ary Search Tree



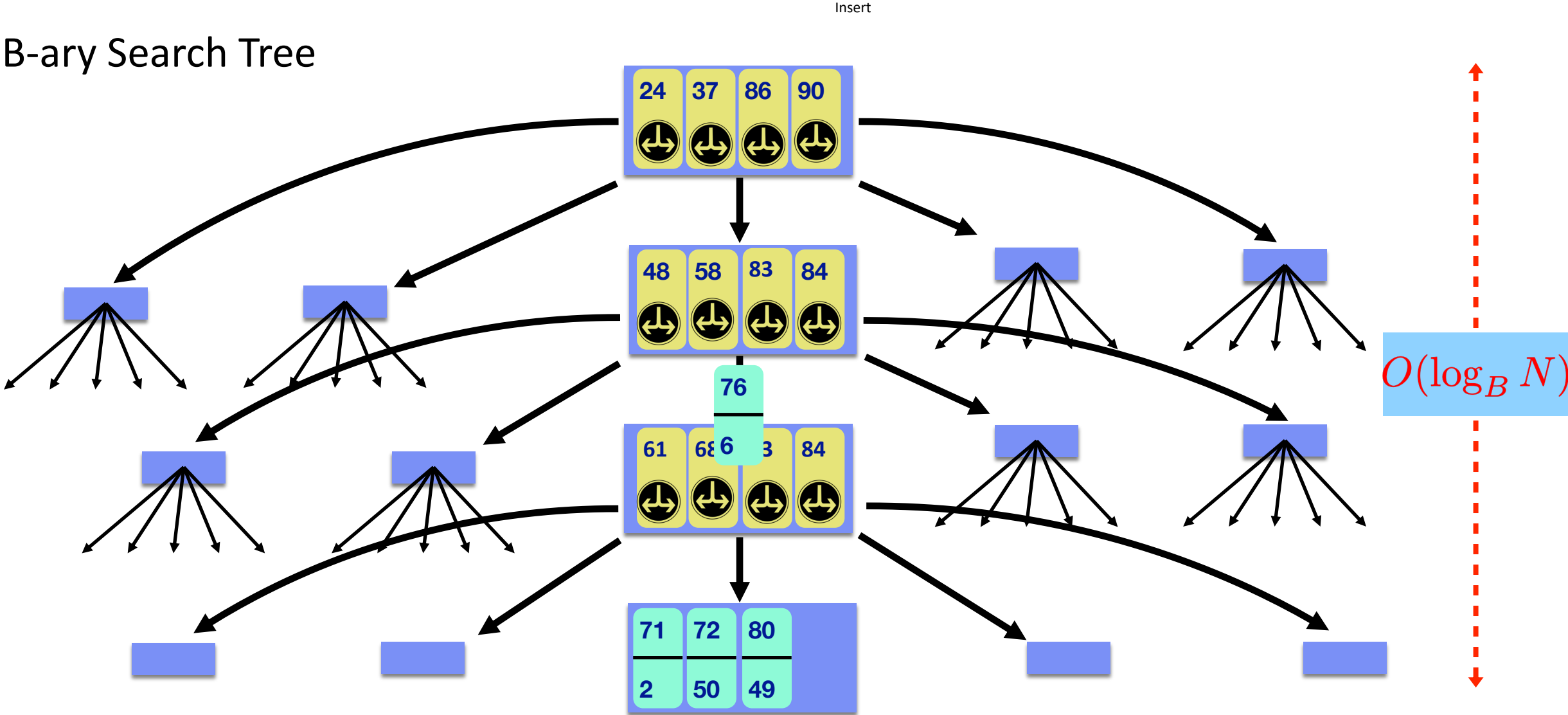
B-Trees

B-ary Search Tree



B-Trees

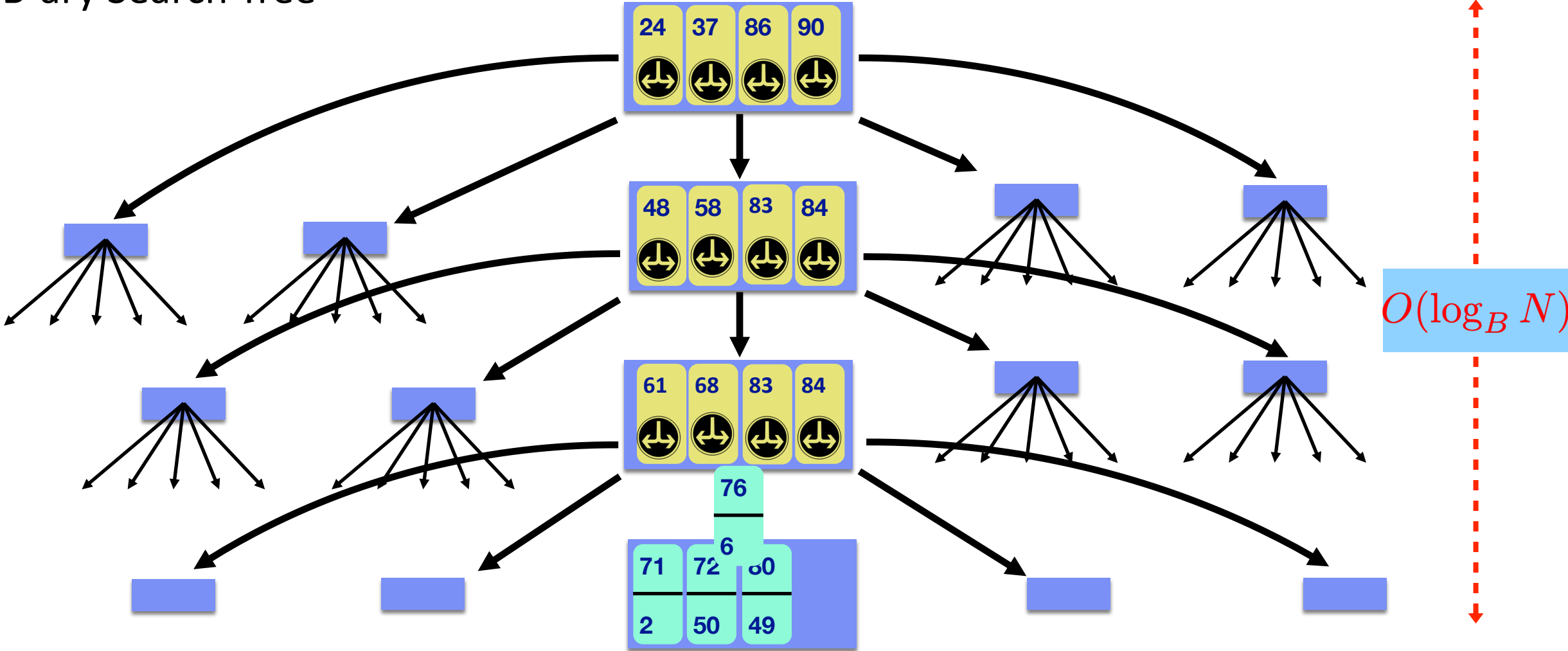
B-ary Search Tree



B-Trees

B-ary Search Tree

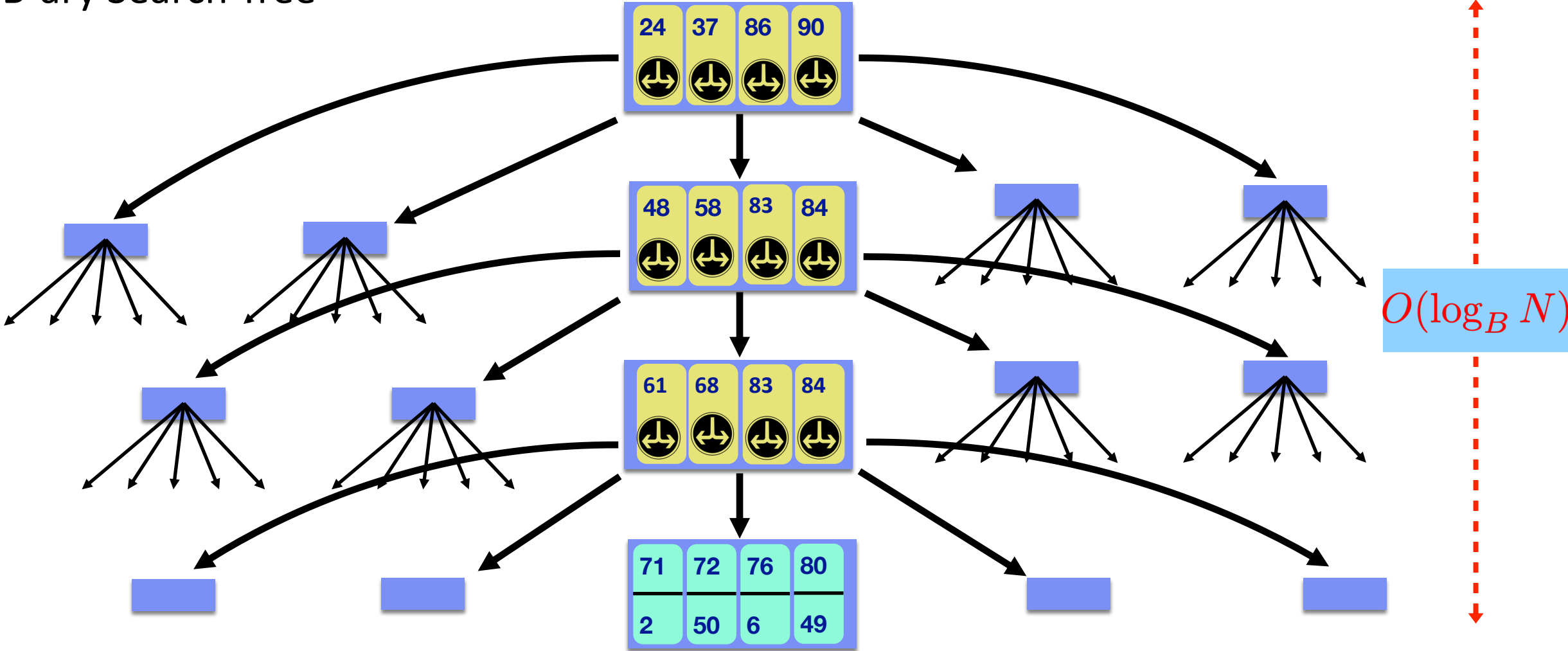
Insert



B-Trees

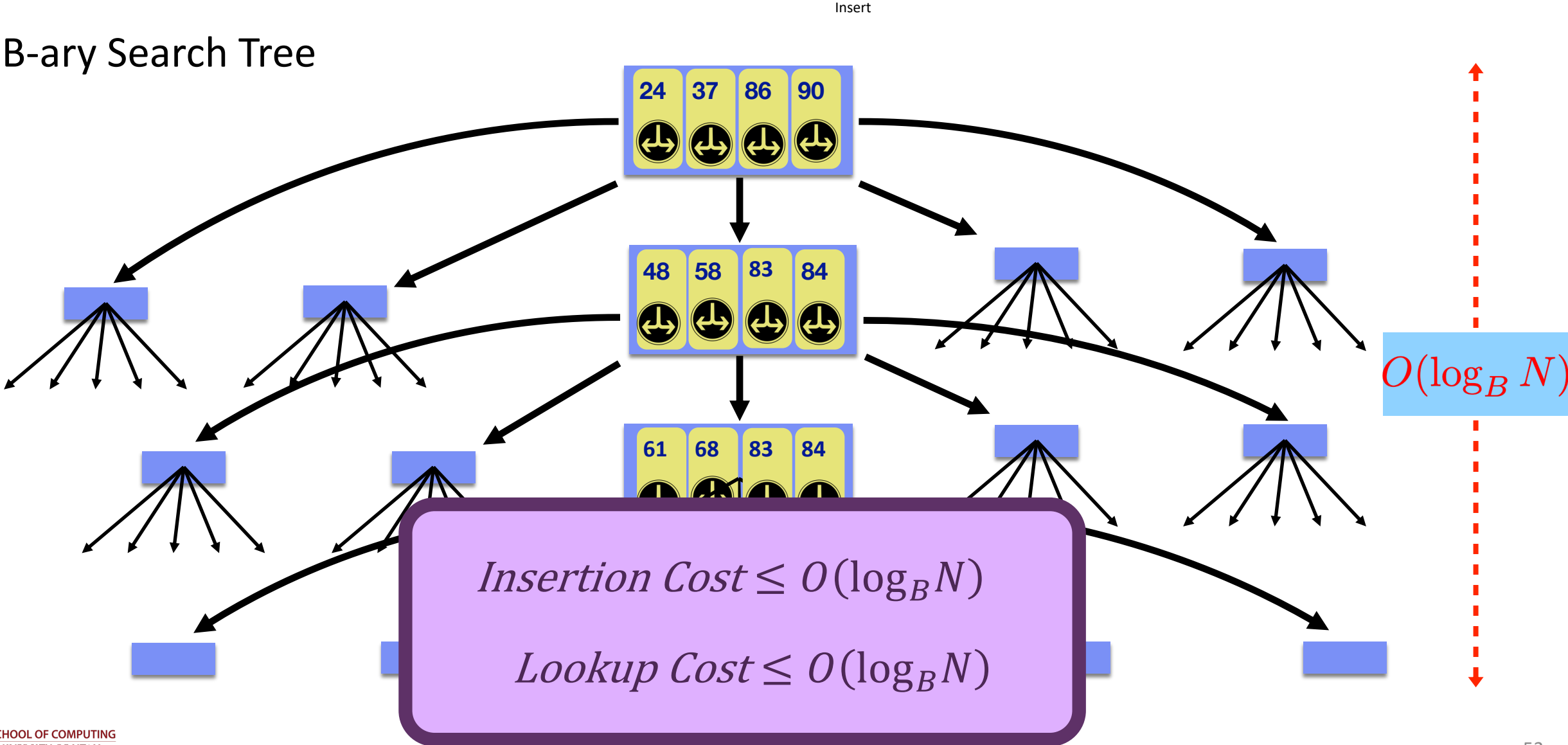
B-ary Search Tree

Insert



B-Trees

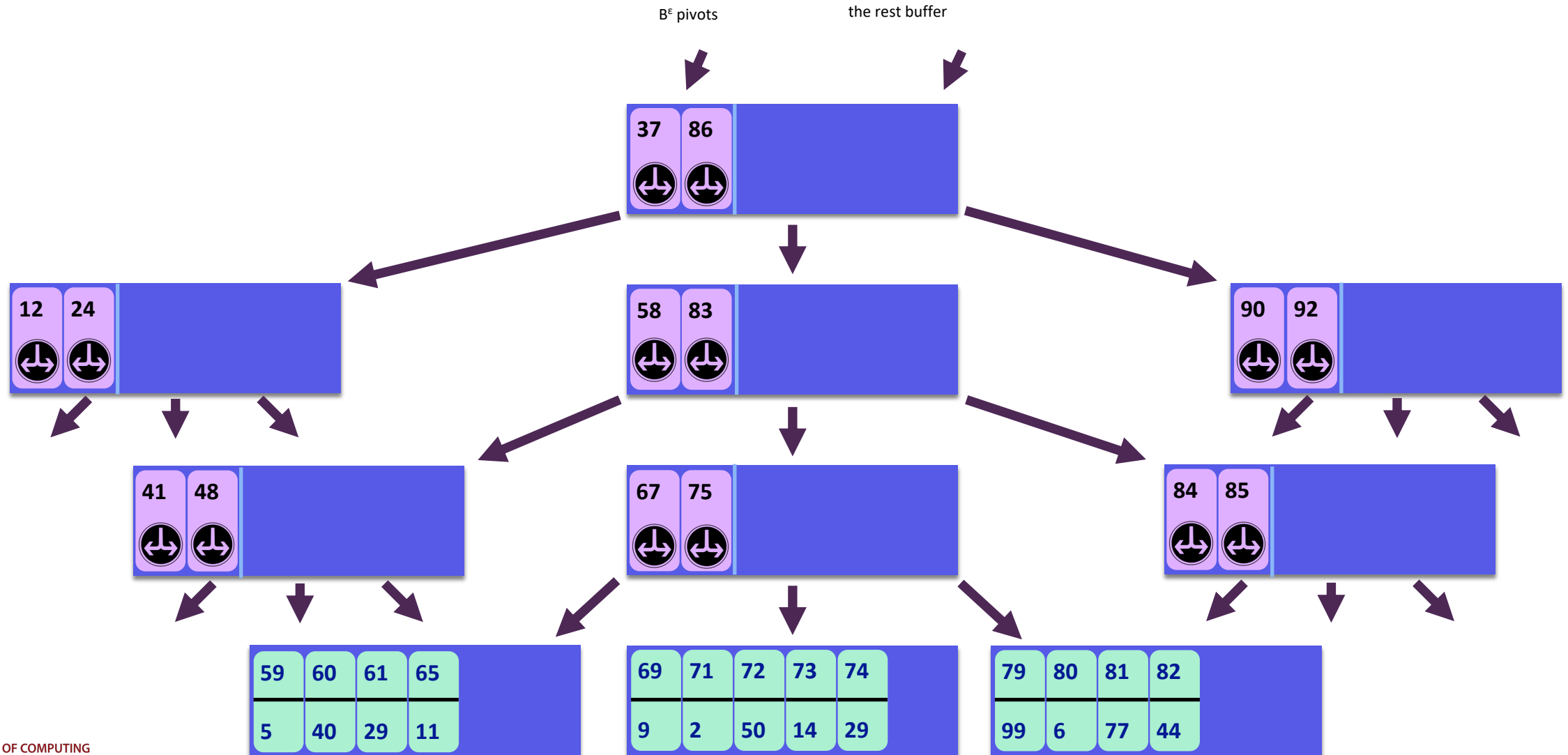
B-ary Search Tree



B^ϵ -Trees

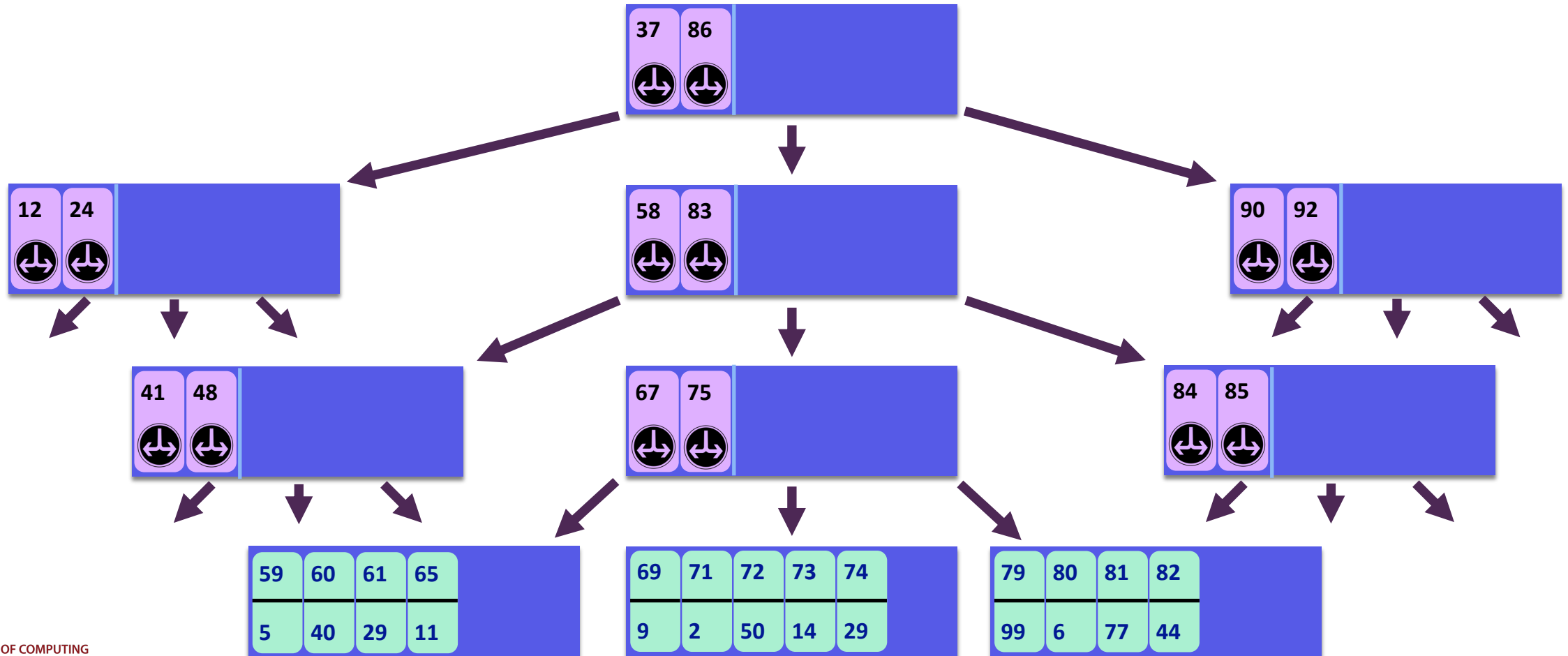
B^ε-Trees

A B^ε-tree is a search tree (like a B-tree)



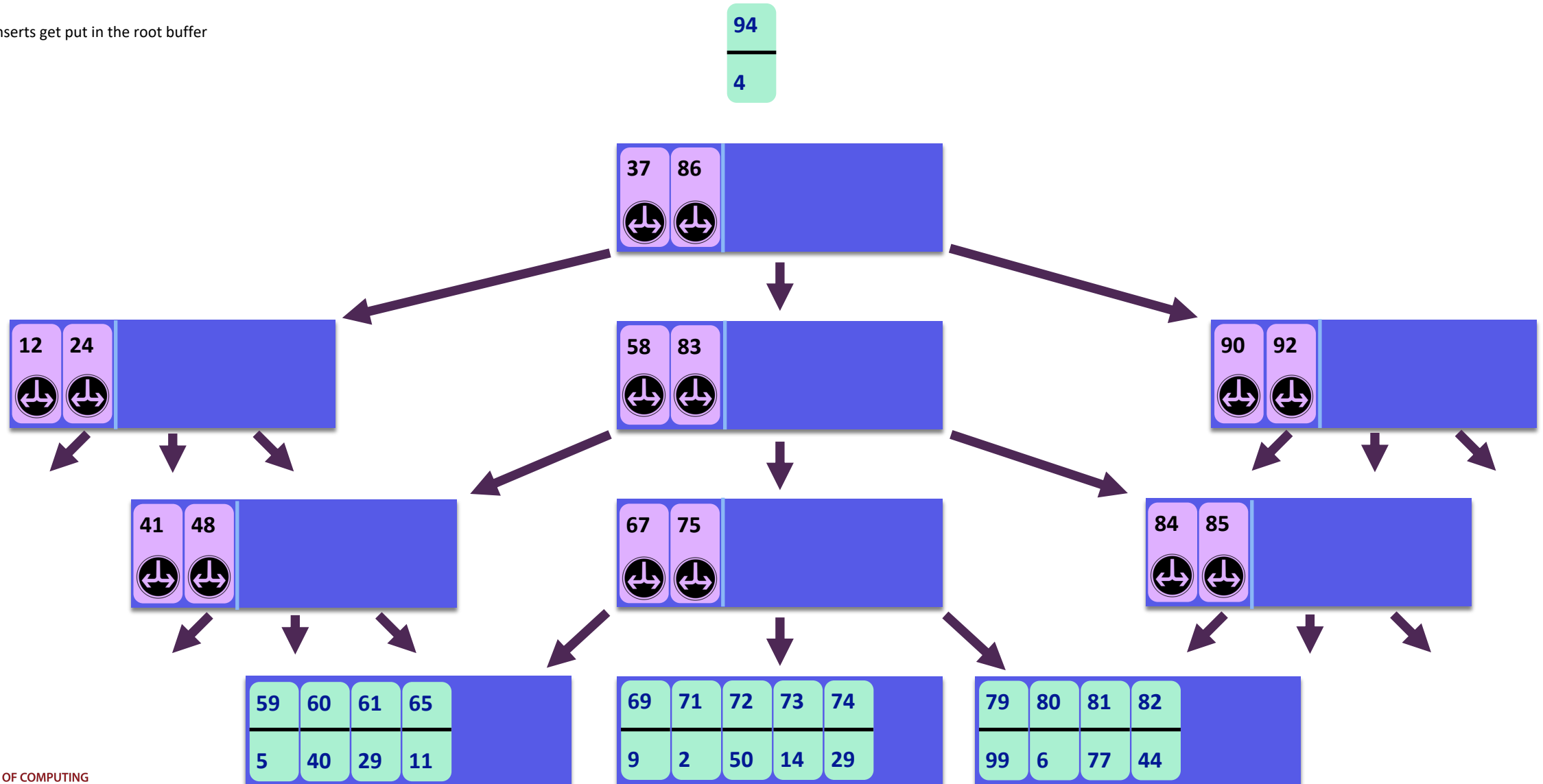
B^ε-Trees

Inserts get put in the root buffer



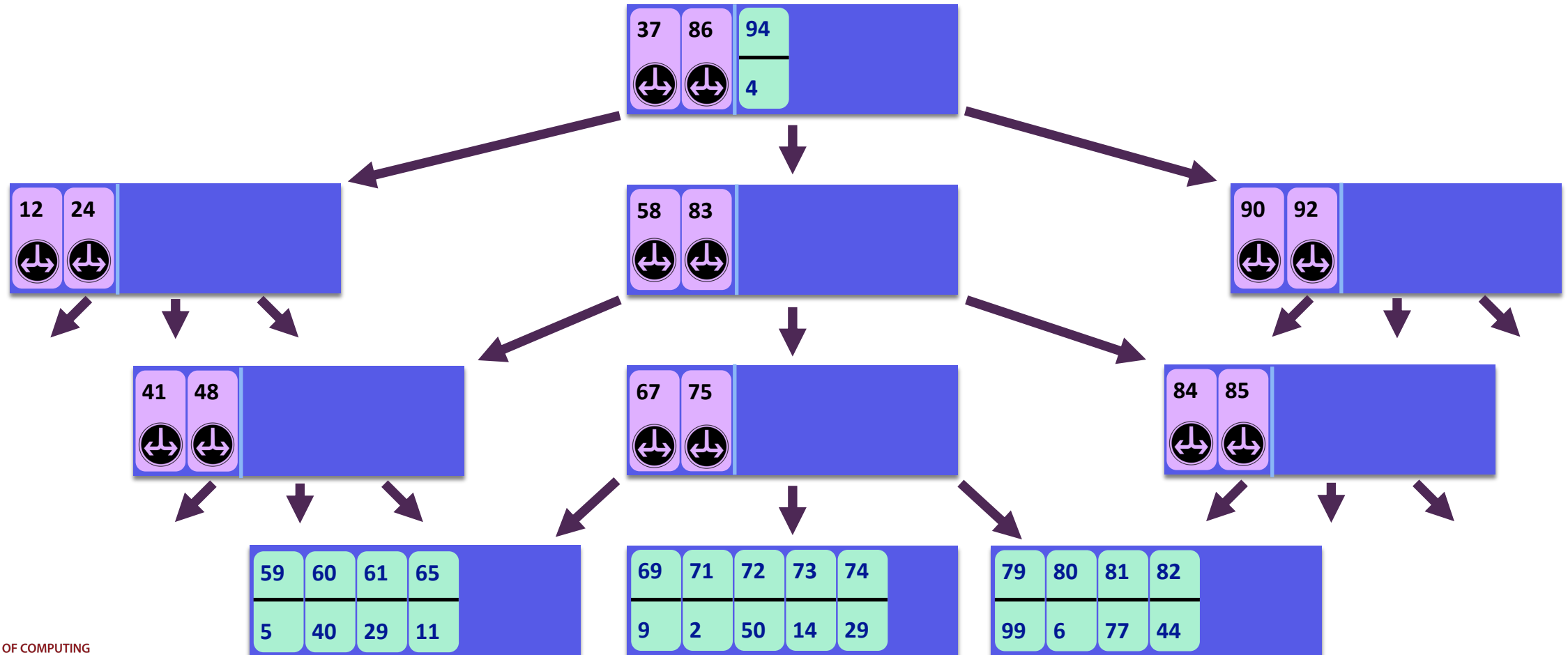
B^ε-Trees

Inserts get put in the root buffer



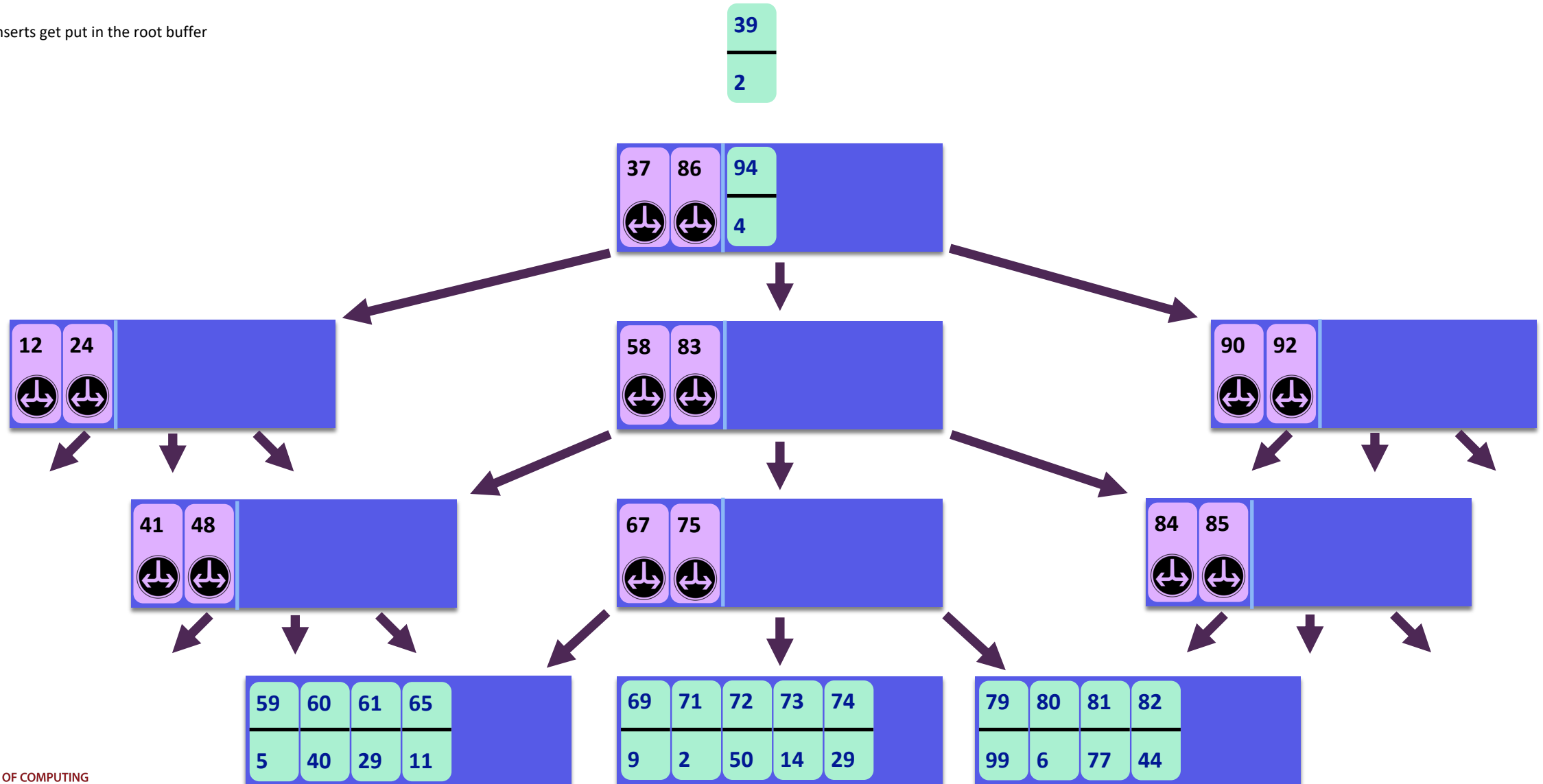
B^ε-Trees

Inserts get put in the root buffer



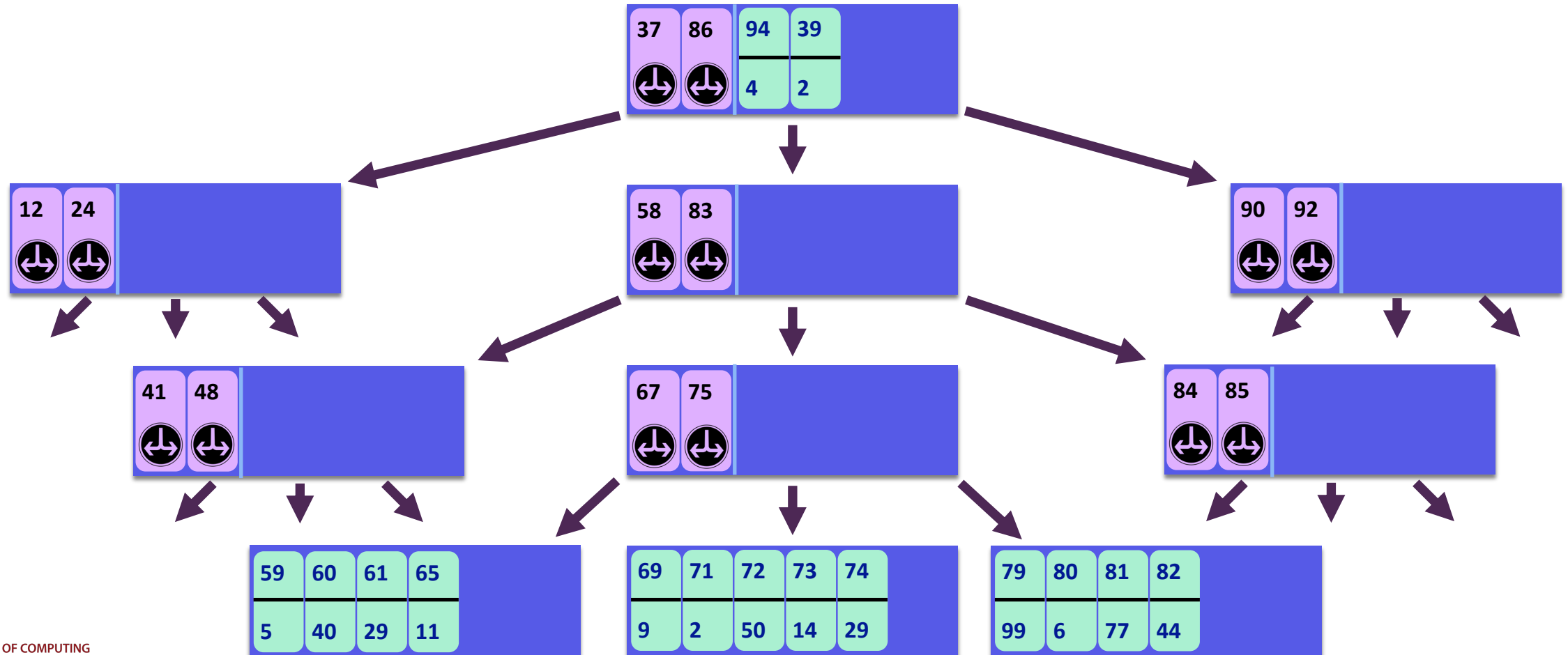
B^ε-Trees

Inserts get put in the root buffer



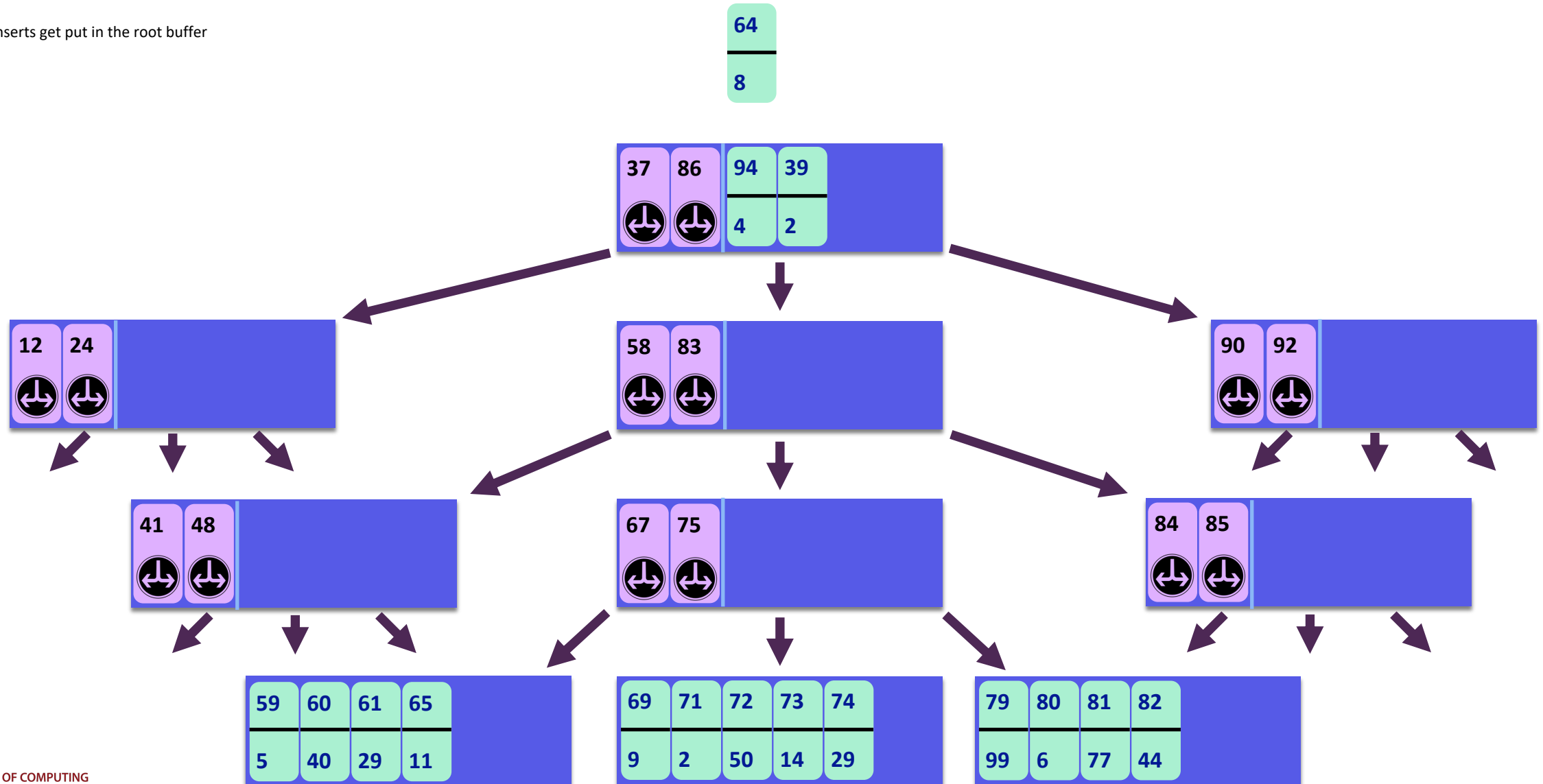
B^ε-Trees

Inserts get put in the root buffer



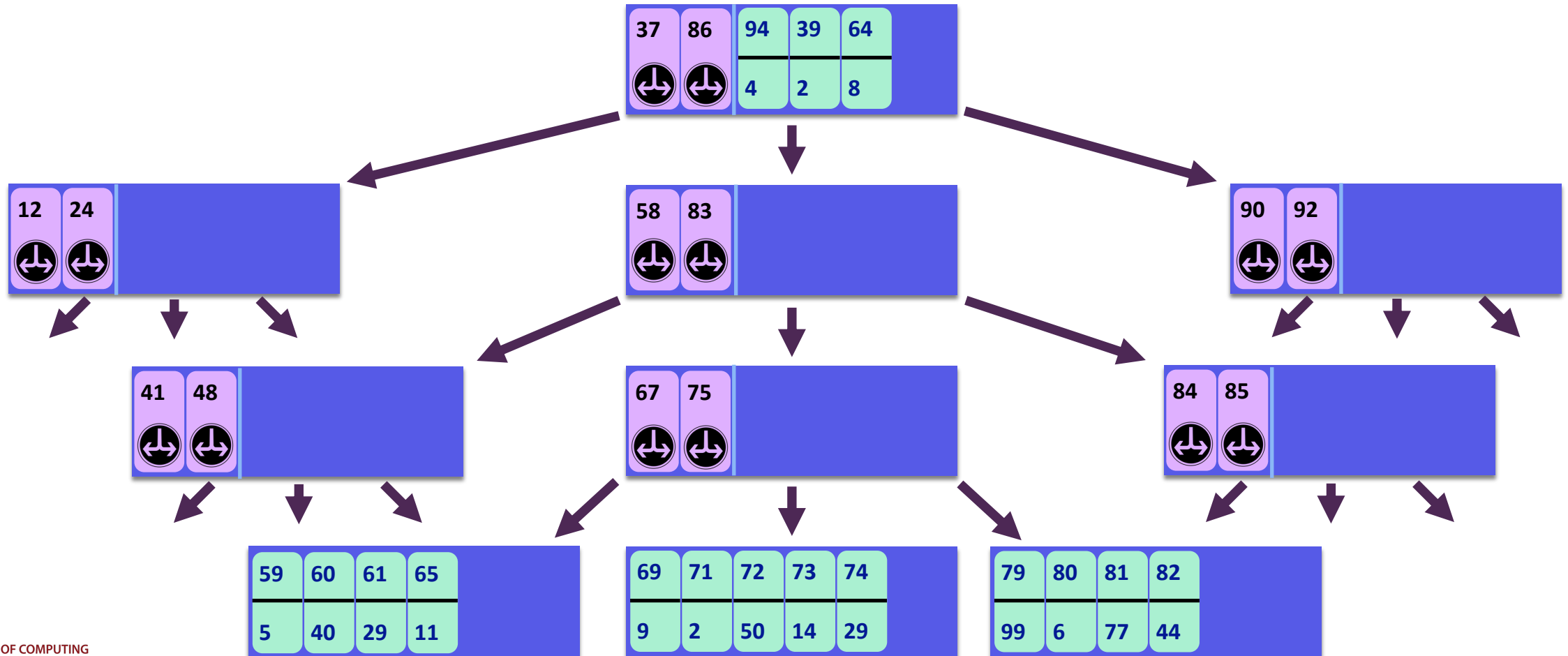
B^ε-Trees

Inserts get put in the root buffer



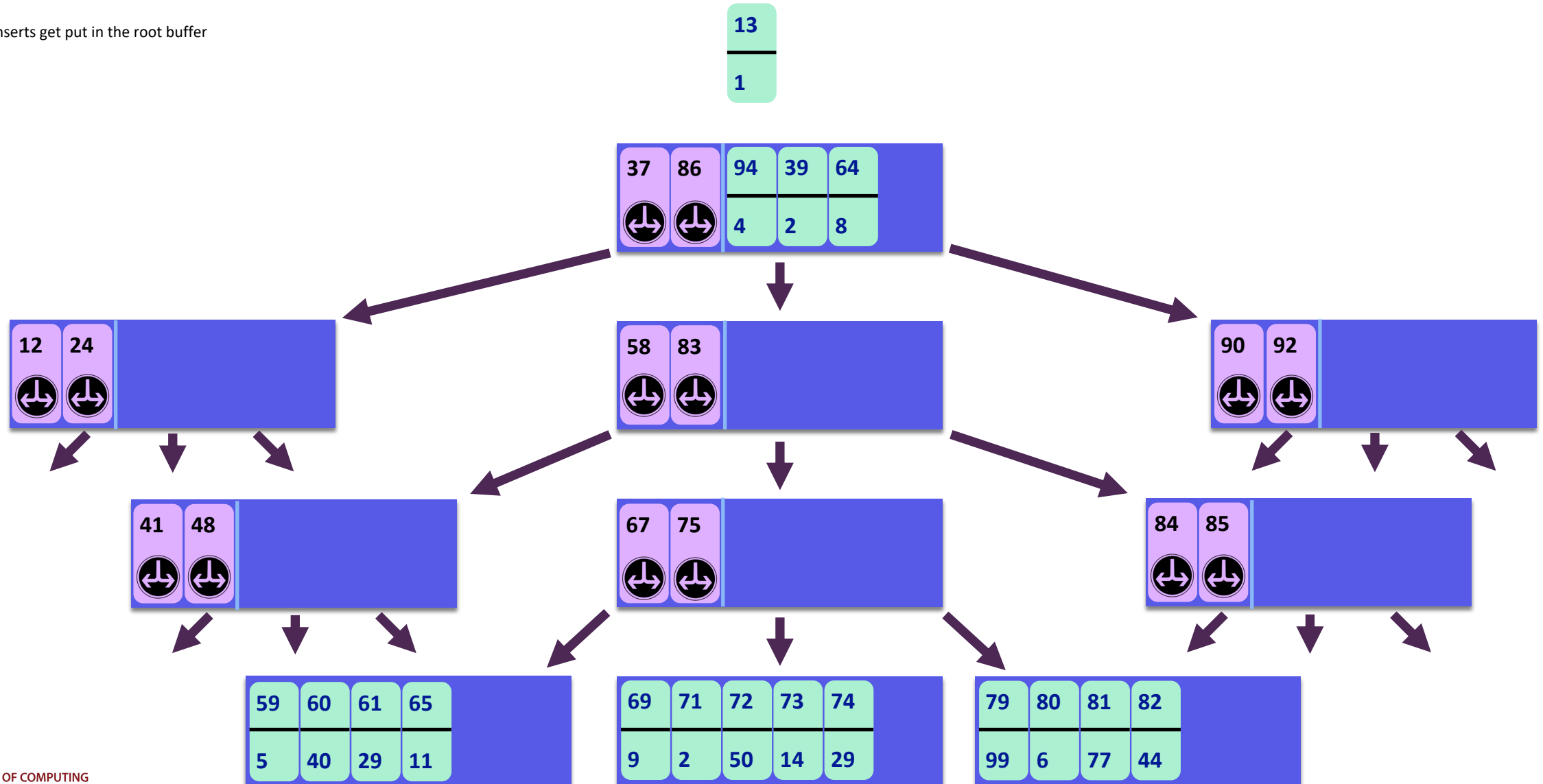
B^ε-Trees

Inserts get put in the root buffer



B^ε-Trees

Inserts get put in the root buffer

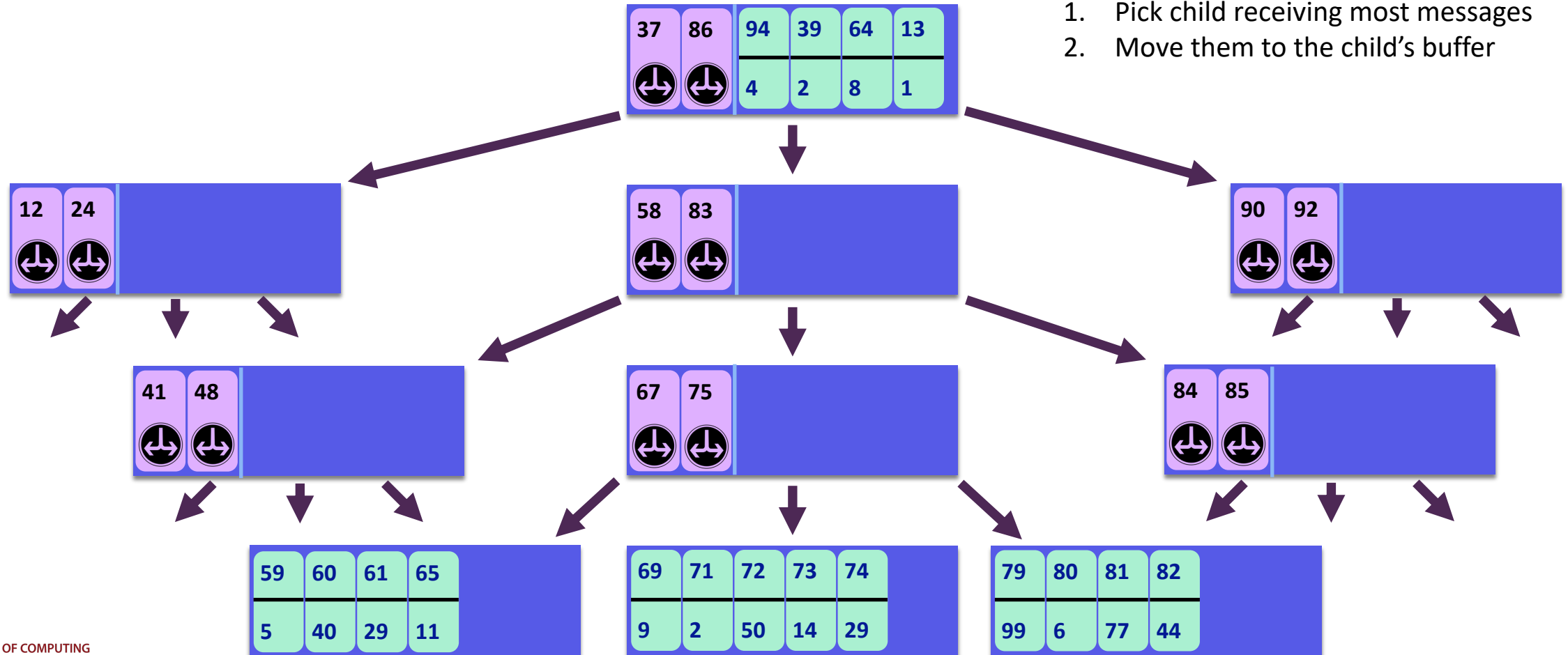


B^ε-Trees

Inserts get put in the root buffer

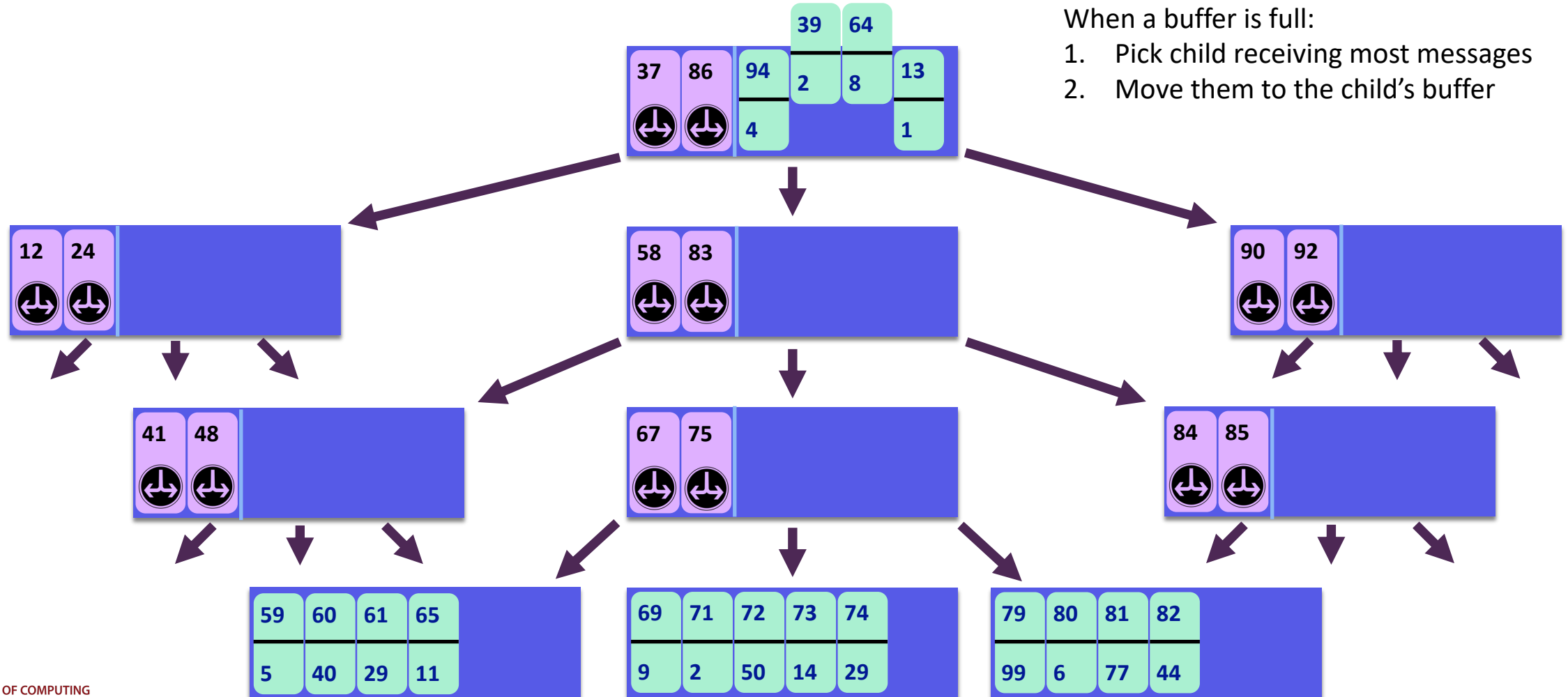
When a buffer is full:

1. Pick child receiving most messages
2. Move them to the child's buffer



B^ε-Trees

Inserts get put in the root buffer

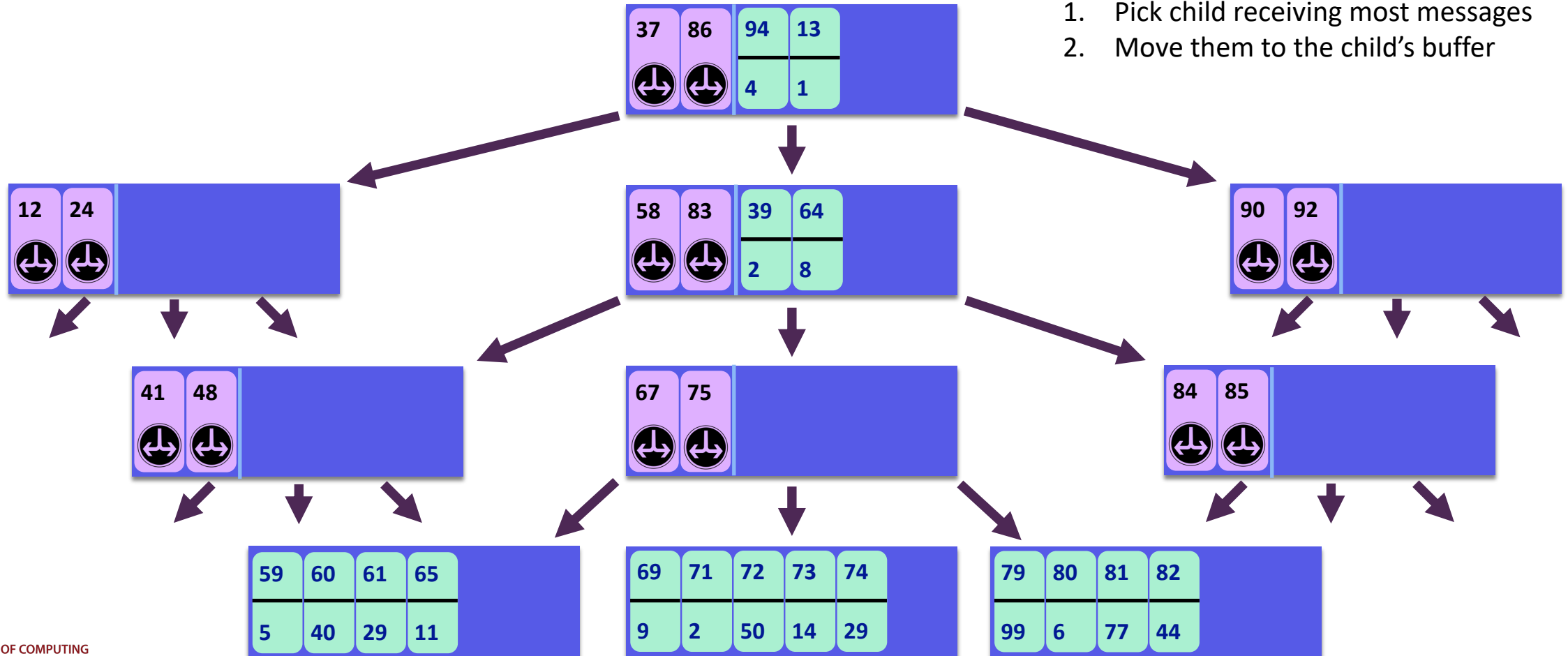


B^ε-Trees

Inserts get put in the root buffer

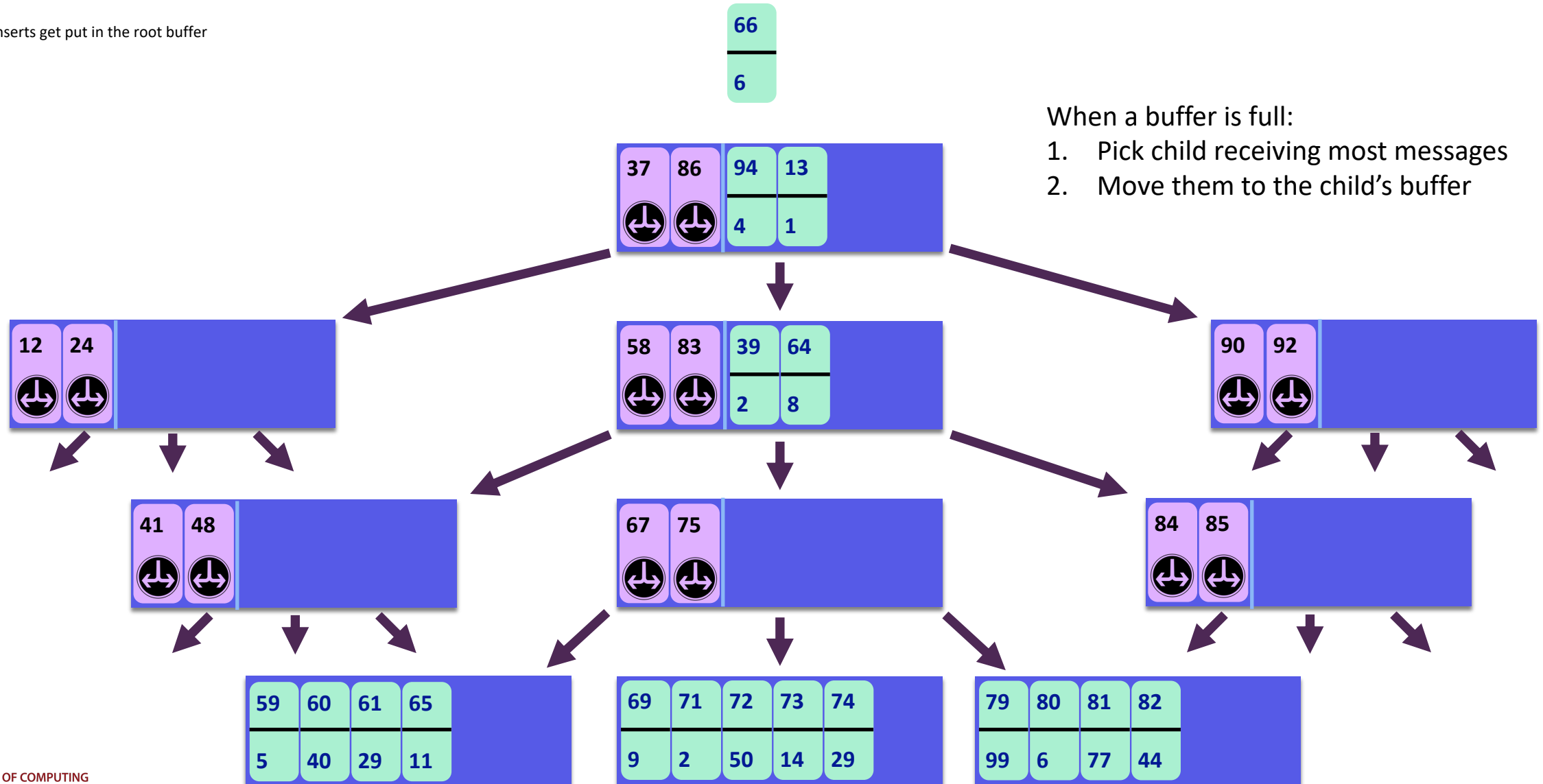
When a buffer is full:

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B^ε-Trees

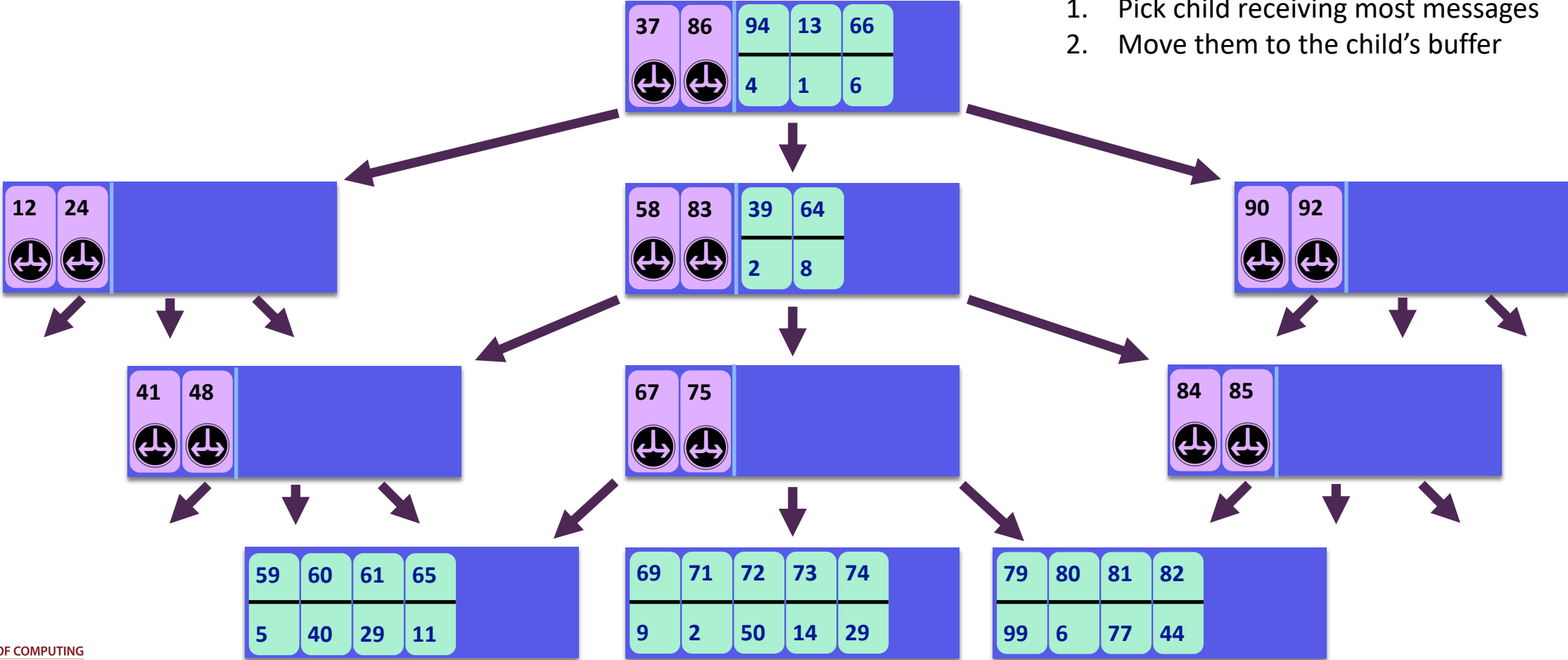
Inserts get put in the root buffer



B-Trees

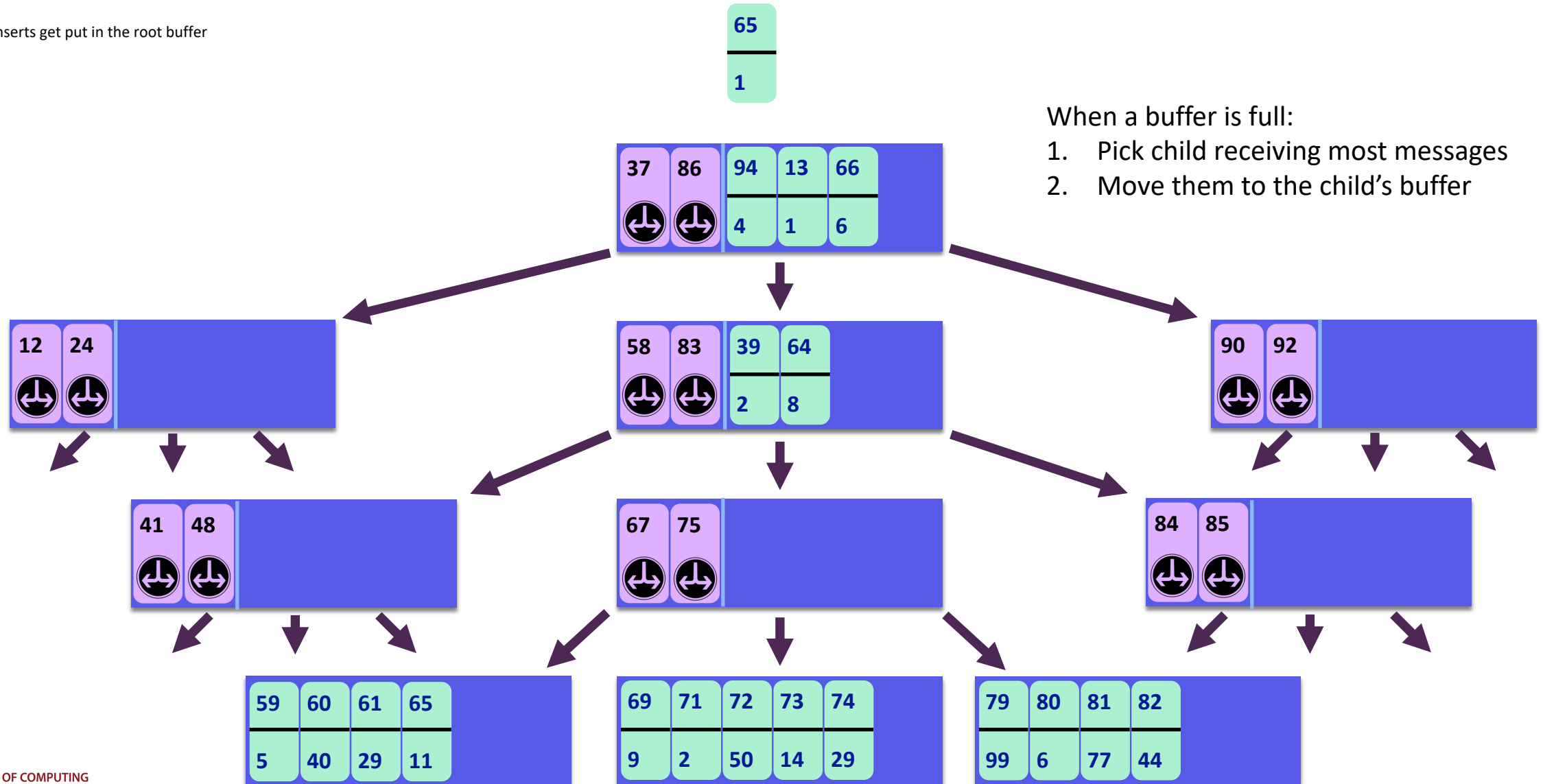
Inserts get put in the root buffer

- When a buffer is full:
1. Pick child receiving most messages
 2. Move them to the child's buffer



B^ε-Trees

Inserts get put in the root buffer

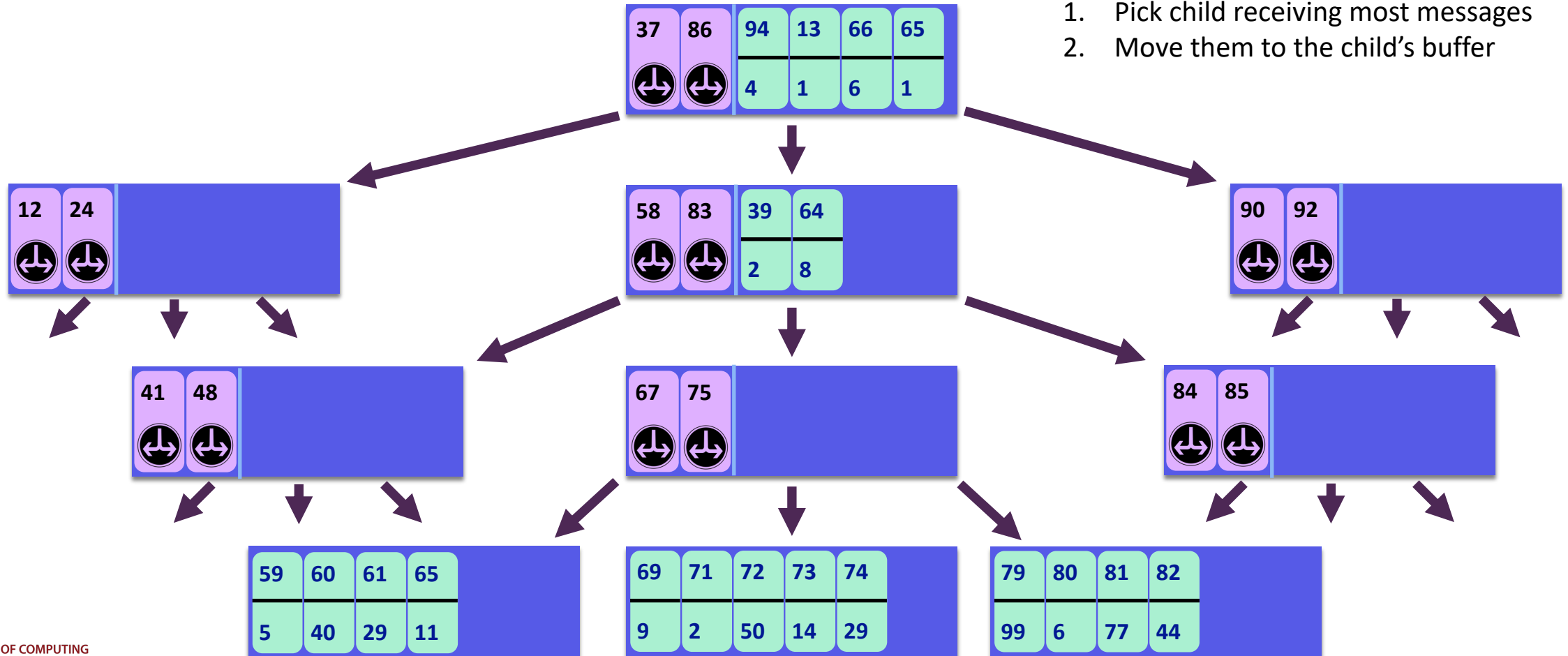


B^ε-Trees

Inserts get put in the root buffer

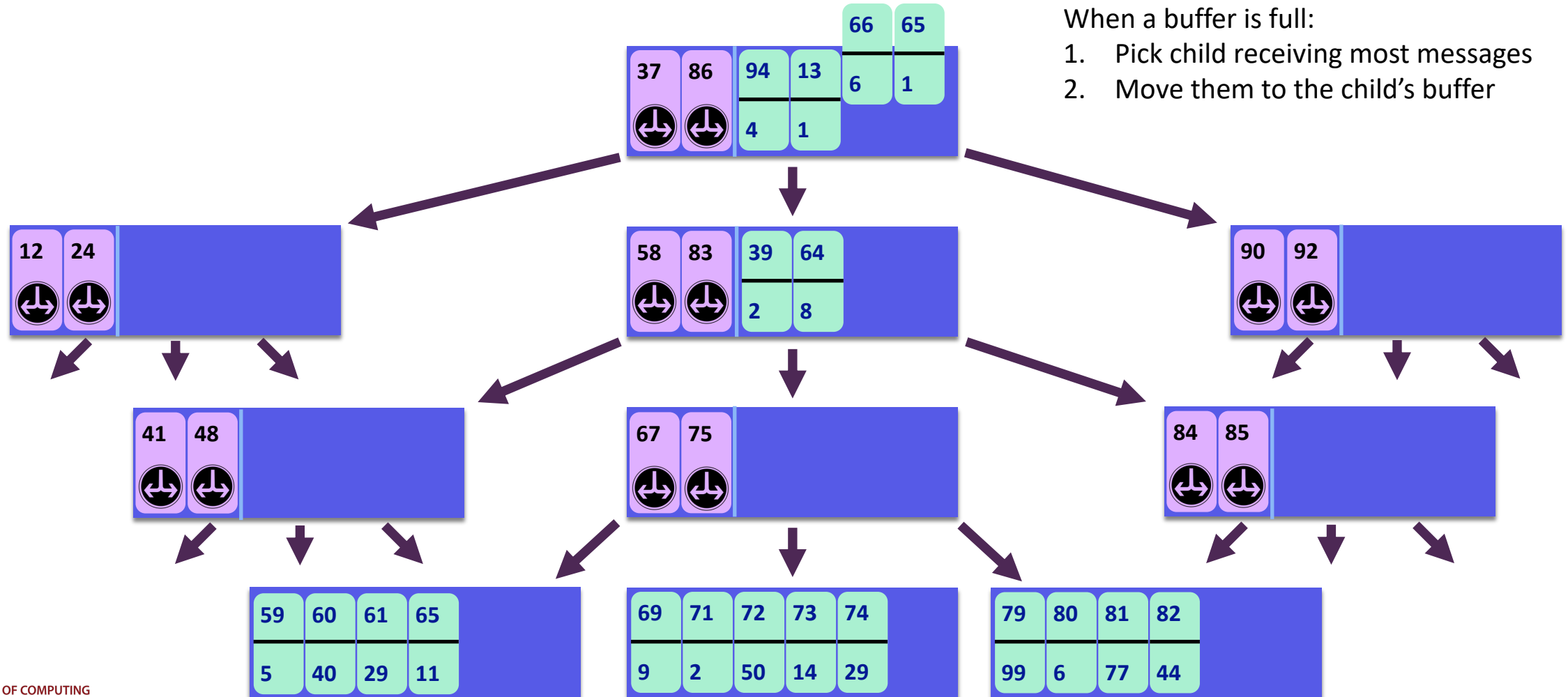
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B^ε-Trees

Inserts get put in the root buffer

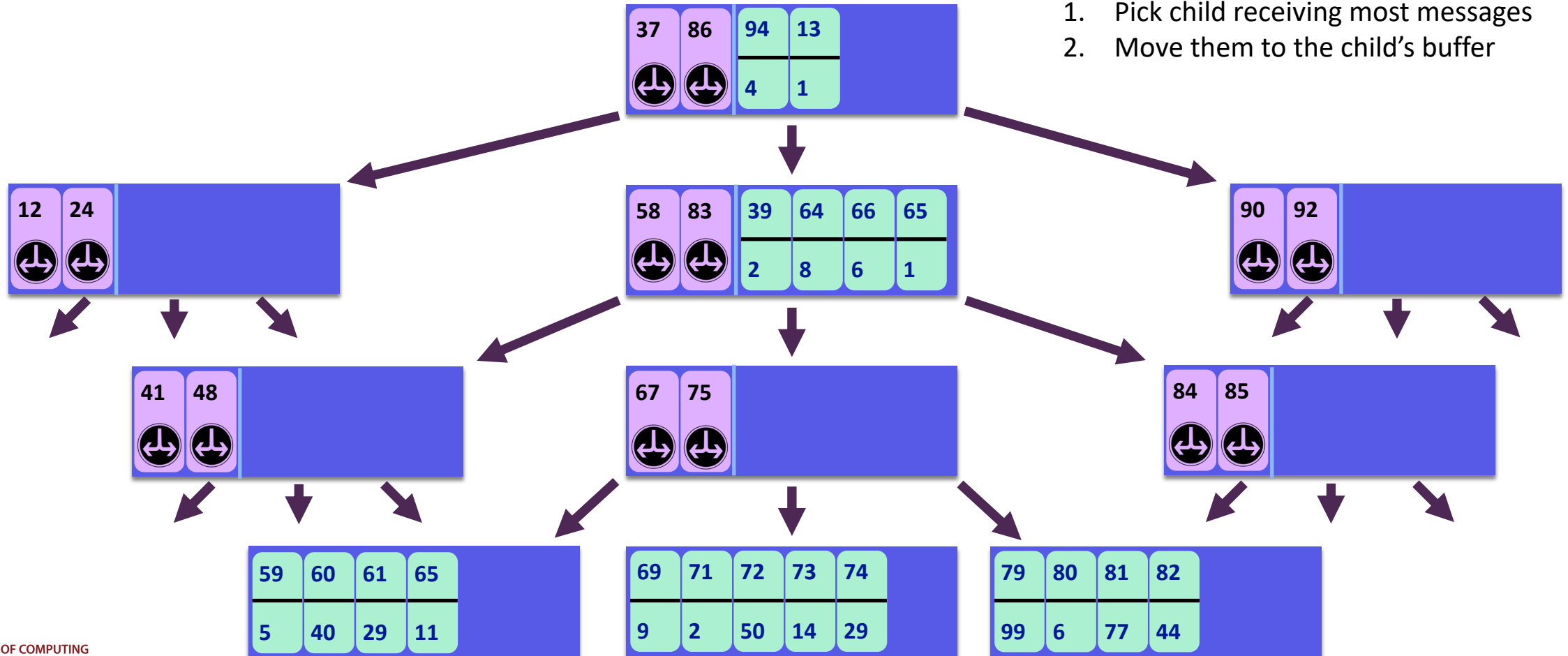


B^ε-Trees

Inserts get put in the root buffer

When a buffer is full:

1. Pick child receiving most messages
2. Move them to the child's buffer

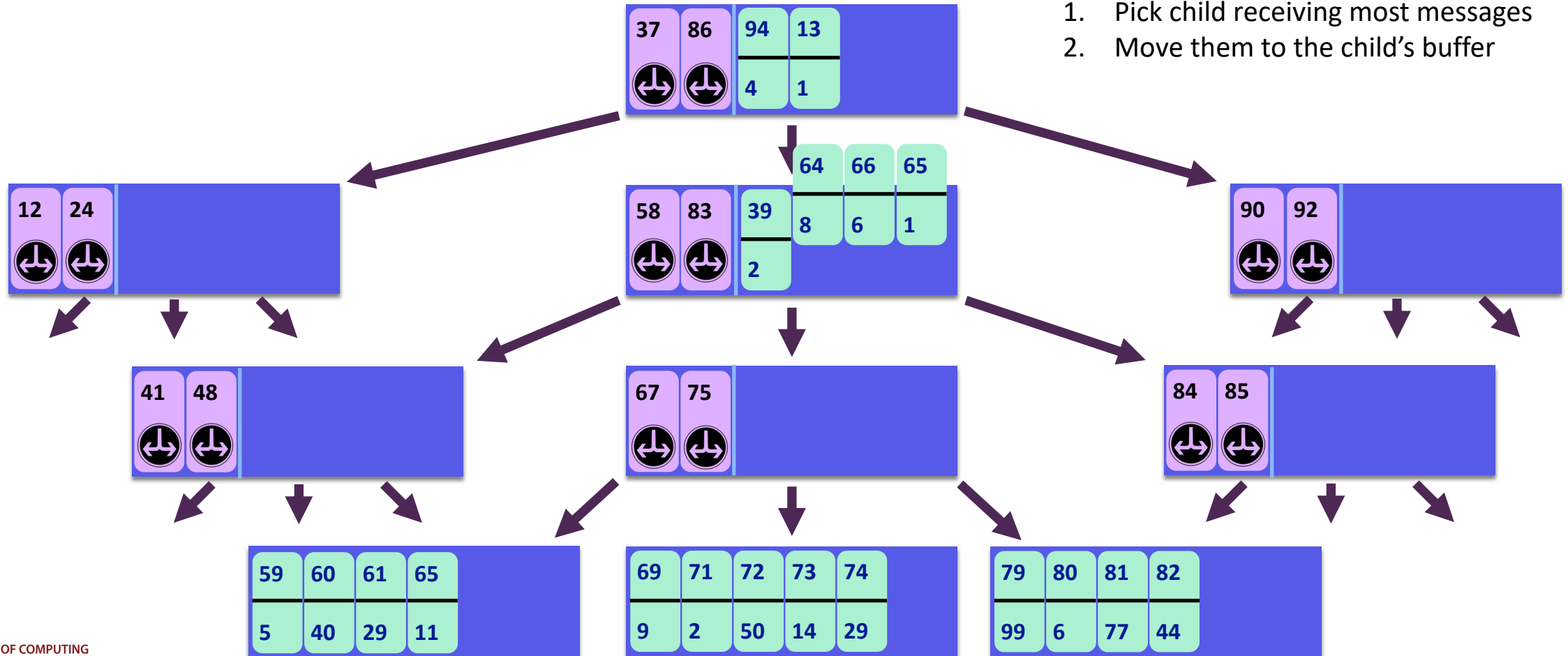


B^ε-Trees

Inserts get put in the root buffer

When a buffer is full:

1. Pick child receiving most messages
2. Move them to the child's buffer

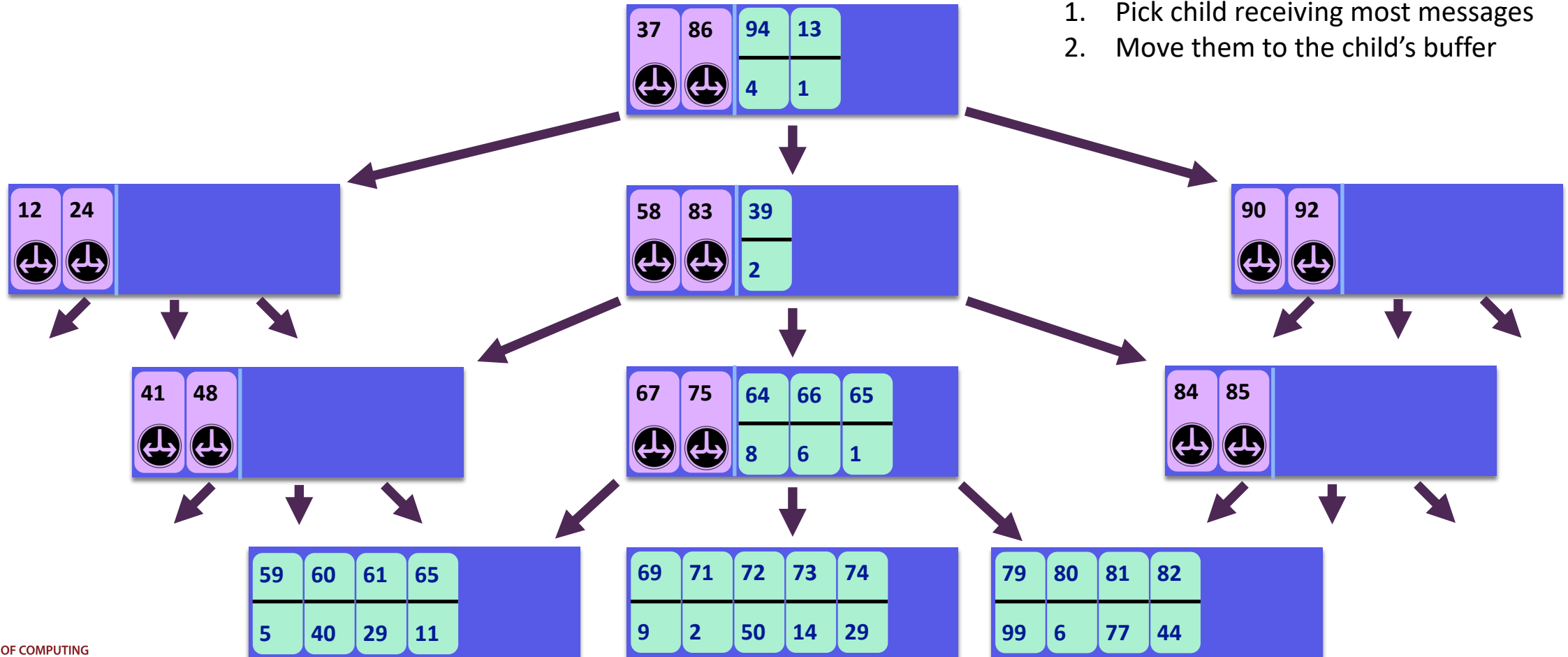


B^ε-Trees

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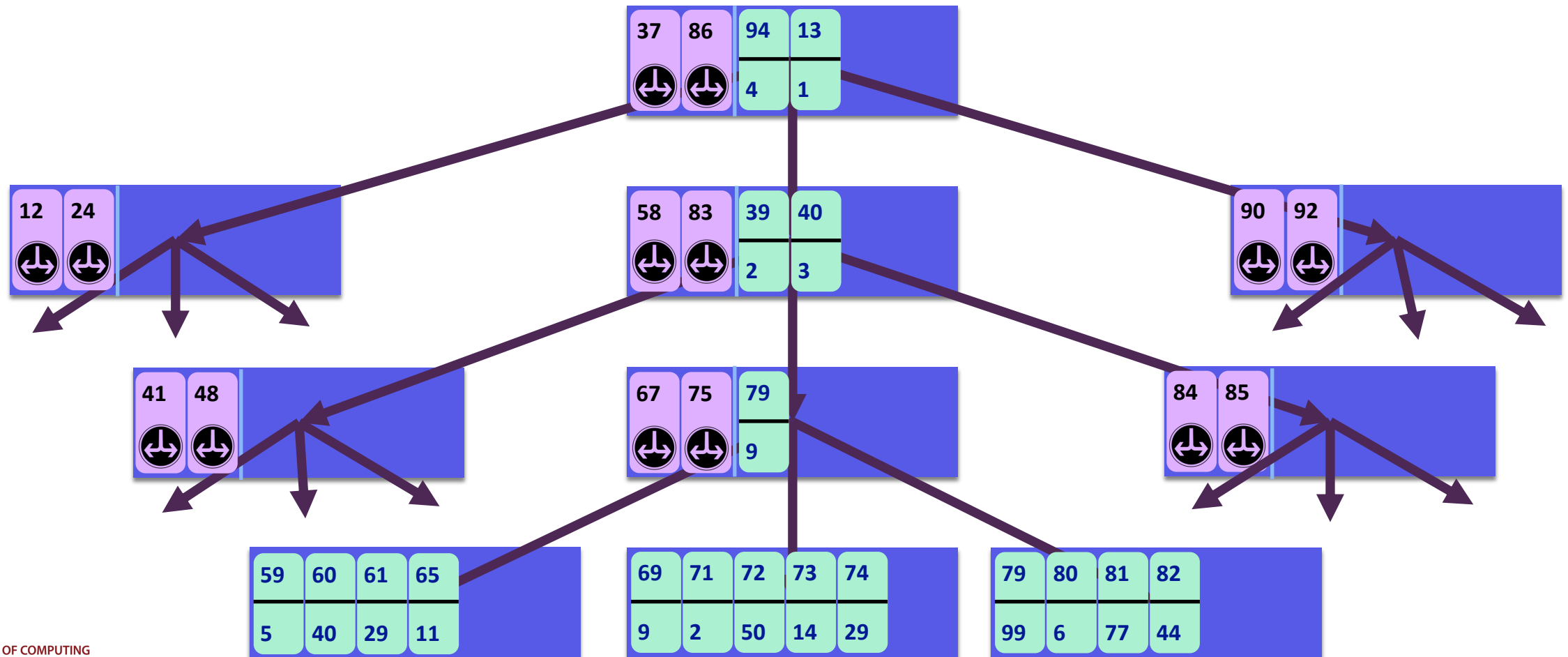


Lookups in B^ϵ -Trees

B^ε-Trees

Query(71)

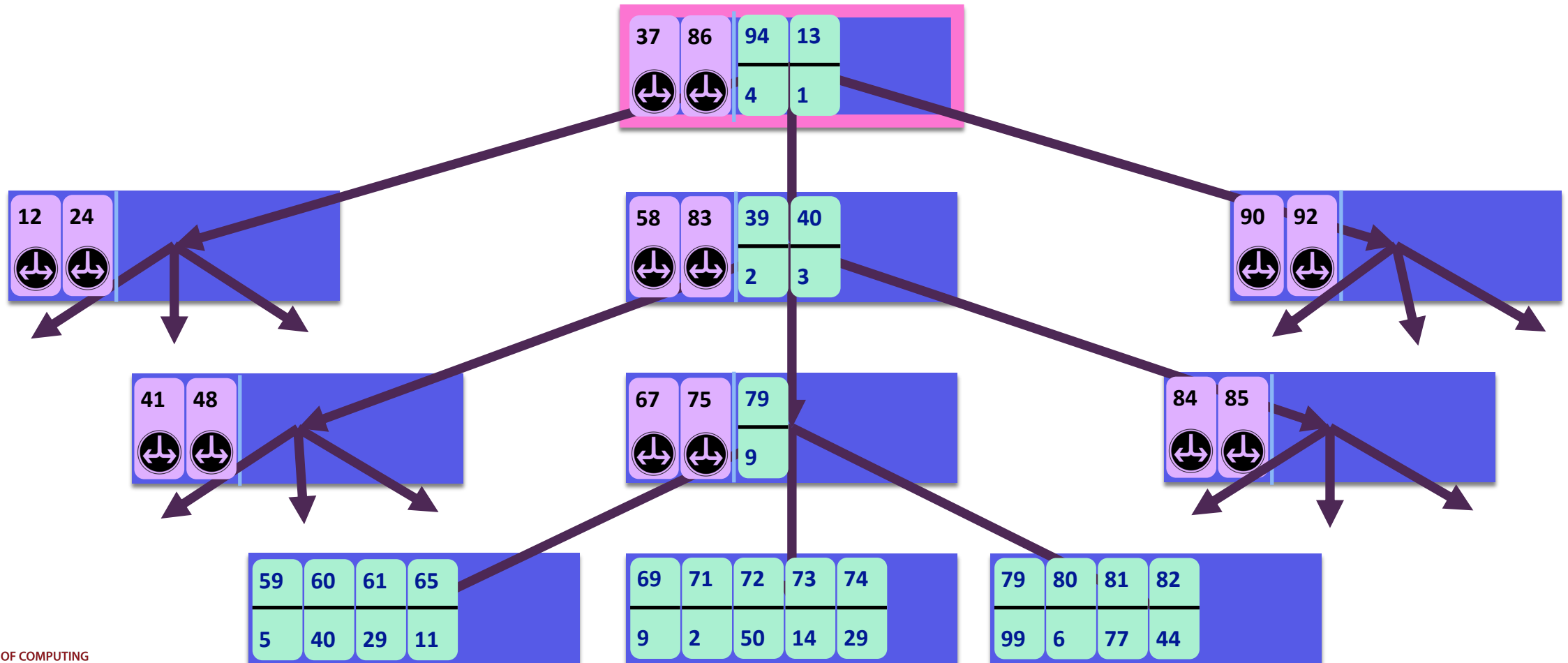
Lookups follow pivots, but check buffers along the way



B^ε-Trees

Query(71)

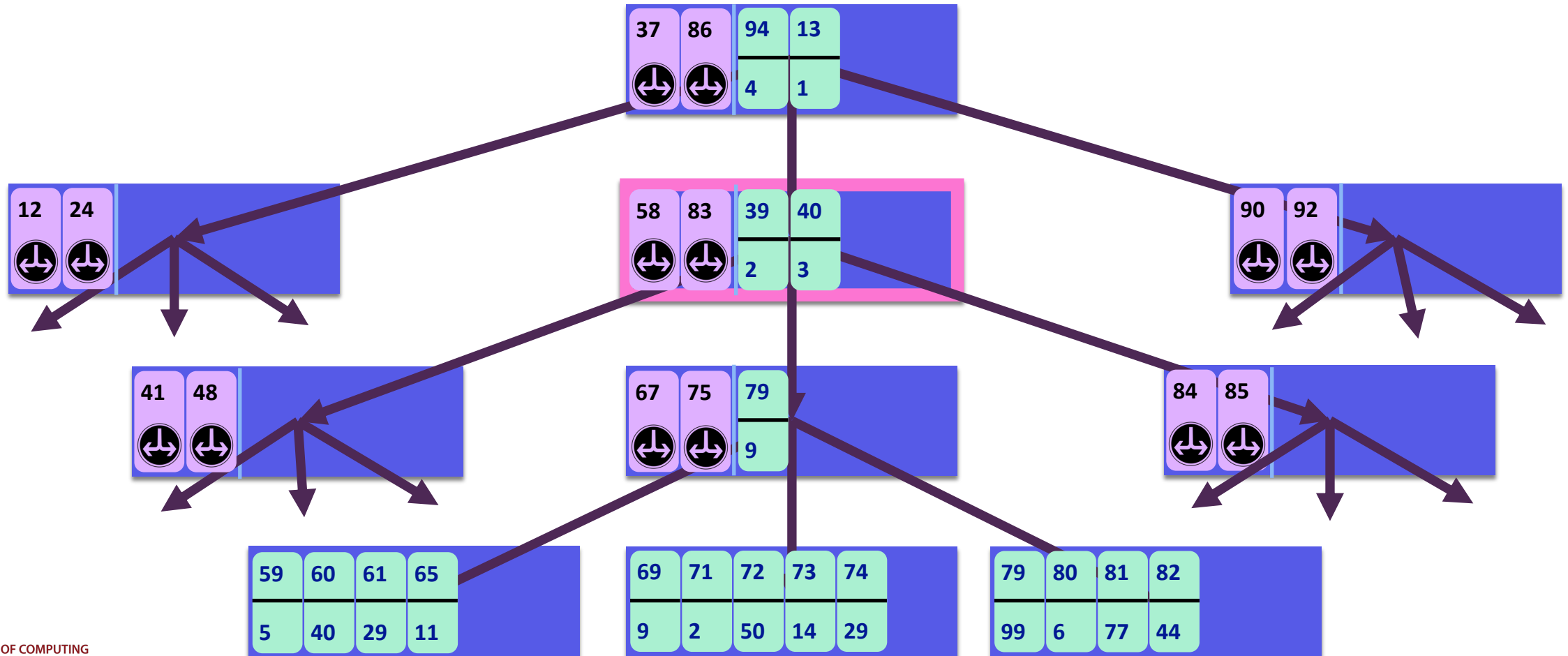
Lookups follow pivots, but check buffers along the way



B^ε-Trees

Query(71)

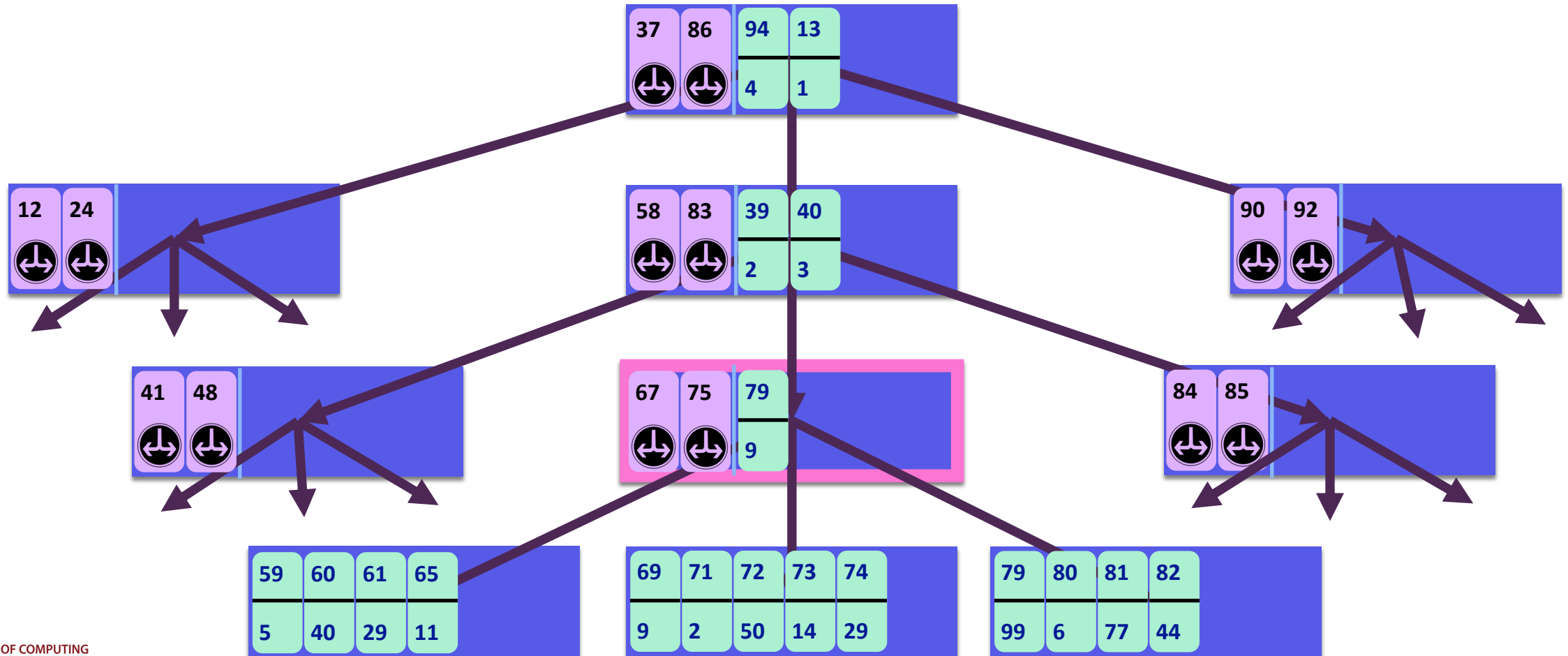
Lookups follow pivots, but check buffers along the way



B^ε-Trees

Query(71)

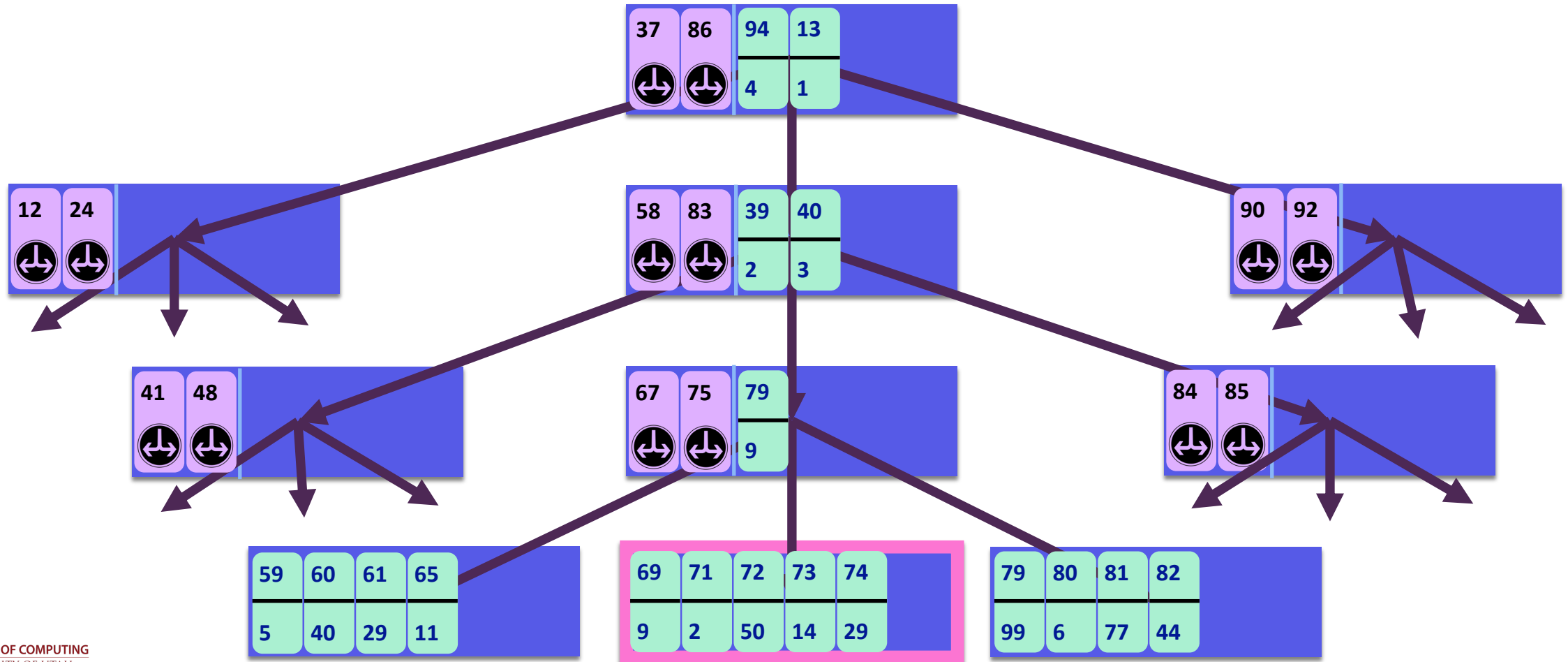
Lookups follow pivots, but check buffers along the way



B^ε-Trees

Lookups follow pivots, but check buffers along the way

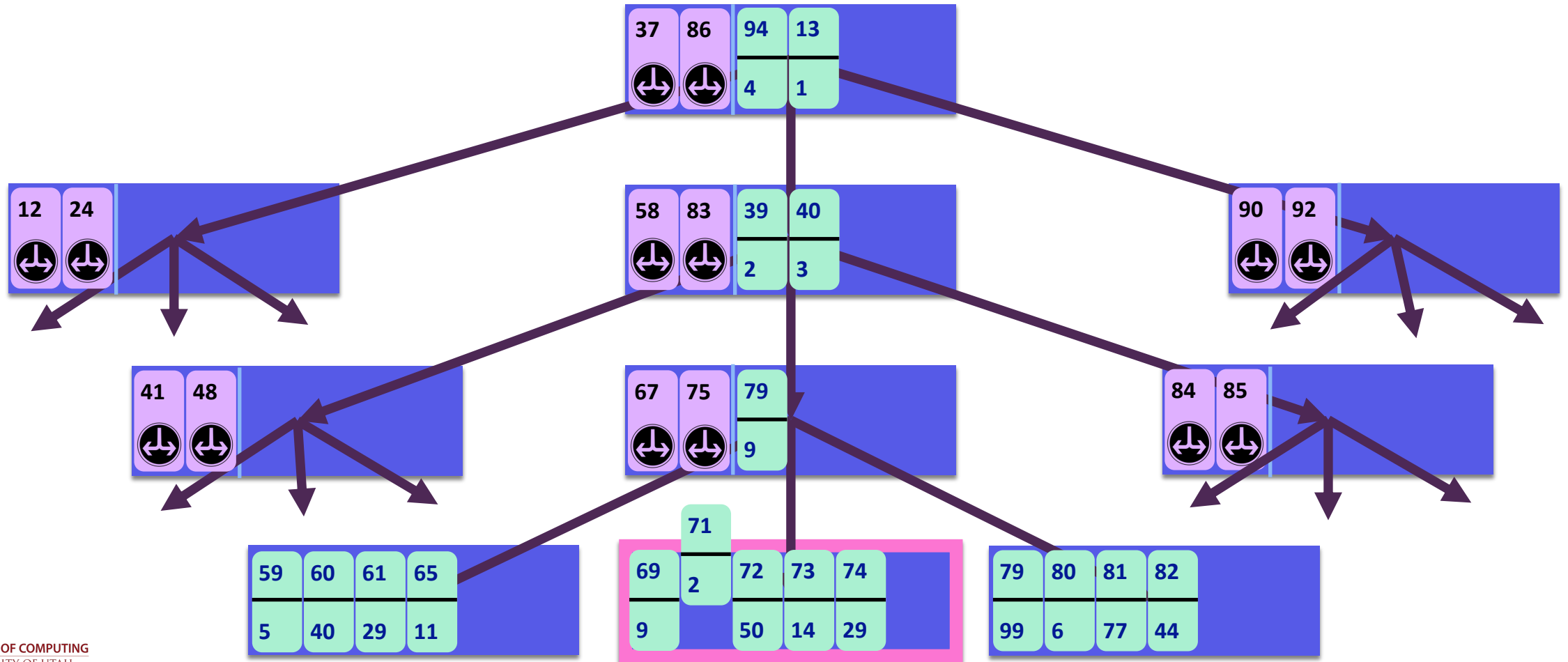
Query(71) → 2



B^ε-Trees

Lookups follow pivots, but check buffers along the way

Query(71) → 2



Insertions in B^ϵ -Trees are more expensive than they look

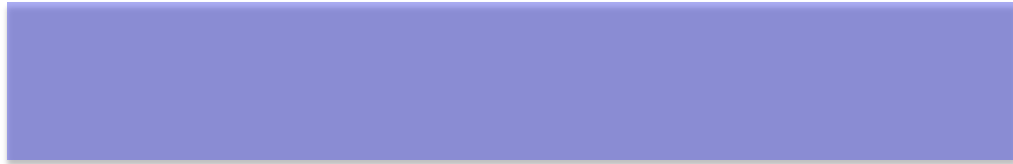
Insertions in B^ϵ -Trees are more expensive than they look

(Also most LSMS)

Insertions in B^ϵ -Trees are more expensive than they look

Recall: Insertions in B^ϵ -trees

65	72	80
11	50	6



Insertions in B^ϵ -Trees are more expensive than they look

Recall: Insertions in B^ϵ -trees

65	72	80
11	50	6

58	83	39	64	66
↕	↕	2	8	6

Read the node



Insertions in B^E -Trees are more expensive than they look

Recall: Insertions in B^E -trees

65	72	80
11	50	6

Merge the data



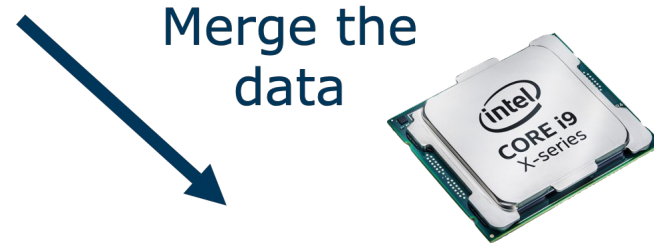
58	83	39	64	66
⬇	⬇	2	8	6

Read the node

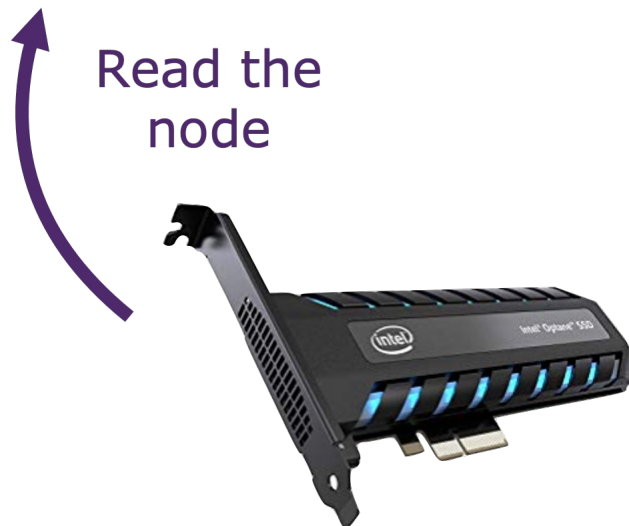


Insertions in B^ϵ -Trees are more expensive than they look

Recall: Insertions in B^ϵ -trees



58	83	39	64	65	66	72	80													
↕	↕	2	8	11	6	50	6													



Insertions in B^ϵ -Trees are more expensive than they look

Recall: Insertions in B^ϵ -trees



58	83	39	64	65	66	72	80													
↕	↕	2	8	11	6	50	6													



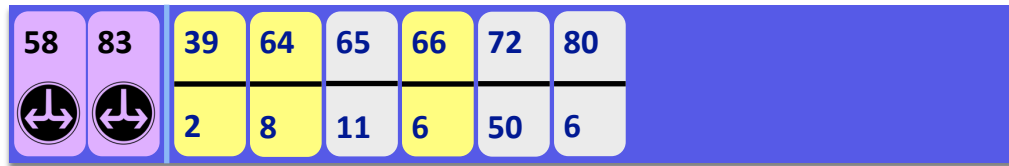
Insertions in B^ϵ -Trees are more expensive than they look

Recall: Insertions in B^ϵ -trees



CPU Work = $O(\text{old} + \text{new})$

Volume of IO = $O(\text{old} + \text{new})$



Insertions in B^ϵ -Trees are more expensive than they look

Recall: Insertions in B^ϵ -trees

98	44
1	3

Merge the data



58	83	39	64	65	66	72	80
⬇	⬇	2	8	11	6	50	6

CPU Work = $O(\text{old} + \text{new})$

Volume of IO = $O(\text{old} + \text{new})$

Older data gets written over and over again

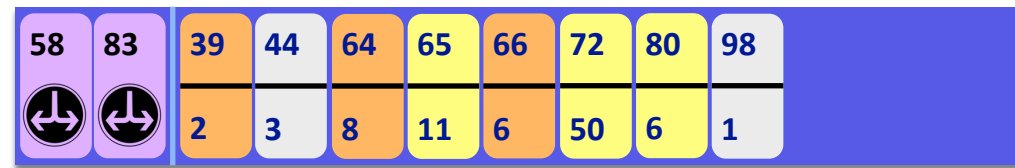
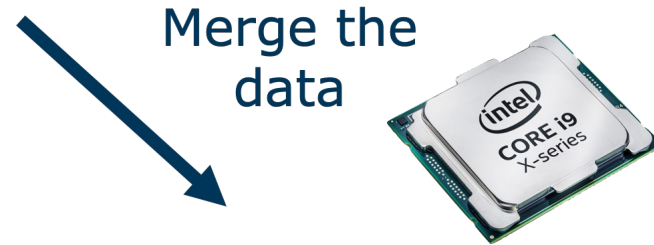
Read the node

Write the node



Insertions in B^ϵ -Trees are more expensive than they look

Recall: Insertions in B^ϵ -trees



CPU Work = $O(\text{old} + \text{new})$

Volume of IO = $O(\text{old} + \text{new})$

Older data gets written over and over again

Insertions in B^ϵ -Trees are more expensive than they look

Recall: Insertions in B^ϵ -trees

28	91
24	43

Merge the data



58	83	39	44	64	65	66	72	80	98
2	3	8	11	6	50	6	1		

Read the node

Write the node



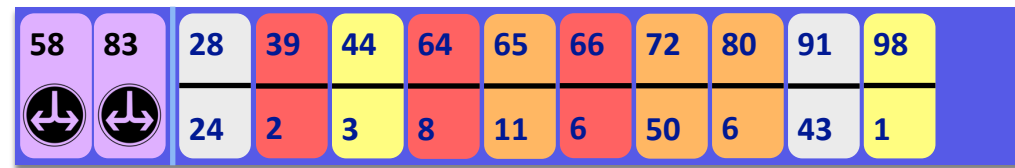
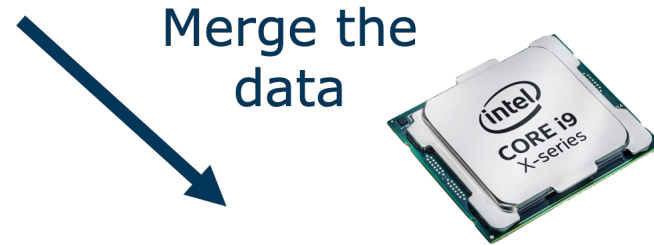
CPU Work = $O(\text{old} + \text{new})$

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Insertions in B^ϵ -Trees are more expensive than they look

Recall: Insertions in B^ϵ -trees



CPU Work = $O(\text{old} + \text{new})$

Volume of IO = $O(\text{old} + \text{new})$

Older data gets written over and over again

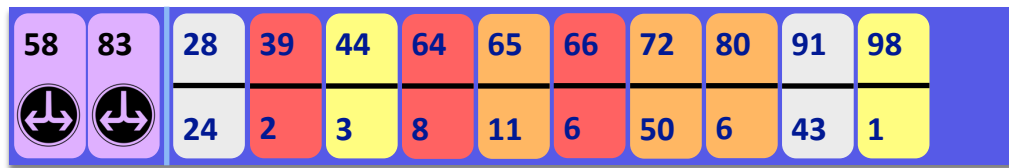
Insertions in B^ϵ -Trees are more expensive than they look

Recall: Insertions in B^ϵ -trees



CPU Work = $O(\text{old} + \text{new})$

Volume of IO = $O(\text{old} + \text{new})$



Older data gets written over and over again



Up to B^ϵ times per node!

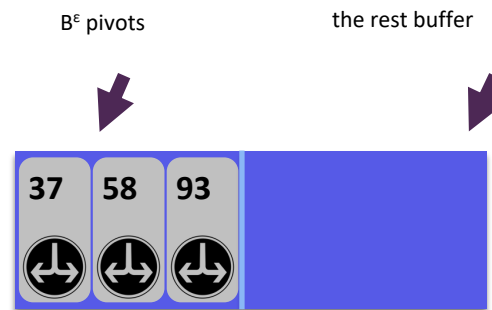
Size-Tiered B^ϵ -Trees

SplinterDB: Closing the Bandwidth Gap for NVMe Key-Value Stores
Conway, Gupta, Chidambaram, Farach-Colton, Spillane, Tai, Johnson,
ATC 2020

Size-Tiered B^ϵ -Trees

A Size-Tiered B^ϵ -tree is a B^ϵ -tree where the buffer is stored discontinuously

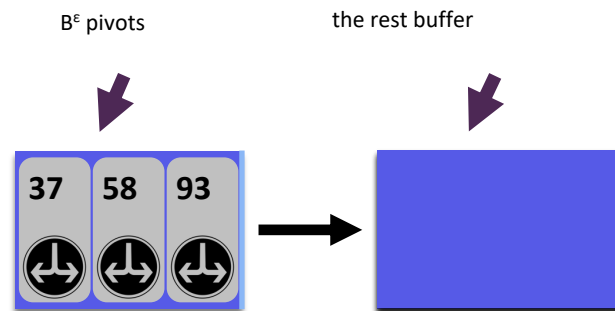
Recall:
a B^ϵ -tree node has pivots and a buffer



Size-Tiered B^ϵ -Trees

A Size-Tiered B^ϵ -tree is a B^ϵ -tree where the buffer is stored discontinuously

Recall:
a B^ϵ -tree node has pivots and a buffer

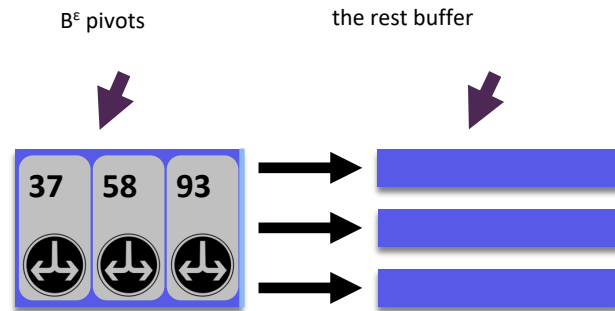


In an STB^ϵ -tree, the buffer is stored separately

Size-Tiered B^ϵ -Trees

A Size-Tiered B^ϵ -tree is a B^ϵ -tree where the buffer is stored discontinuously

Recall:
a B^ϵ -tree node has pivots and a buffer

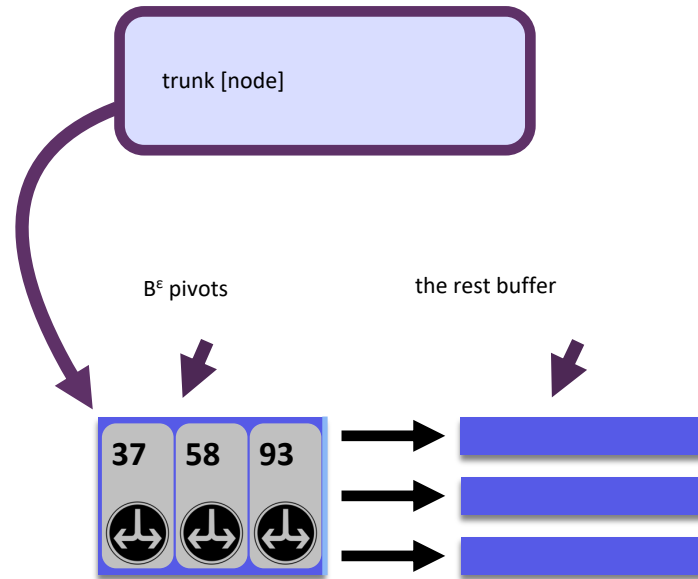


and in several discontinuous pieces

In an STB^ϵ -tree, the buffer is stored separately

Size-Tiered B^ϵ -Trees

A Size-Tiered B^ϵ -tree is a B^ϵ -tree where the buffer is stored discontinuously



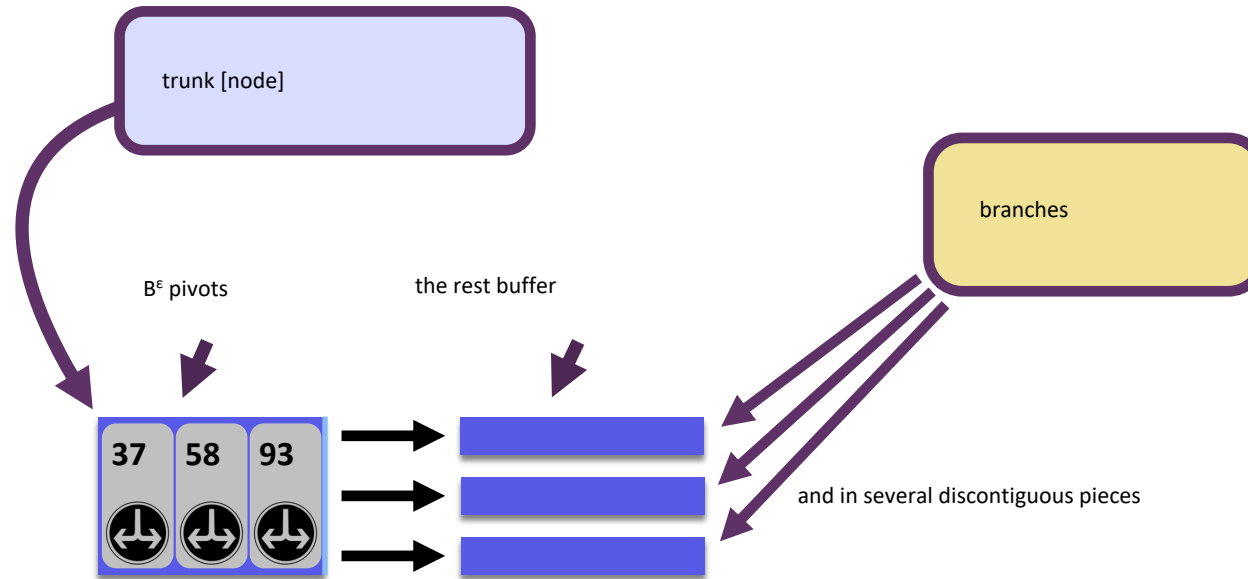
Recall:
a B^ϵ -tree node has pivots and a buffer

In an STB^ϵ -tree, the buffer is stored separately

and in several discontinuous pieces

Size-Tiered B^ϵ -Trees

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Recall:
a B^ϵ -tree node has pivots and a buffer

In an STB^ϵ -tree, the buffer is stored separately

Insertions in Size-Tiered B^ϵ -Trees

Size-Tiered B^ϵ -Trees

A Size-Tiered B^ϵ -tree is a B^ϵ -tree where the buffer is stored discontinuously

When new data is flushed into the trunk node...



Size-Tiered B^ε-Trees

A Size-Tiered B^ε-tree is a B^ε-tree where the buffer is stored discontinuously

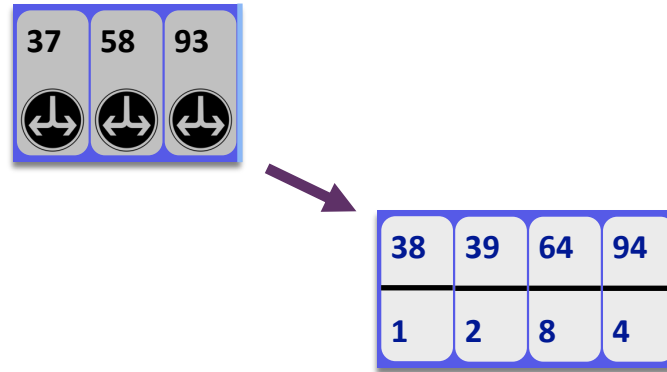
38	39	64	94
1	2	8	4

When new data is flushed into the trunk node...

37	58	93
		

Size-Tiered B^ε-Trees

A Size-Tiered B^ε-tree is a B^ε-tree where the buffer is stored discontinuously

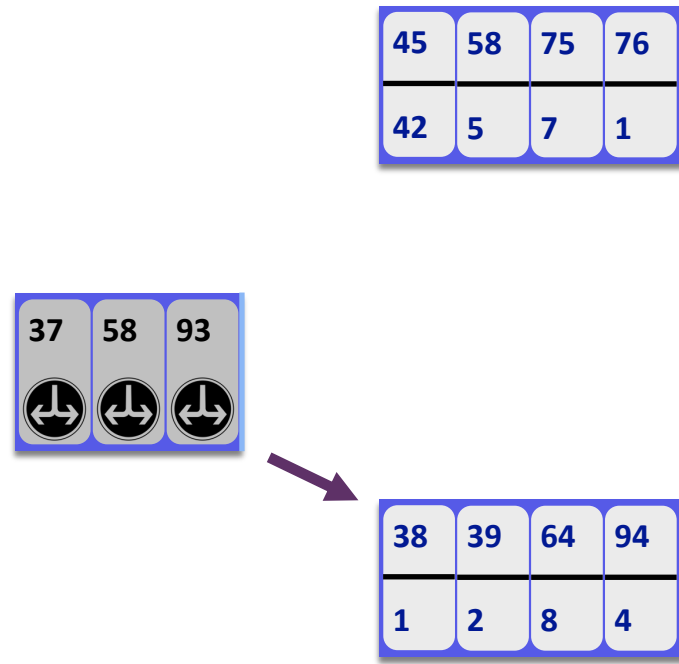


When new data is flushed into the trunk node...

...it is added as a new branch

Size-Tiered B^ε-Trees

A Size-Tiered B^ε-tree is a B^ε-tree where the buffer is stored discontinuously

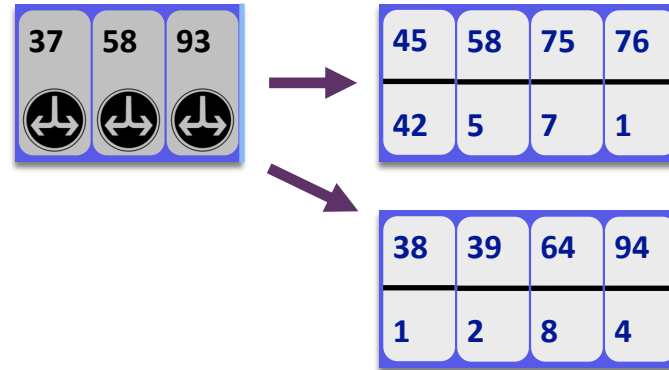


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When new data is flushed into the trunk node...

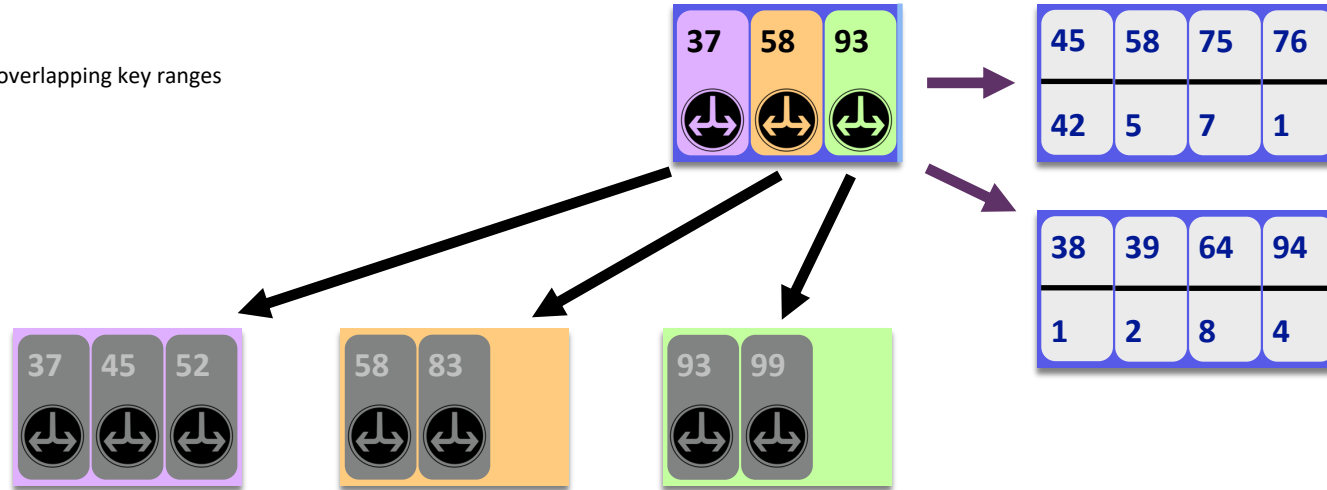
...it is added as a new branch

The old branches do not need to be rewritten

Size-Tiered B^ε-Trees

A Size-Tiered B^ε-tree is a B^ε-tree where the buffer is stored discontinuously

Branches may have overlapping key ranges



When new data is flushed into the trunk node...

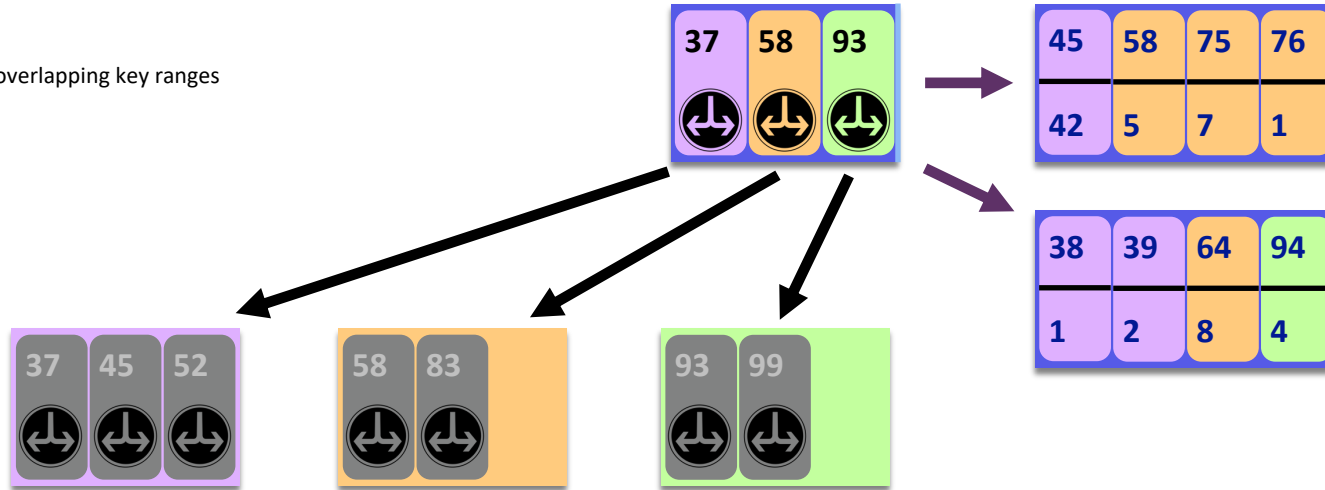
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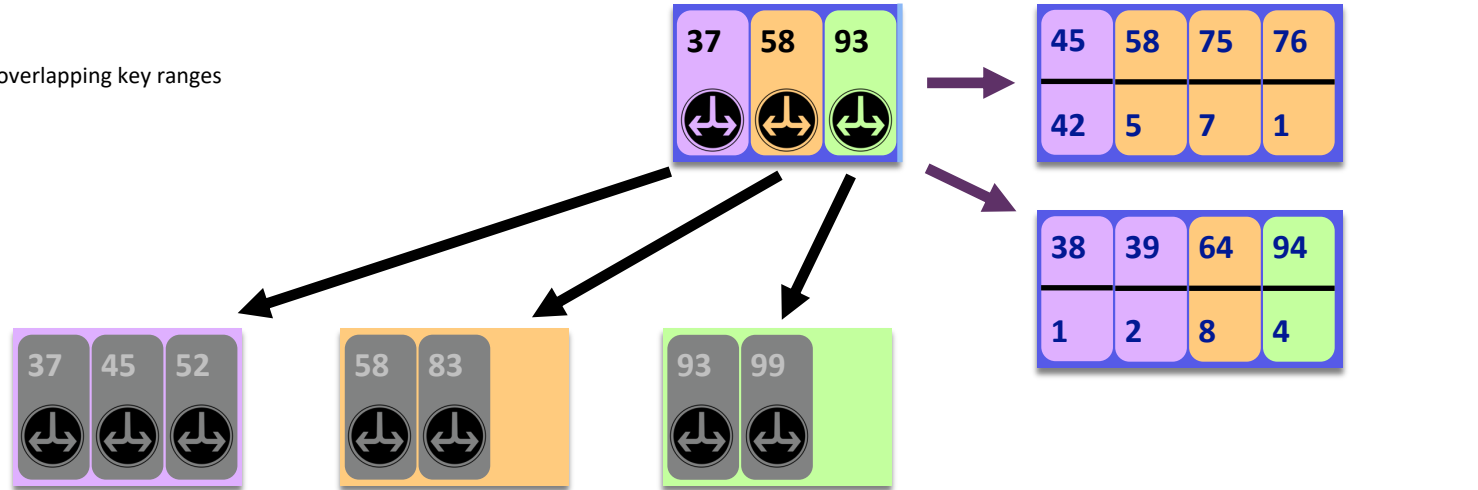
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Branches may have overlapping key ranges



41	42	43	79	85	91
2	5	11	1	2	9

When new data is flushed into the trunk node...

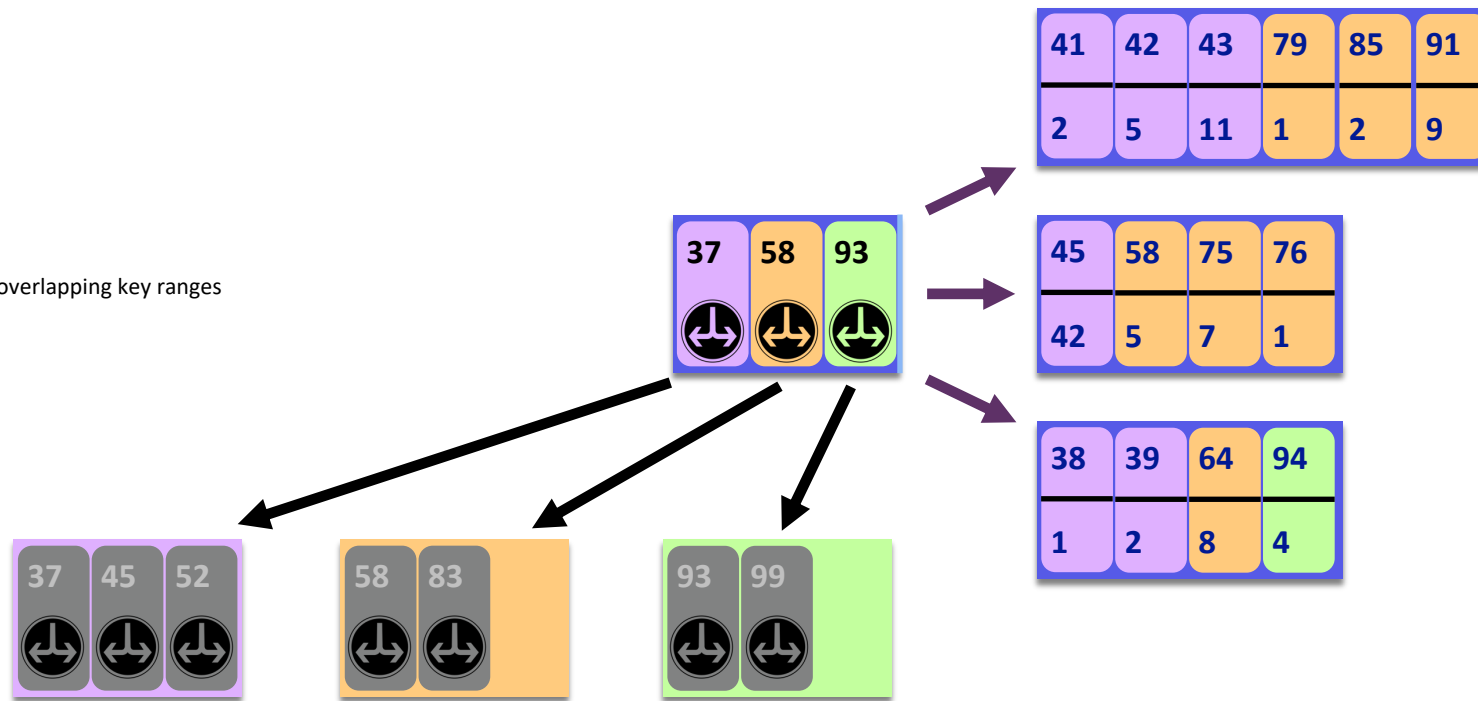
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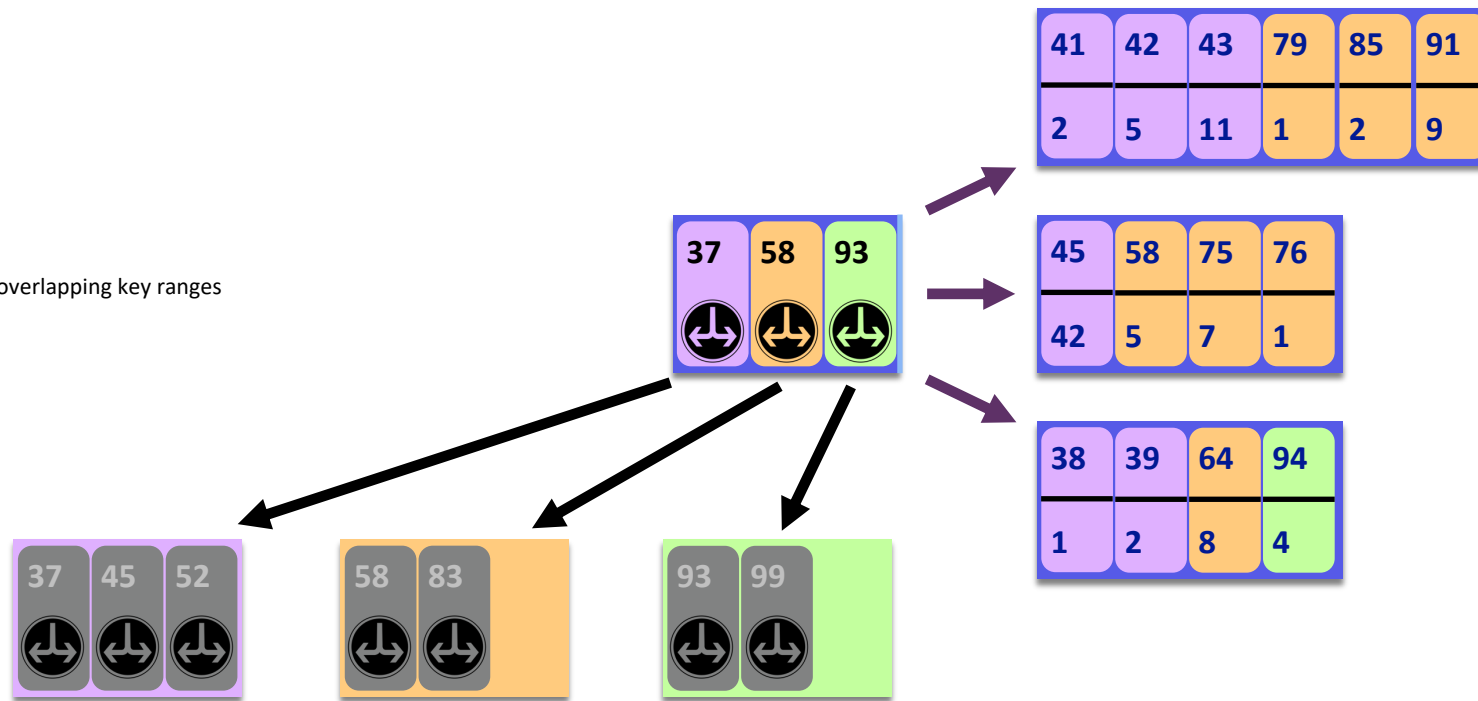
Size-Tiered B^ε-Trees

A Size-Tiered B^ε-tree is a B^ε-tree where the buffer is stored discontinuously

When the node is full:

1. Pick child receiving most messages
2. Merge them into a new branch for the child

Branches may have overlapping key ranges



When new data is flushed into the trunk node...

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The old branches do not need to be rewritten

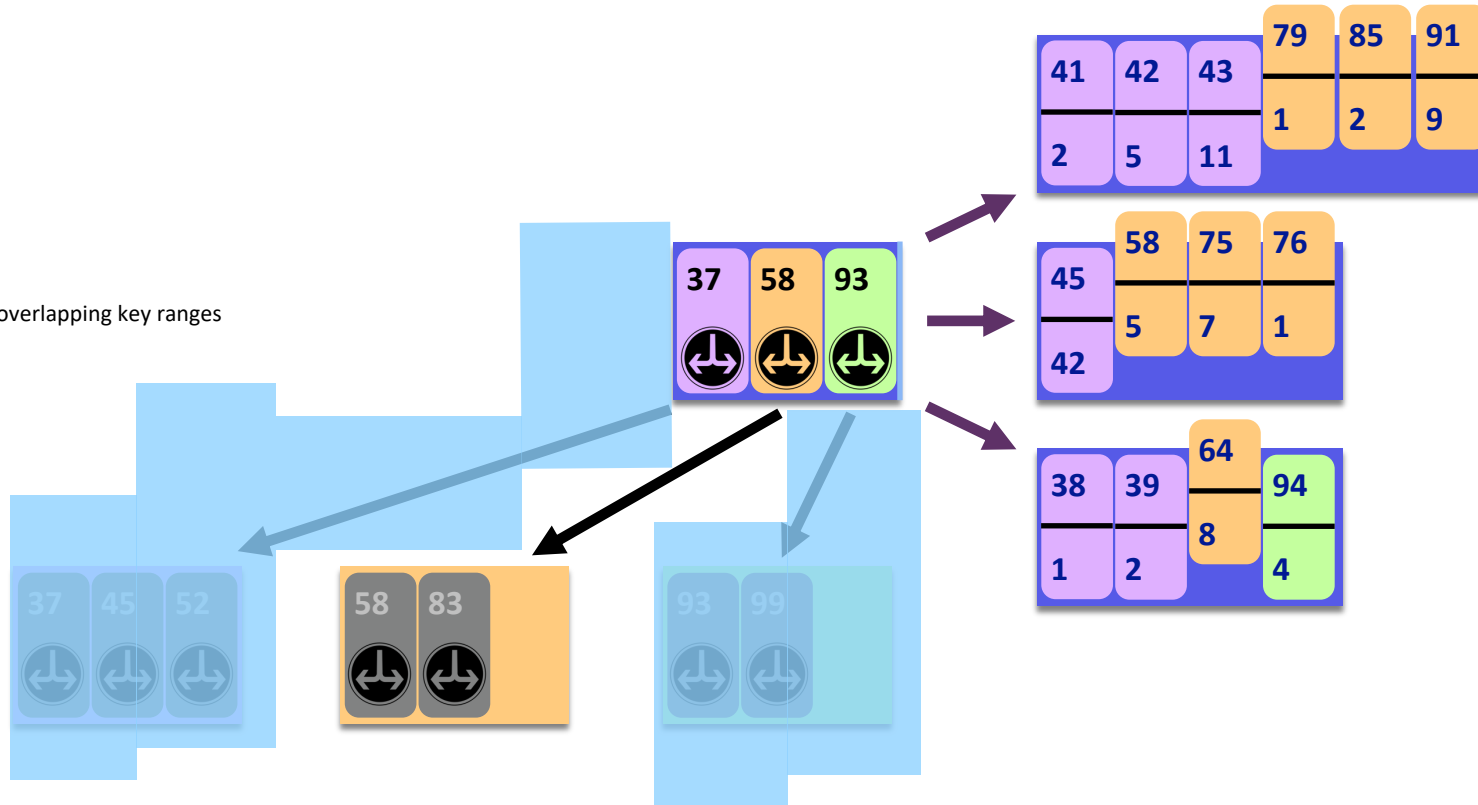
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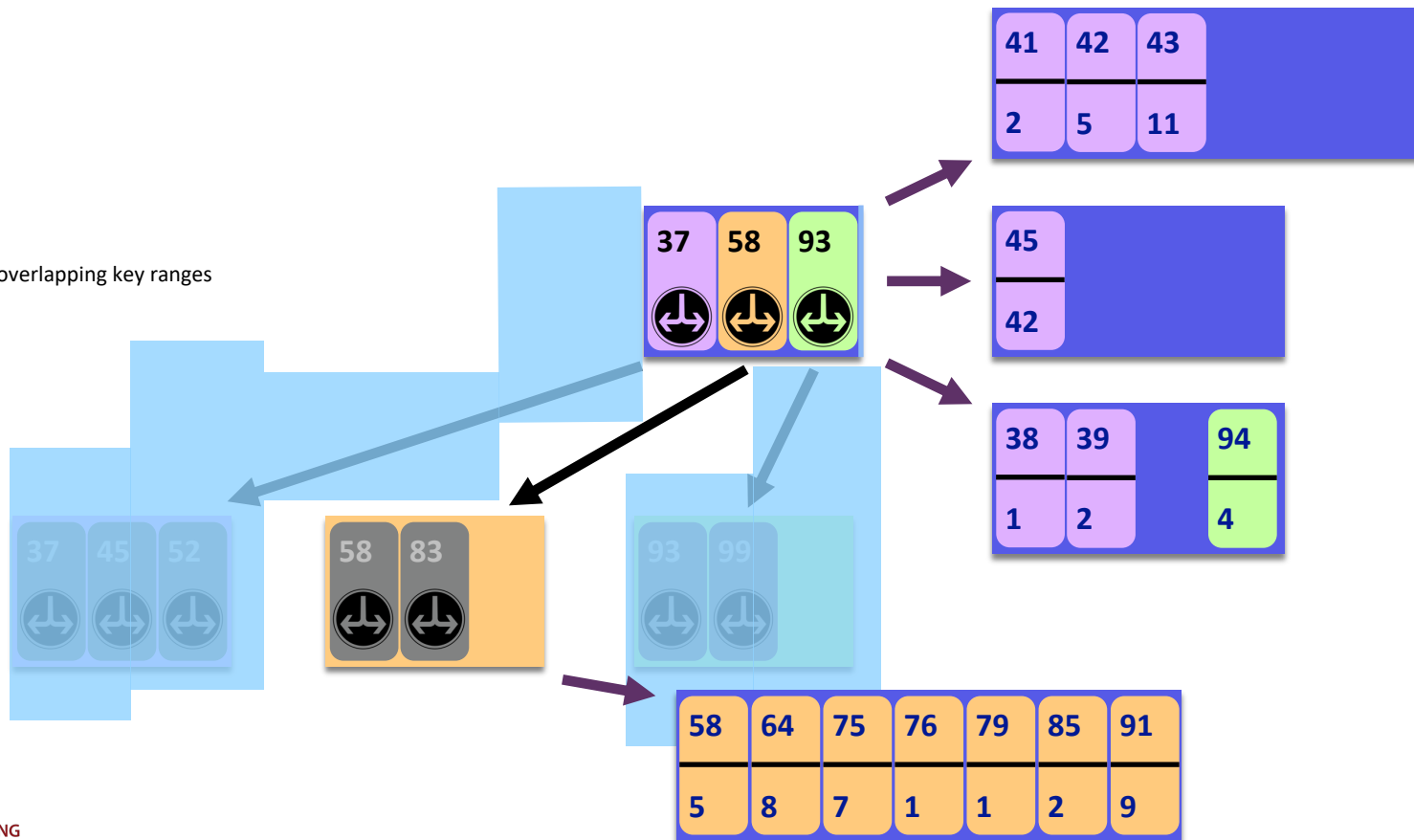
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Branches may have overlapping key ranges



When new data is flushed into the trunk node...

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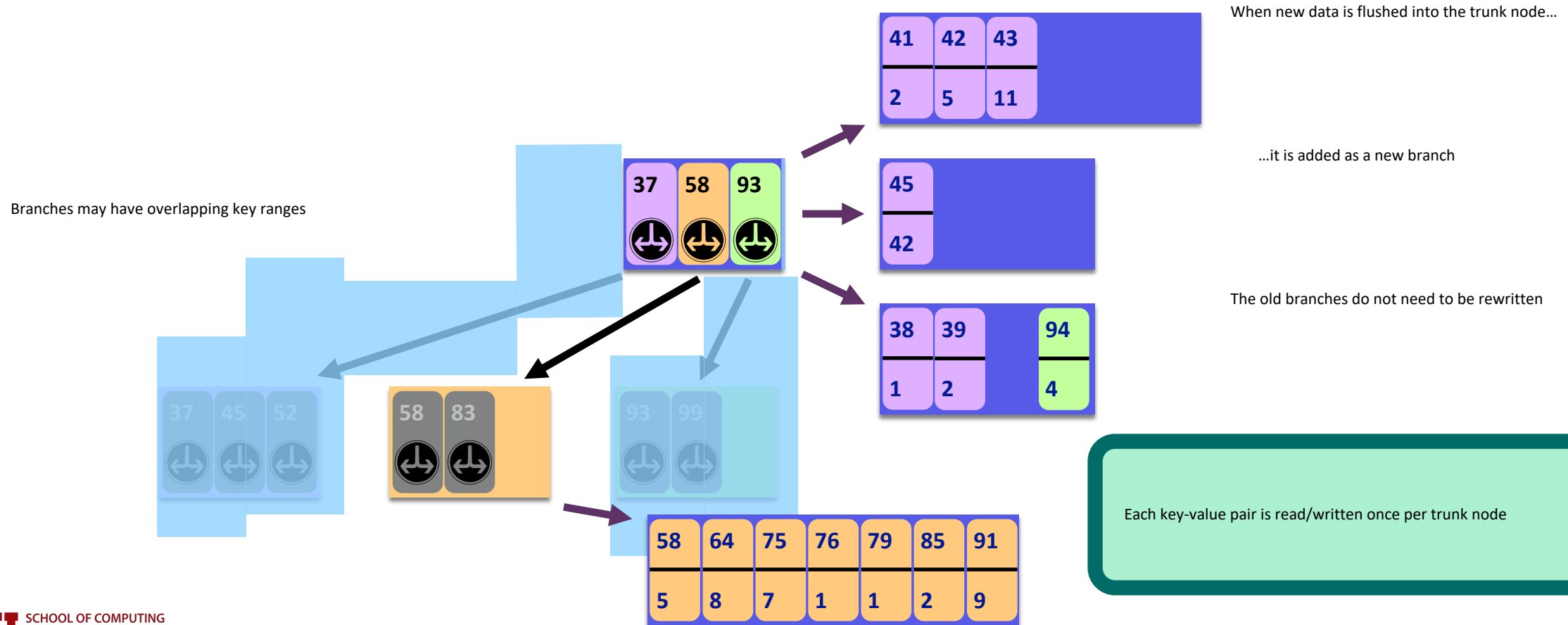
The old branches do not need to be rewritten

Size-Tiered B^ε-Trees

A Size-Tiered B^ε-tree is a B^ε-tree where the buffer is stored discontinuously

When the node is full:

1. Pick child receiving most messages
2. Merge them into a new branch for the child

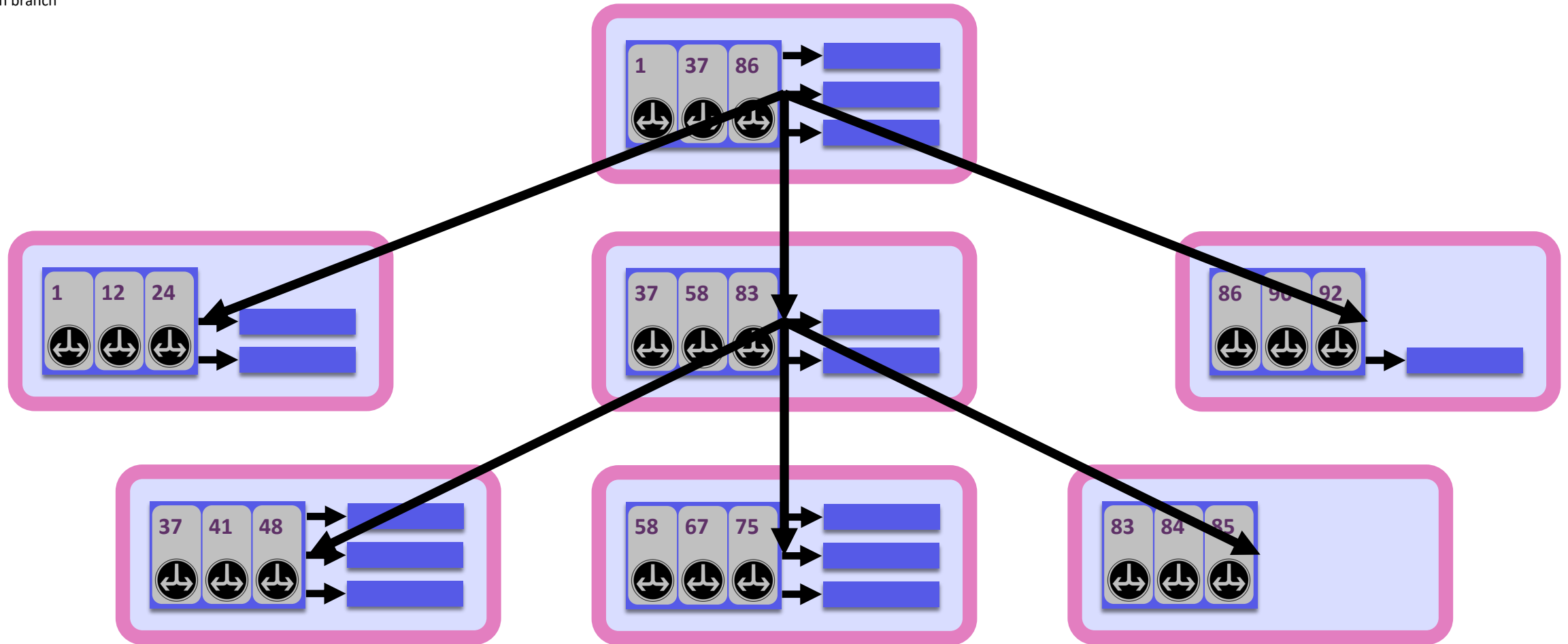


Lookups in Size-Tiered B^ϵ -Trees

Size-Tiered B^ϵ -Trees

Lookups in a STB^ϵ -tree are like lookups in a B^ϵ -tree, except they must check each branch

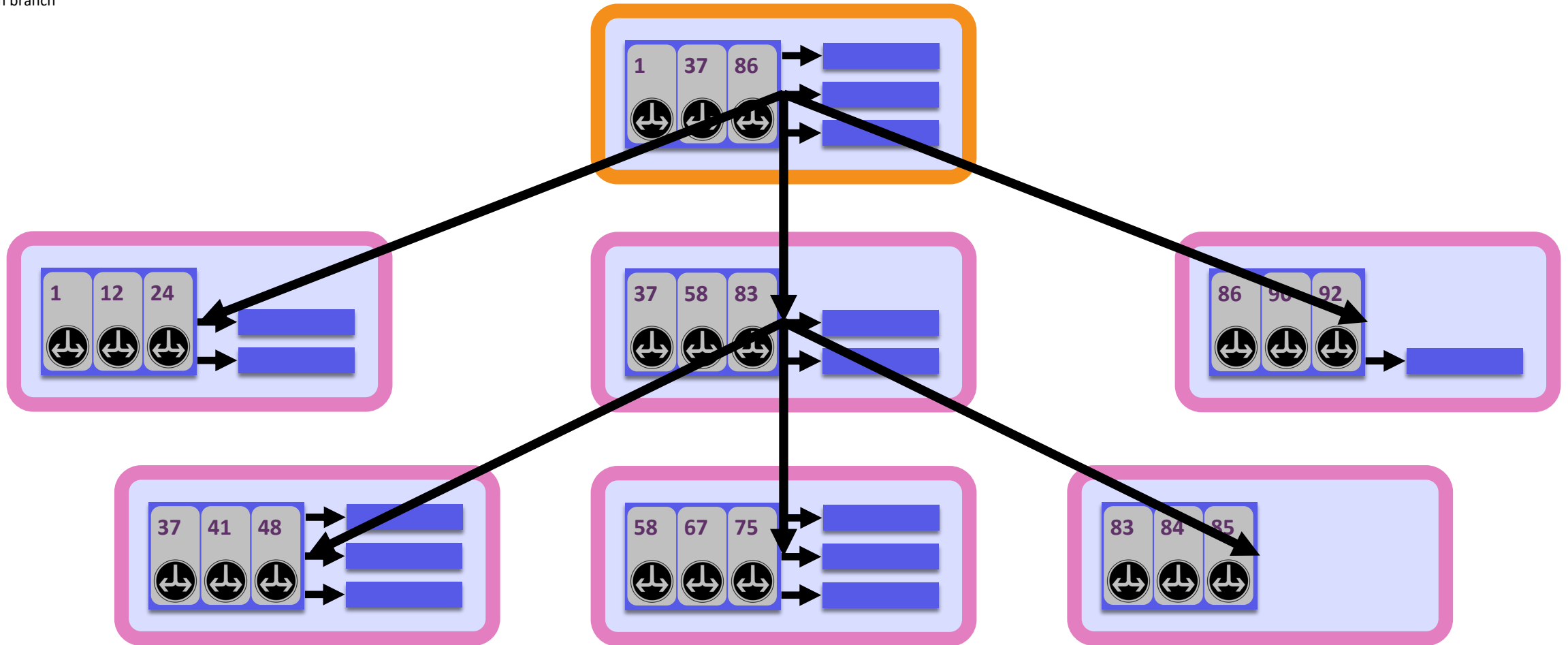
Query(71)



Size-Tiered B^ϵ -Trees

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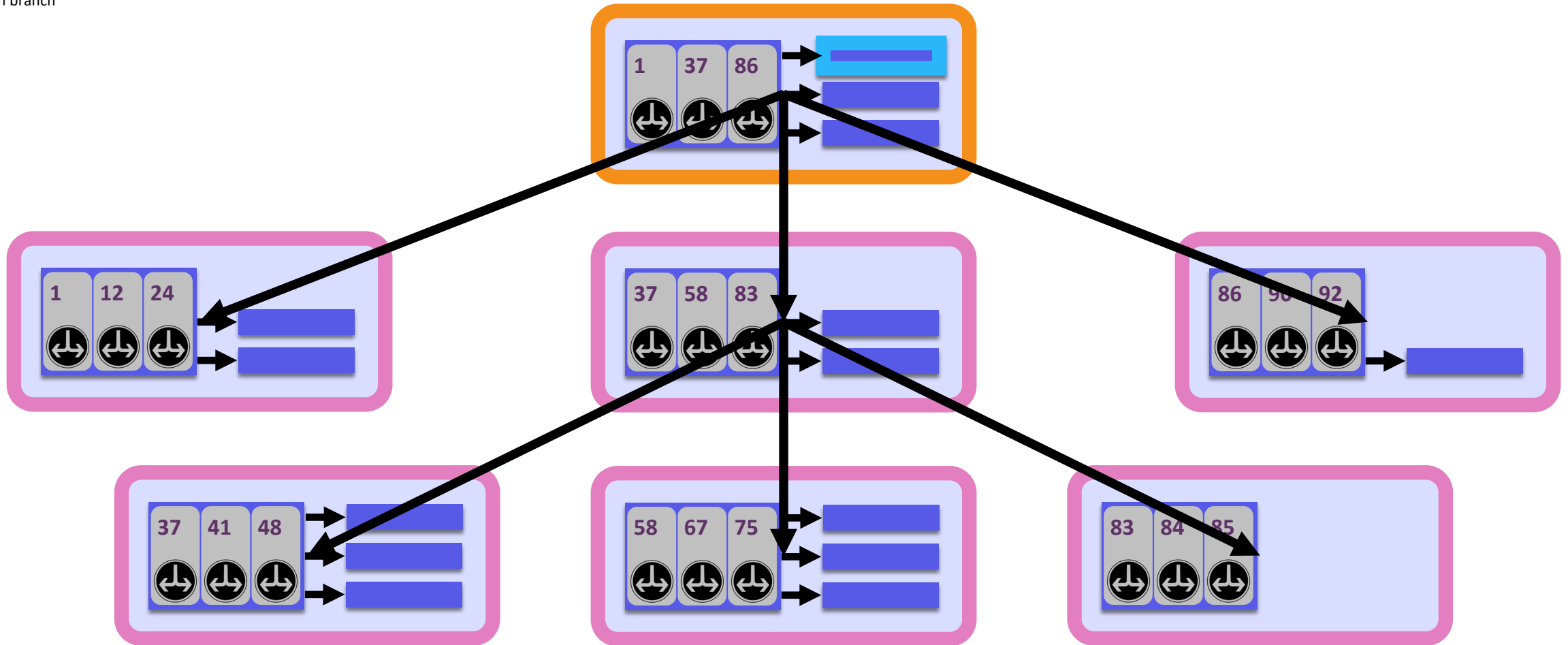
Query(71)



Size-Tiered B^ε-Trees

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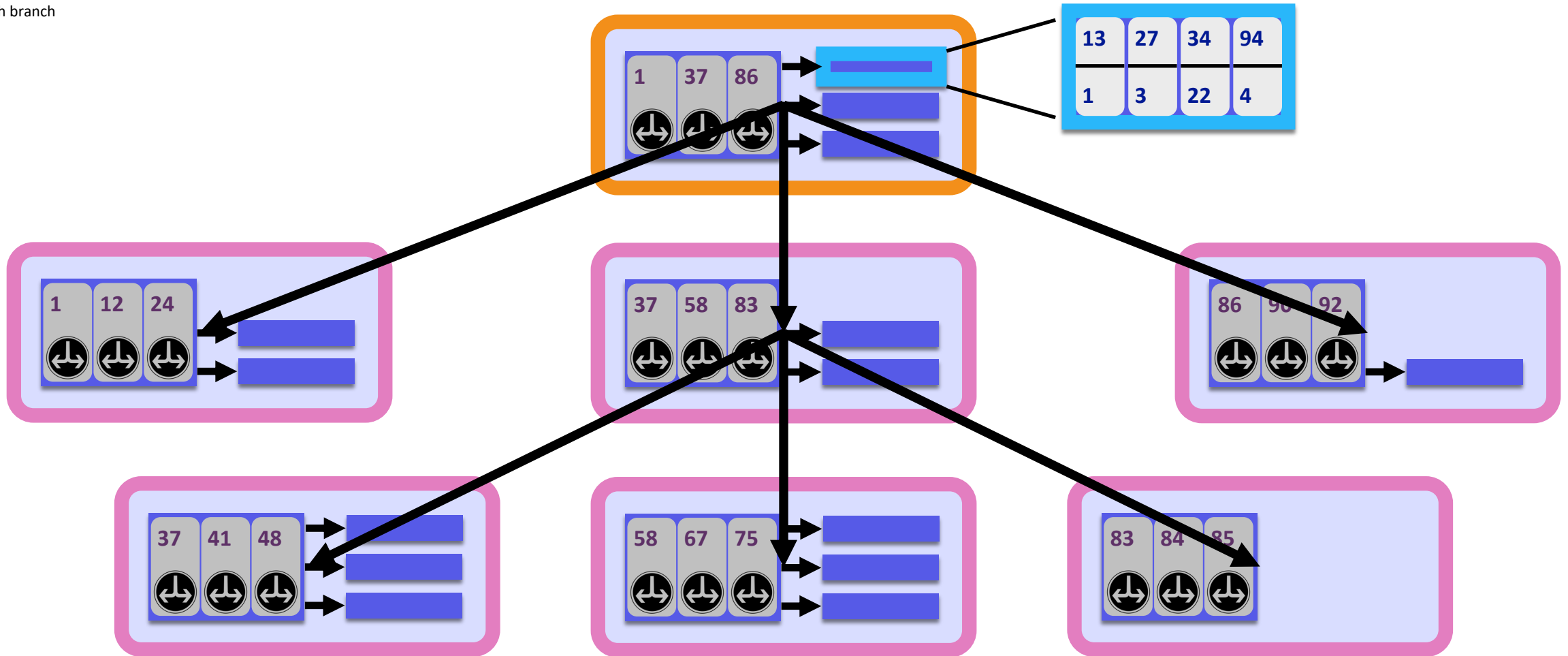
Query(71)



Size-Tiered B^ε-Trees

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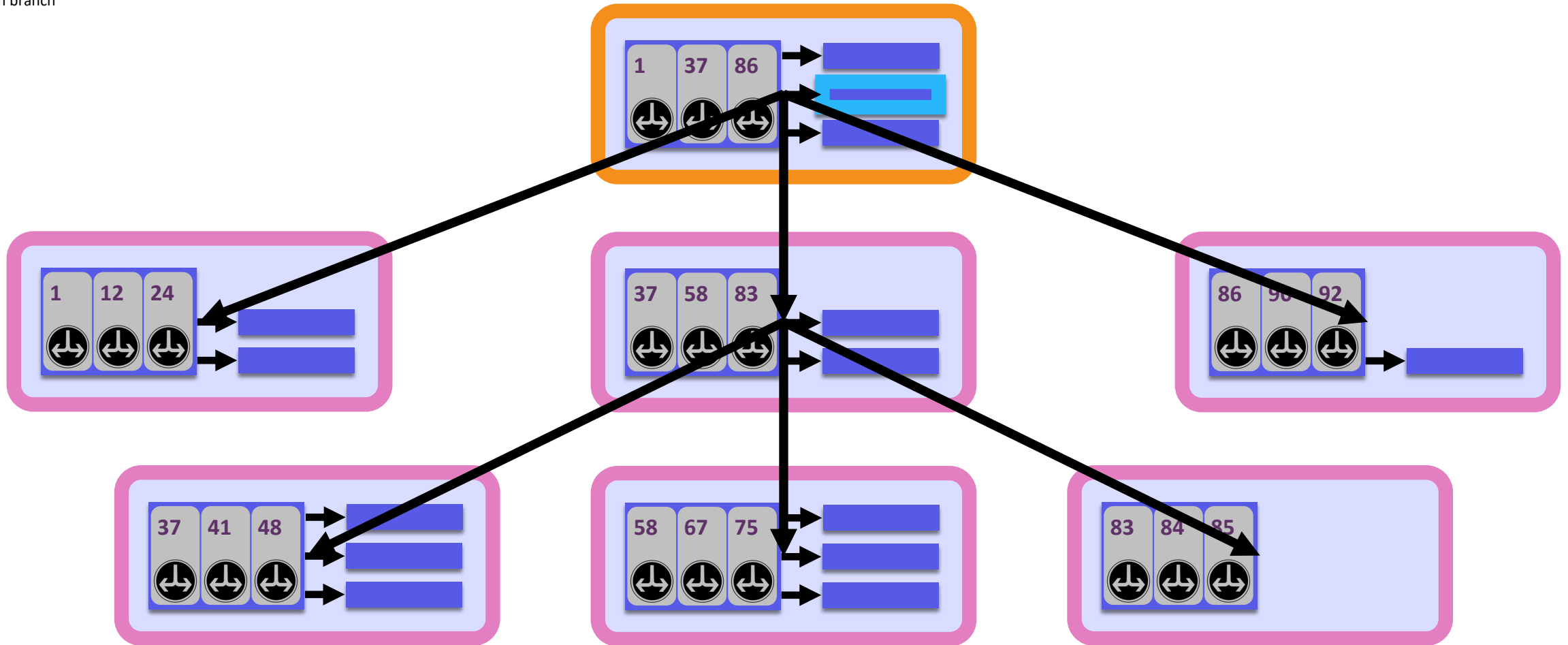
Query(71)



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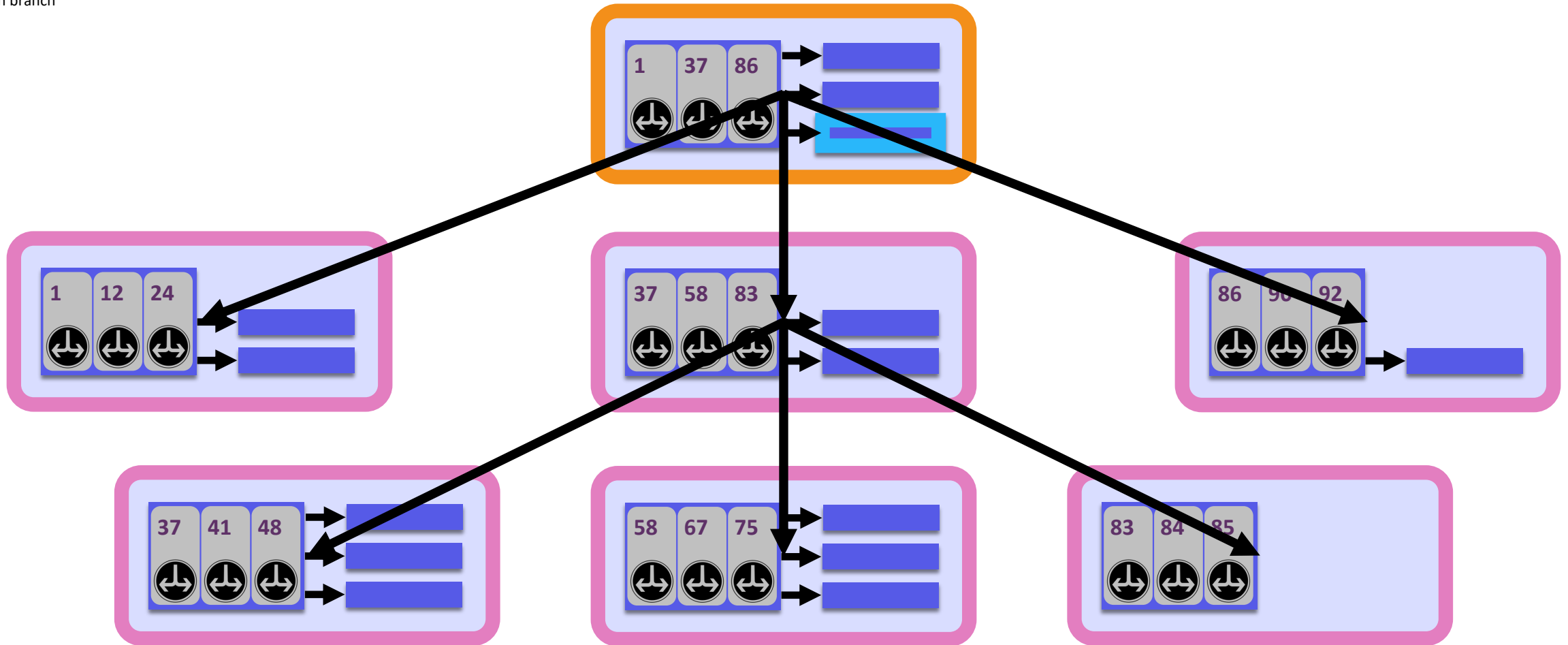
Query(71)



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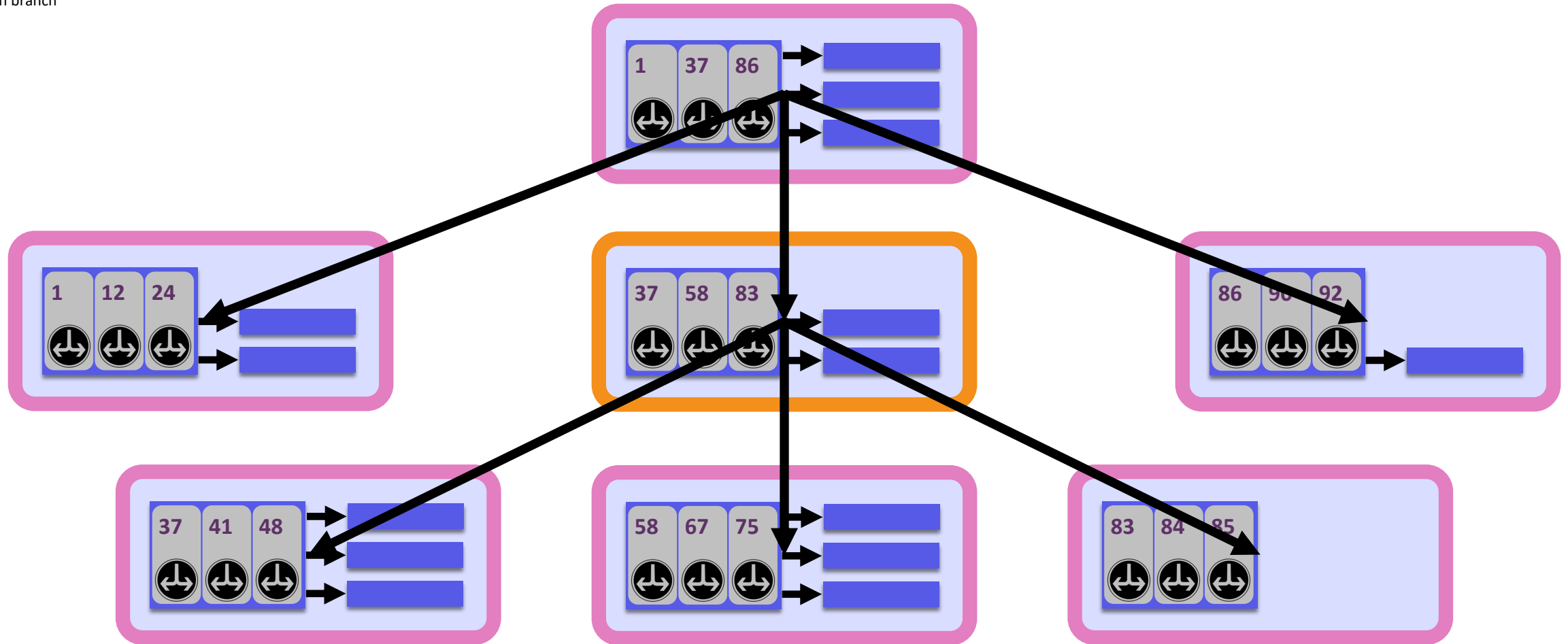
Query(71)



Size-Tiered B^ε-Trees

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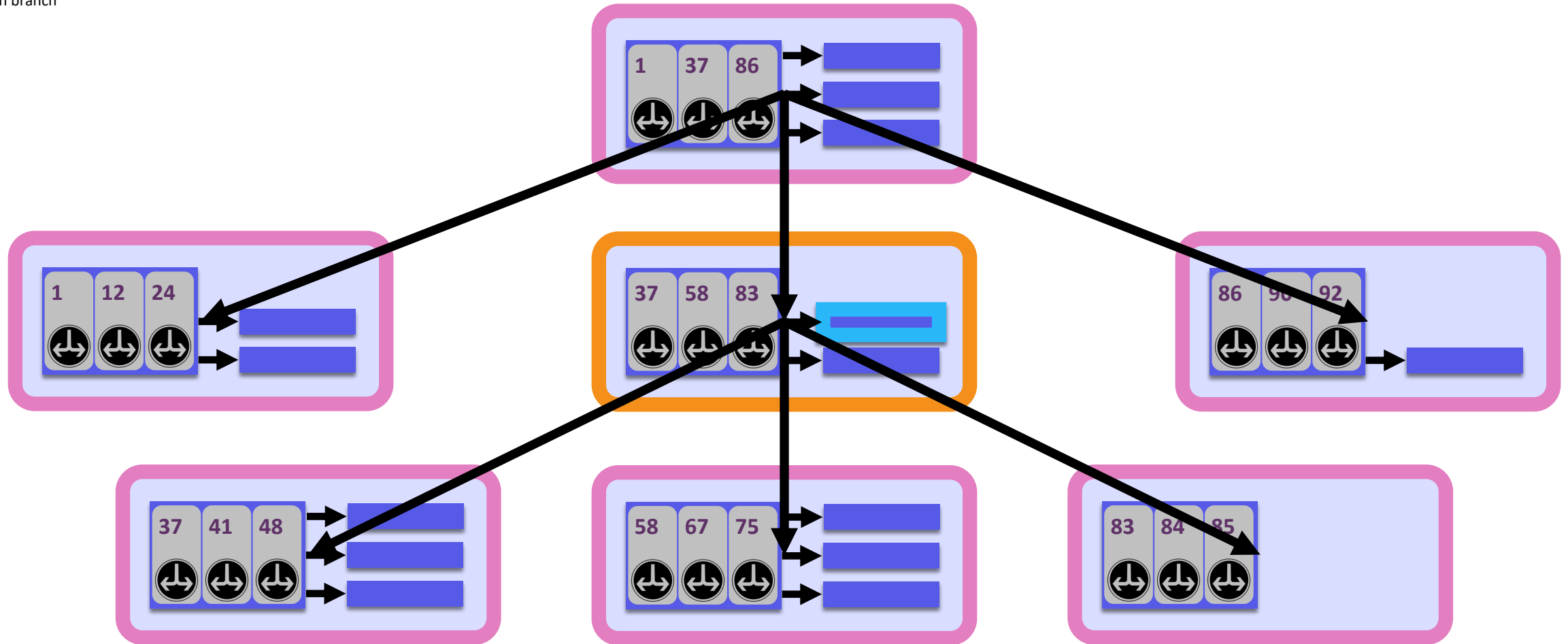
Query(71)



Size-Tiered B^ε-Trees

Lookups in a STB^ε-tree are like lookups in a B^ε-tree, except they must check each branch

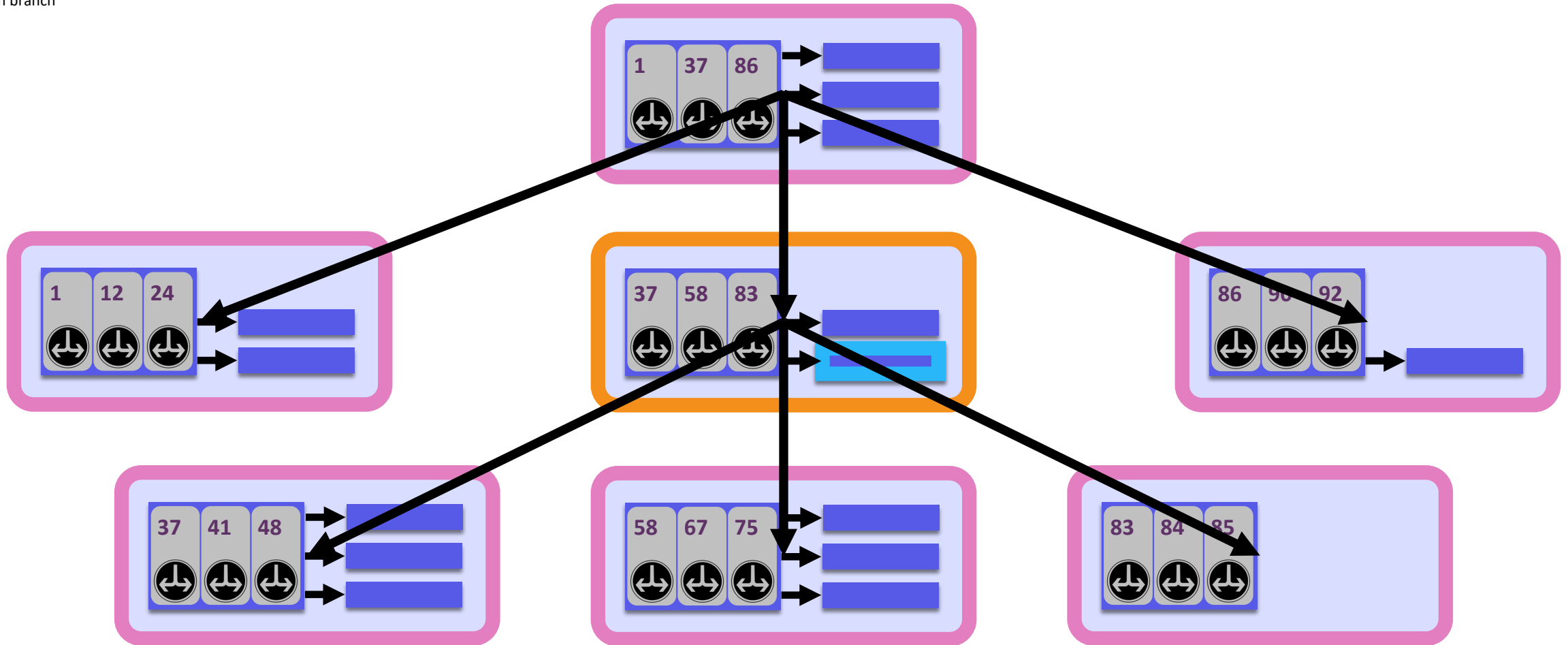
Query(71)



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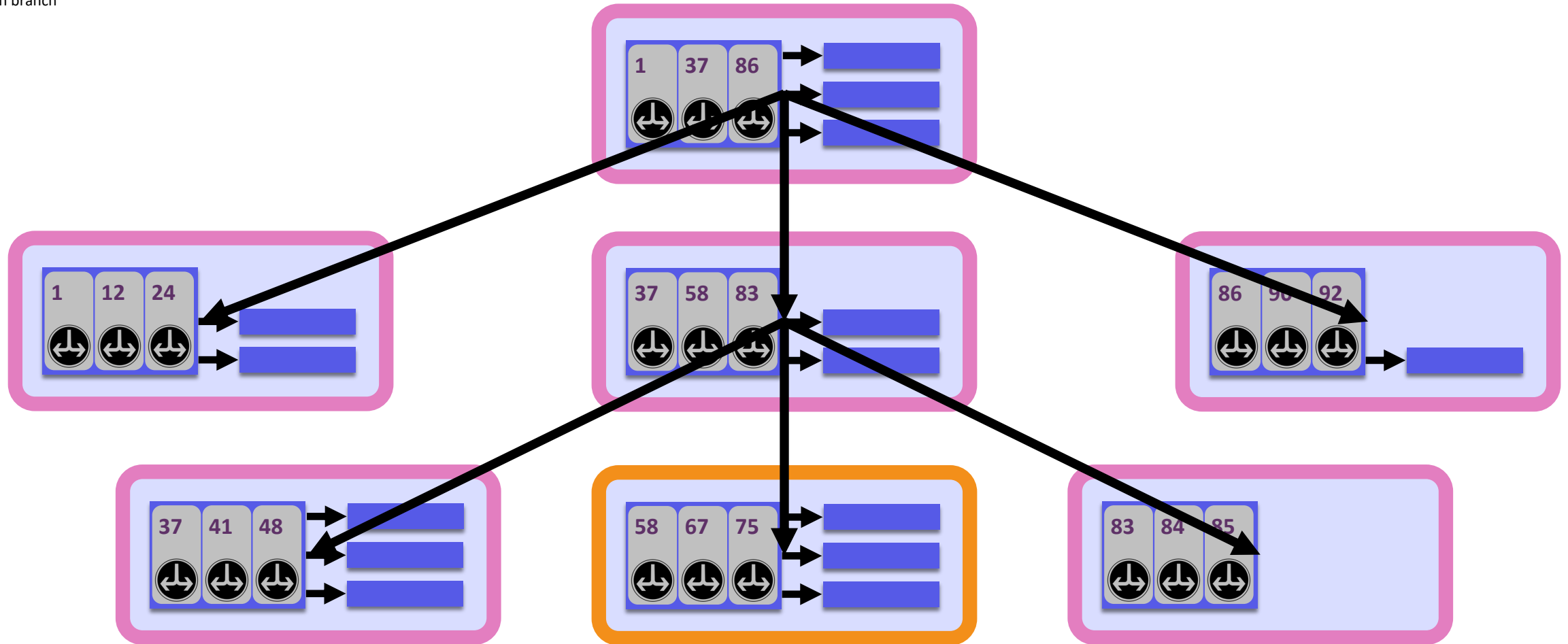
Query(71)



Size-Tiered B^ε-Trees

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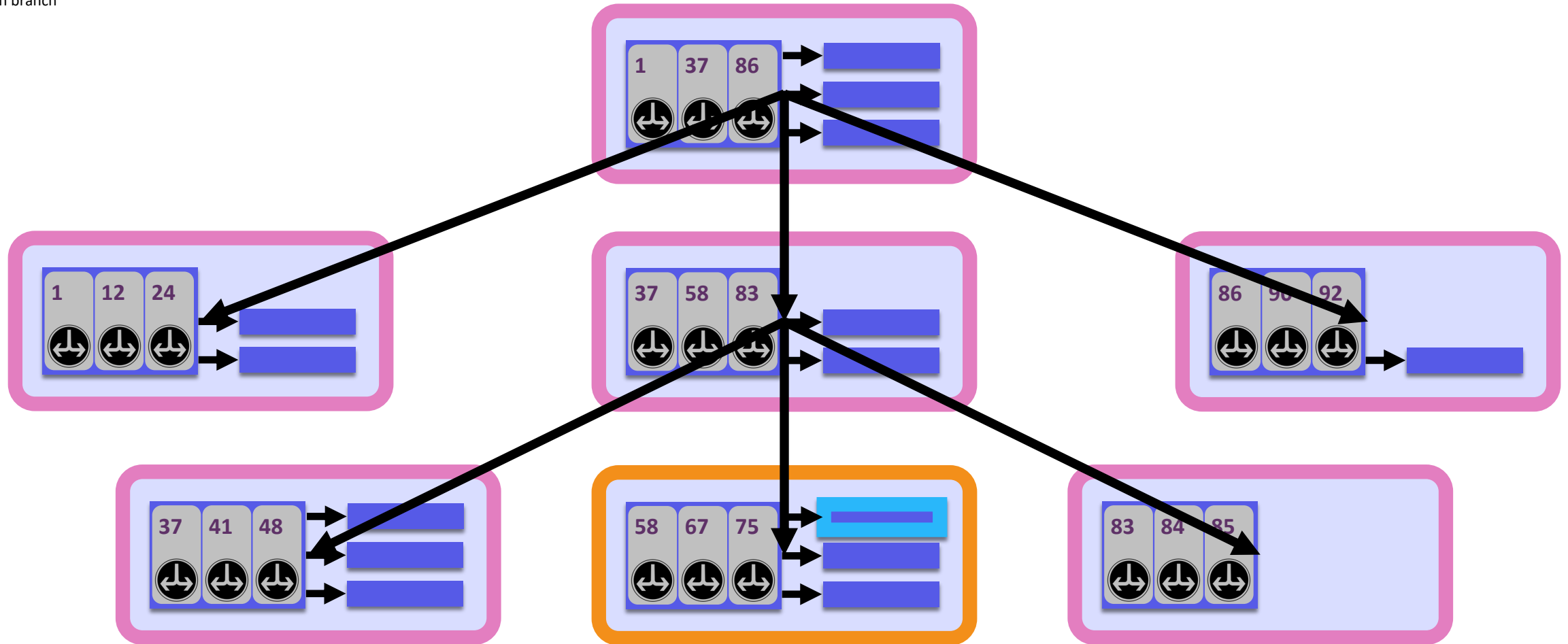
Query(71)



Size-Tiered B^ε-Trees

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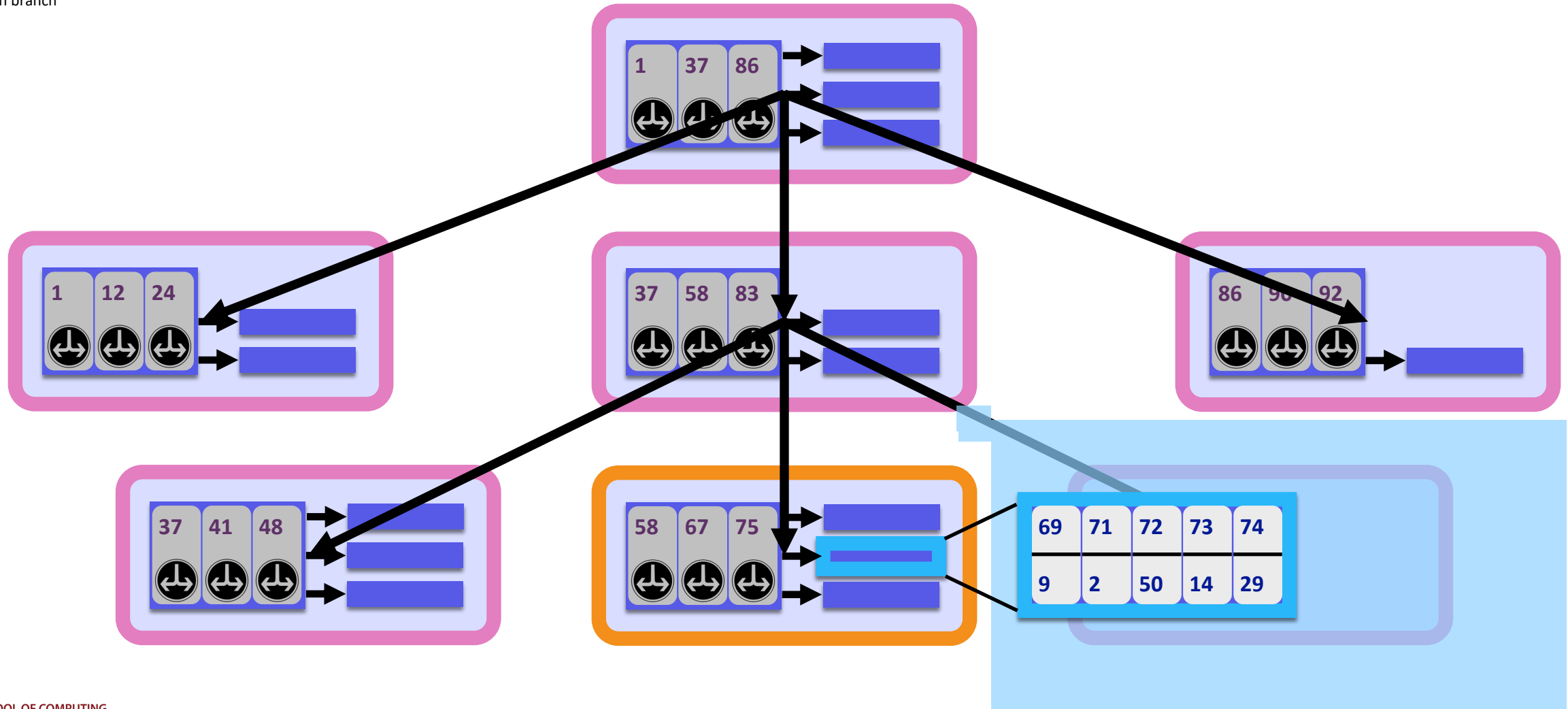
Query(71)



Size-Tiered B^ε-Trees

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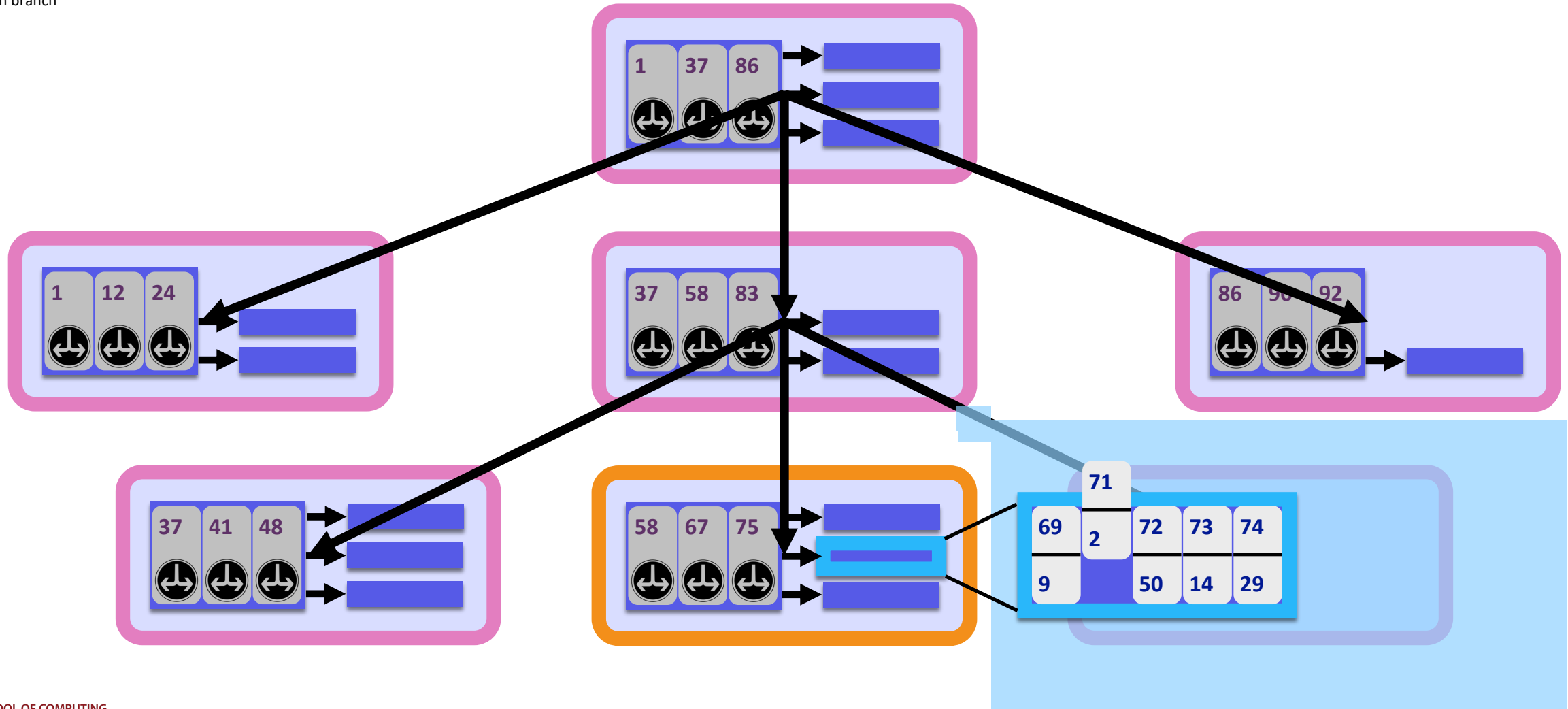
Query(71)



Size-Tiered B^ε-Trees

Lookups in a STB^ε-tree are like lookups in a B^ε-tree, except they must check each branch

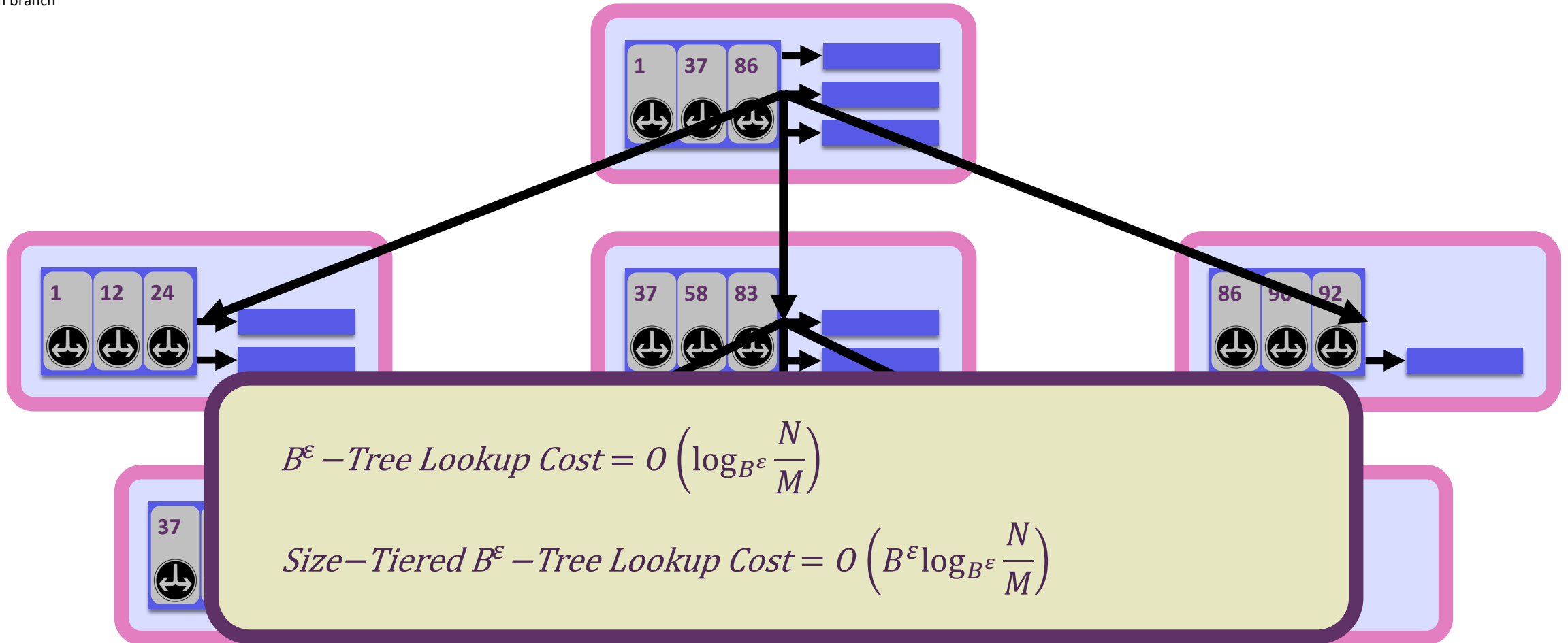
Query(71) → 2



Size-Tiered B^ϵ -Trees

Lookups in a STB^ϵ -tree are like lookups in a B^ϵ -tree, except they must check each branch

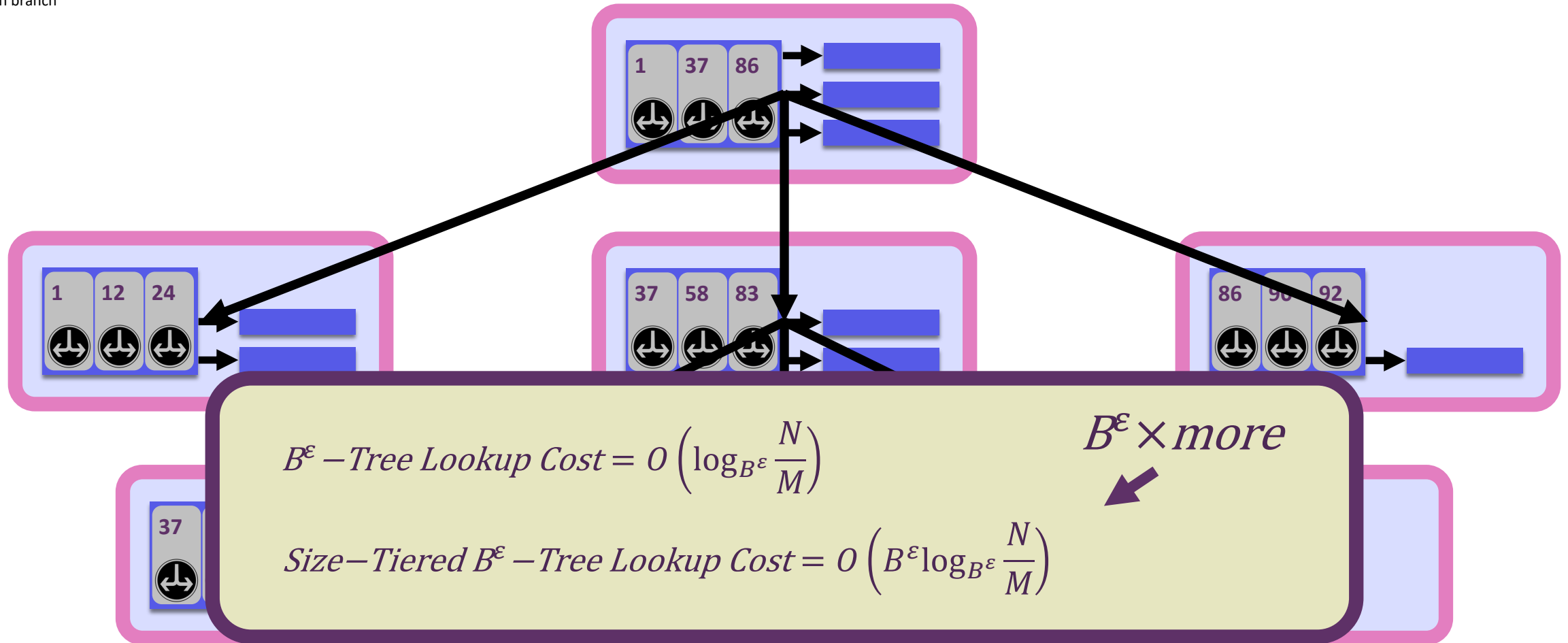
Query(71)



Size-Tiered B^ϵ -Trees

Lookups in a STB^ϵ -tree are like lookups in a B^ϵ -tree, except they must check each branch

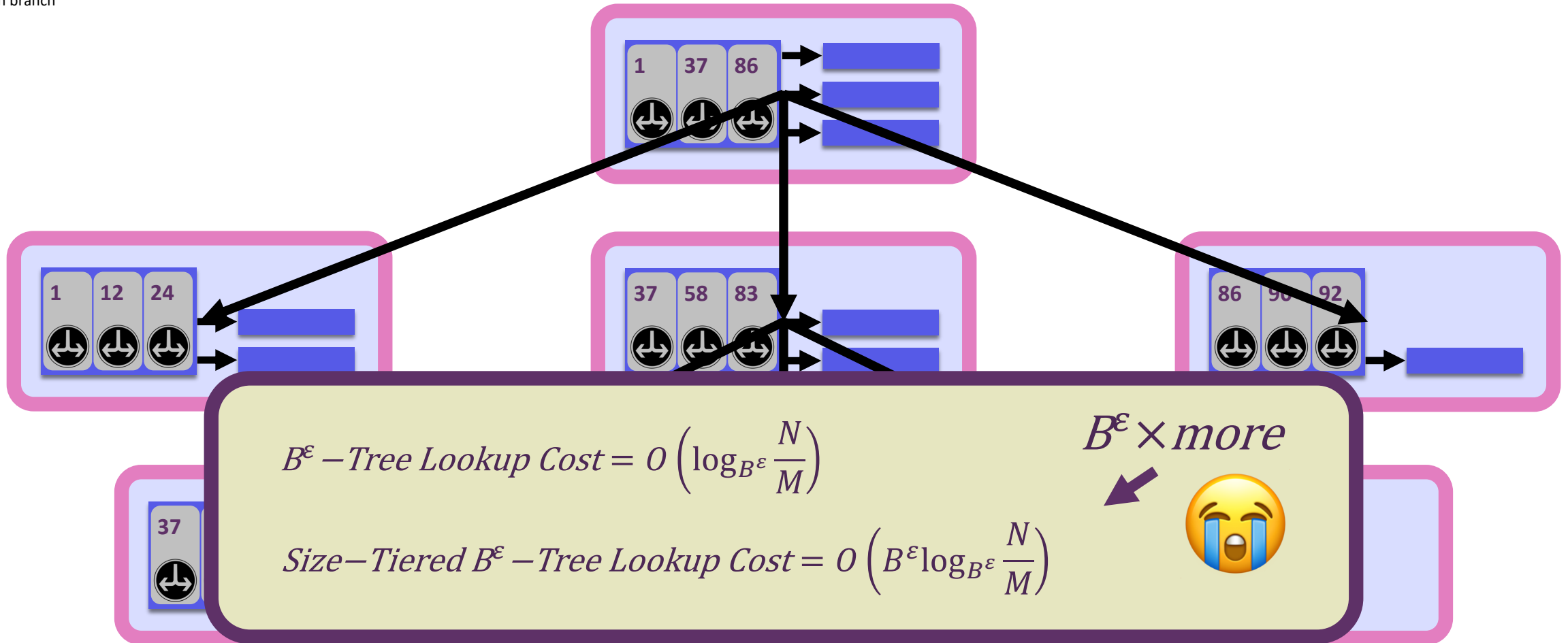
Query(71)



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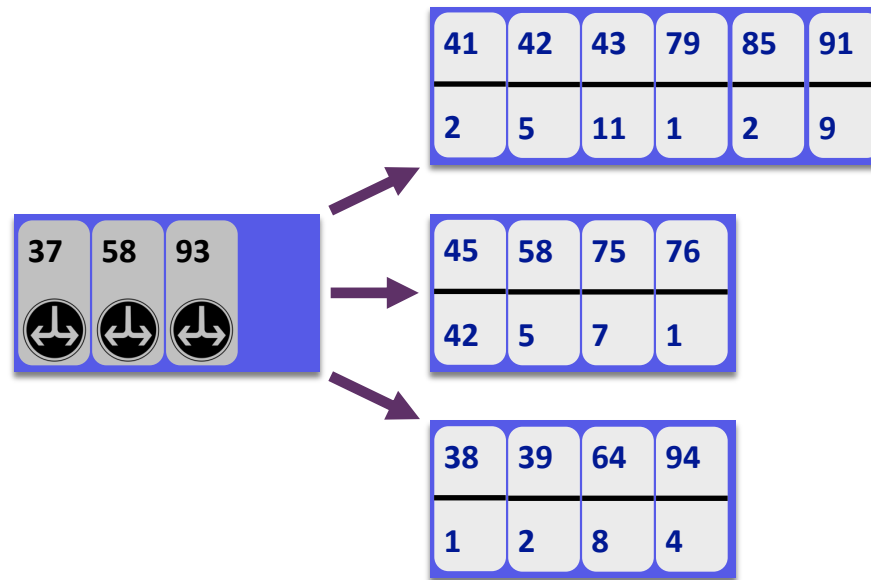
Query(71)



Fixing Lookups (almost)

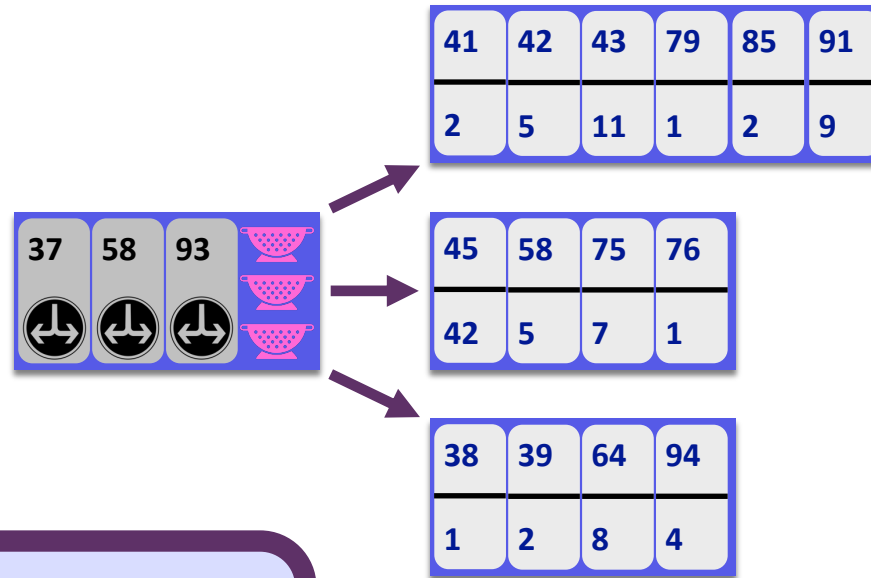
Fixing Lookups (almost)

The problem is that each node has multiple branches

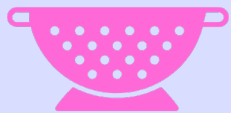


Fixing Lookups (almost)

The problem is that each node has multiple branches



Idea: use filters to avoid searching them

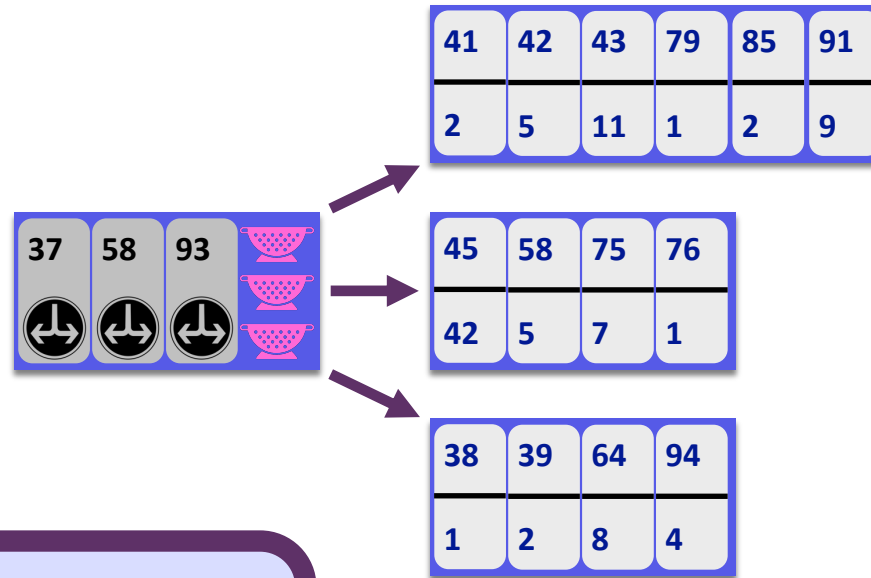


A filter is a probabilistic data structure with answers membership with no false negatives

Examples: Bloom, cuckoo, quotient

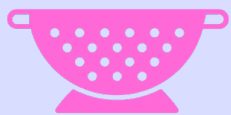
Fixing Lookups (almost)

The problem is that each node has multiple branches



Idea: use filters to avoid searching them

Now a lookup will only search those branches which contain the key (plus rare false positives)



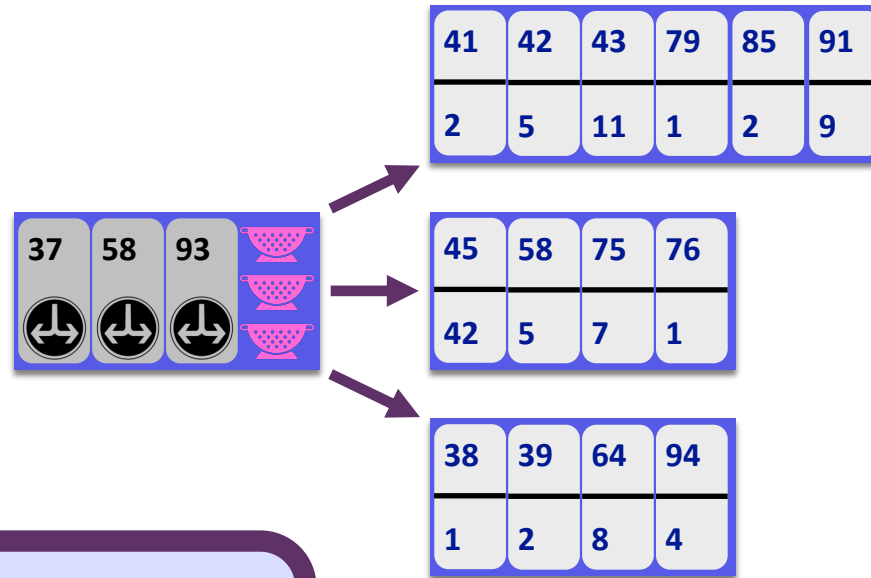
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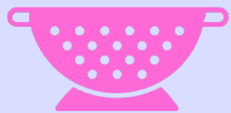
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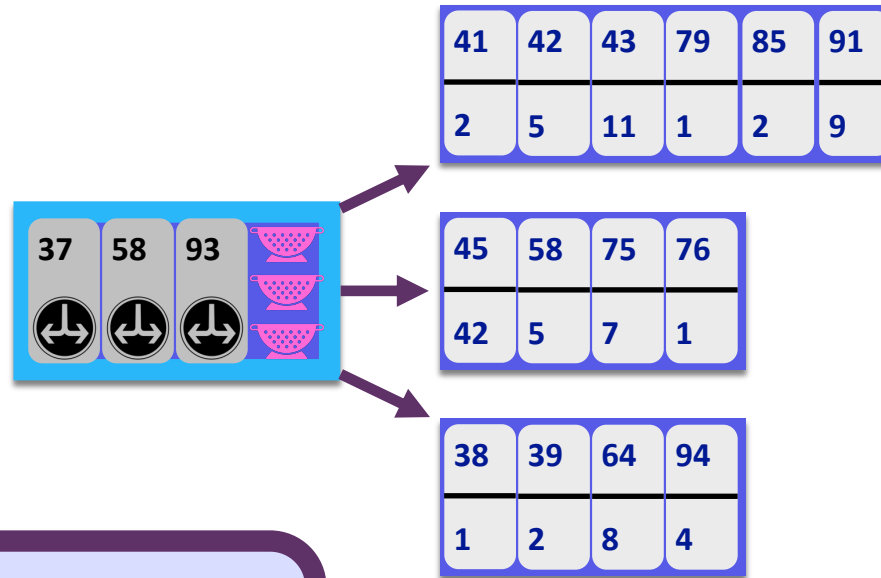
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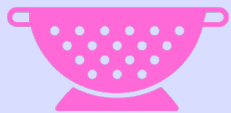
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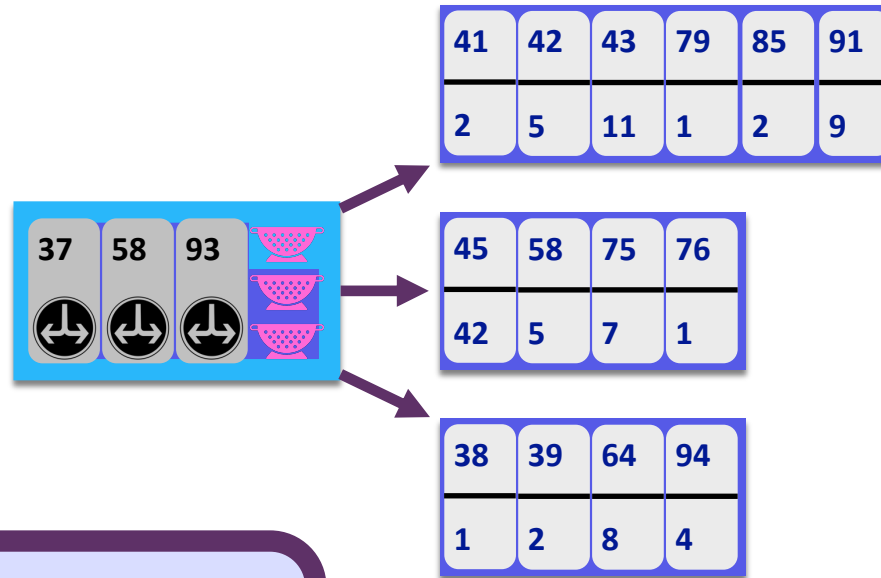
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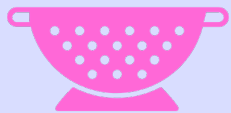
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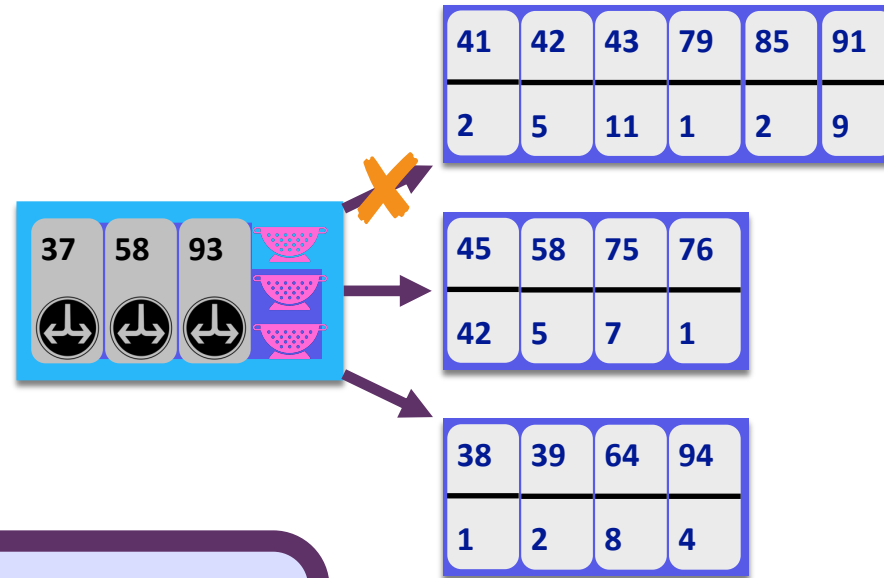
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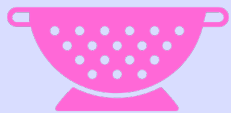
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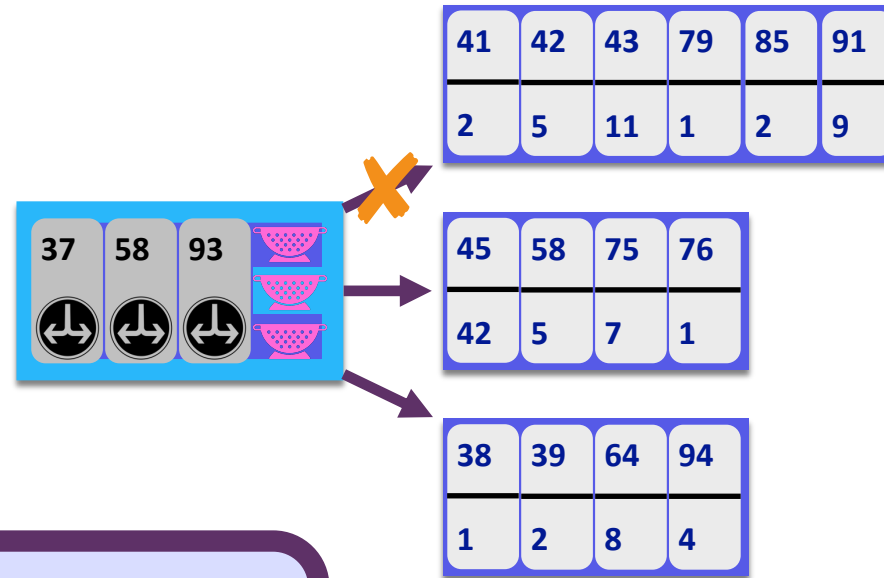
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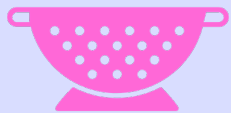
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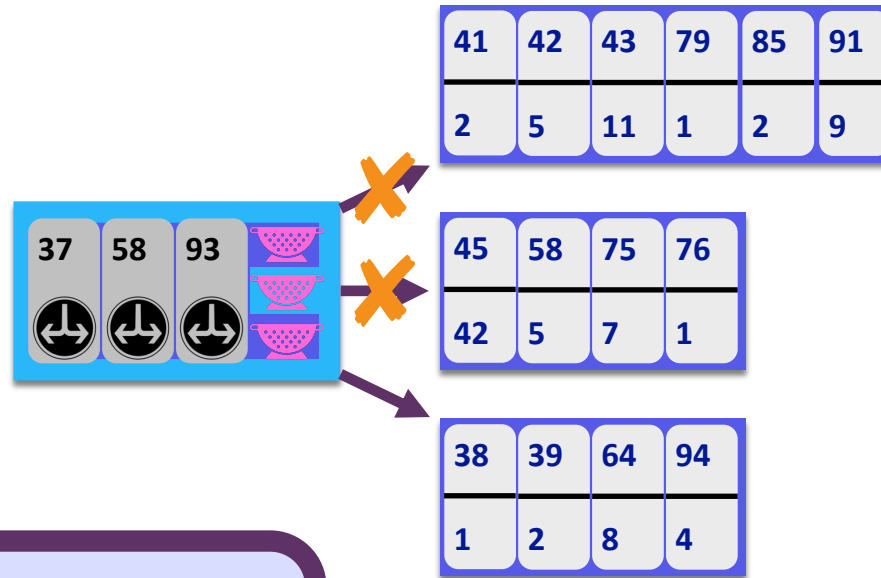
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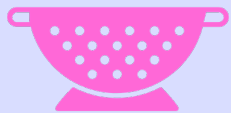
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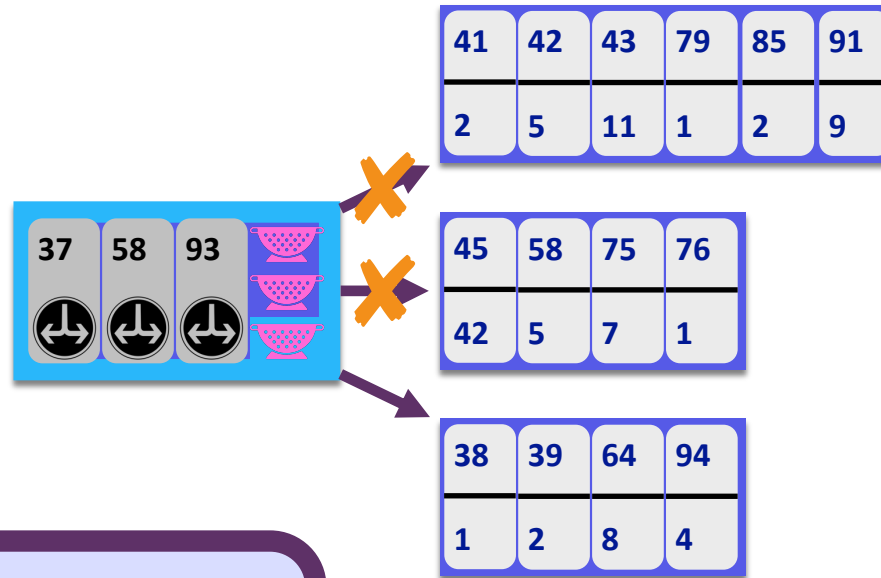


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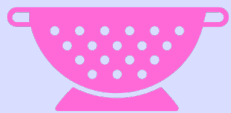
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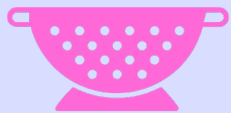
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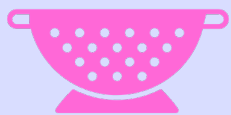
Query(64) → 8

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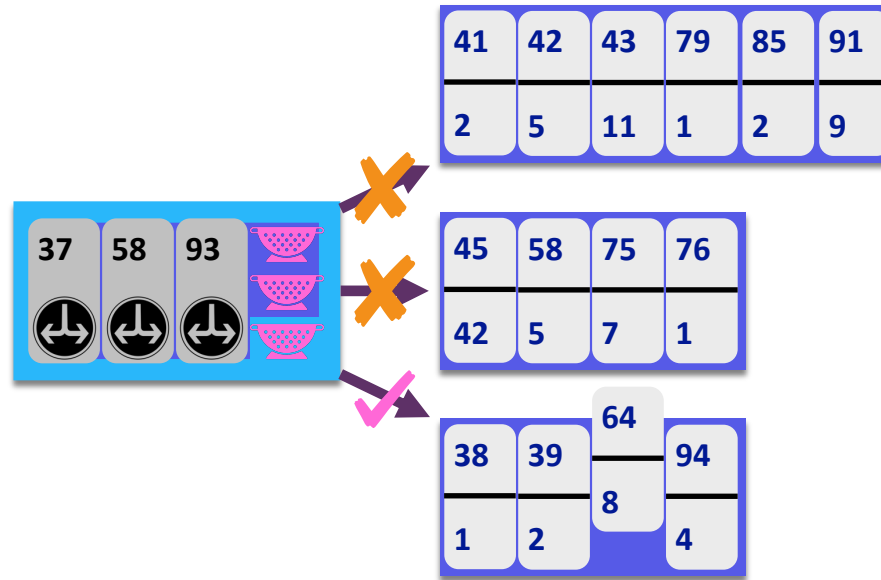
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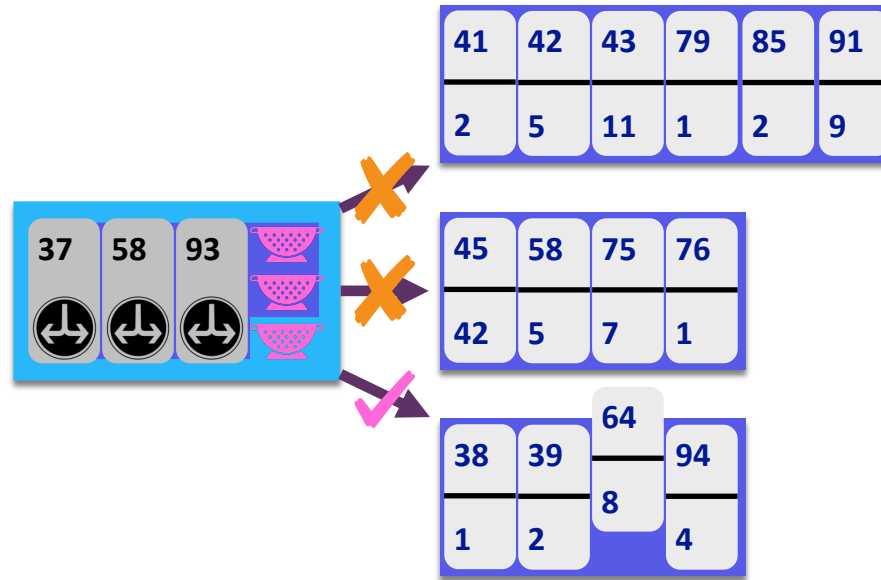
Now a lookup will only search those branches which contain the key (plus rare false positives)

$$\text{False Positive Rate} \leq O\left(\frac{\epsilon}{B^\epsilon \log_B N}\right)$$

Fixing Lookups (almost)

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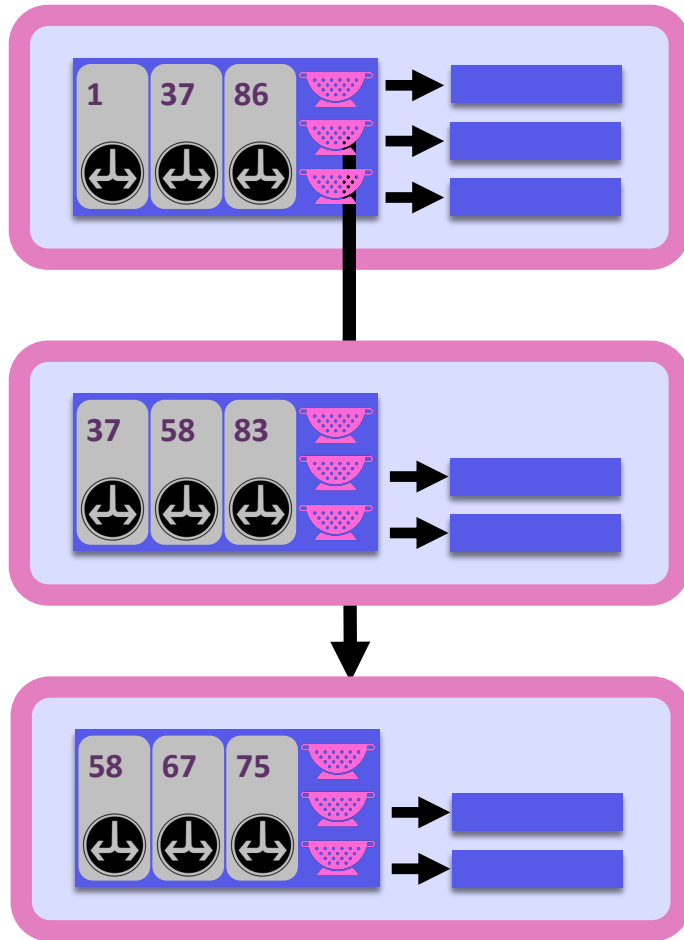
Lookups in $O(1)$ IOs

Really Fixing Lookups in Size-Tiered B^ϵ -Trees

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Querying all these filters is expensive

Root-to-leaf path

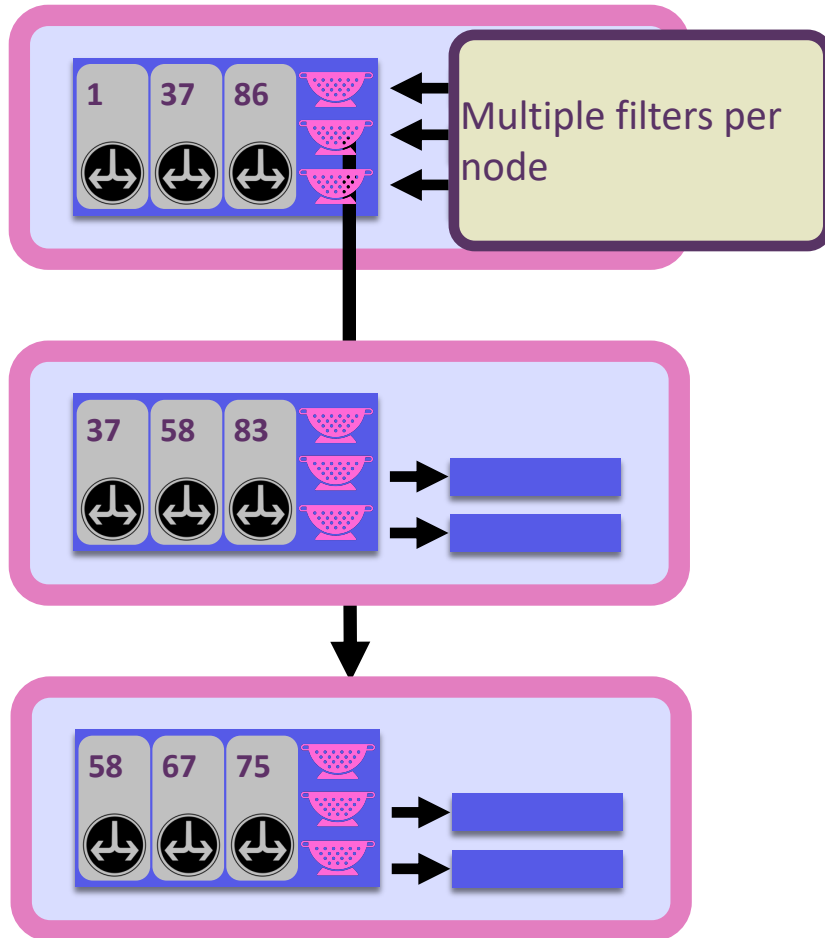


Really Fixing Lookups in Size-Tiered B^ϵ -Trees

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In practice, we see 15-40 filter lookups per point query

Root-to-leaf path



Really Fixing Lookups in Size-Tiered B^ϵ -Trees

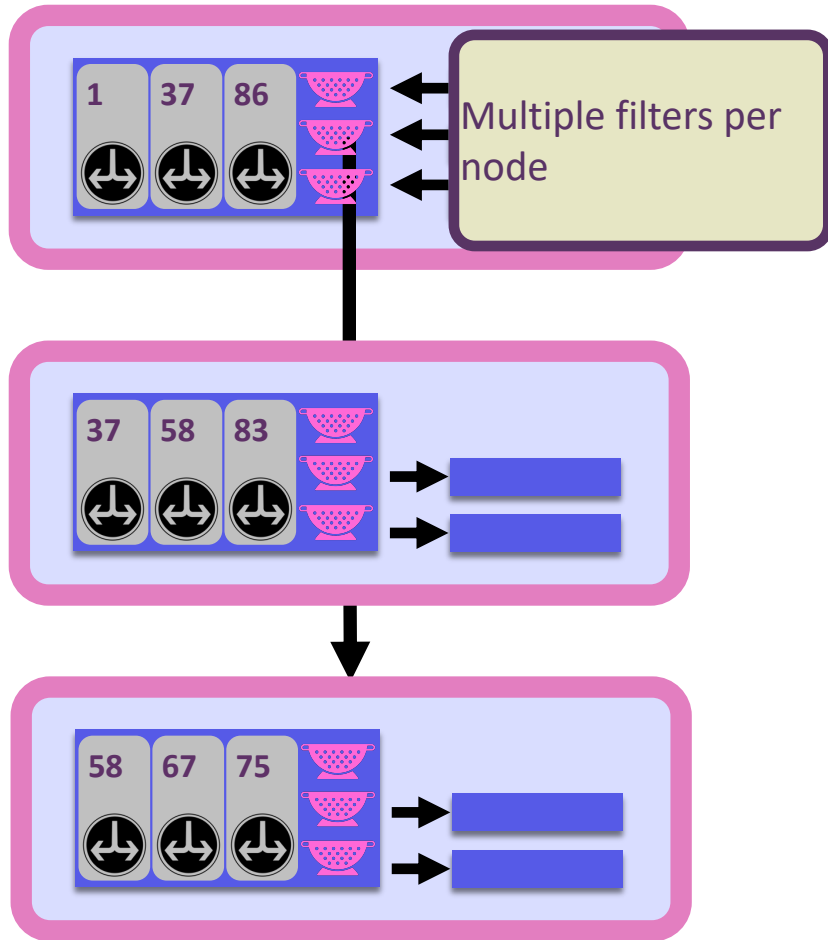
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We could hope to amortize against IO

BUT...

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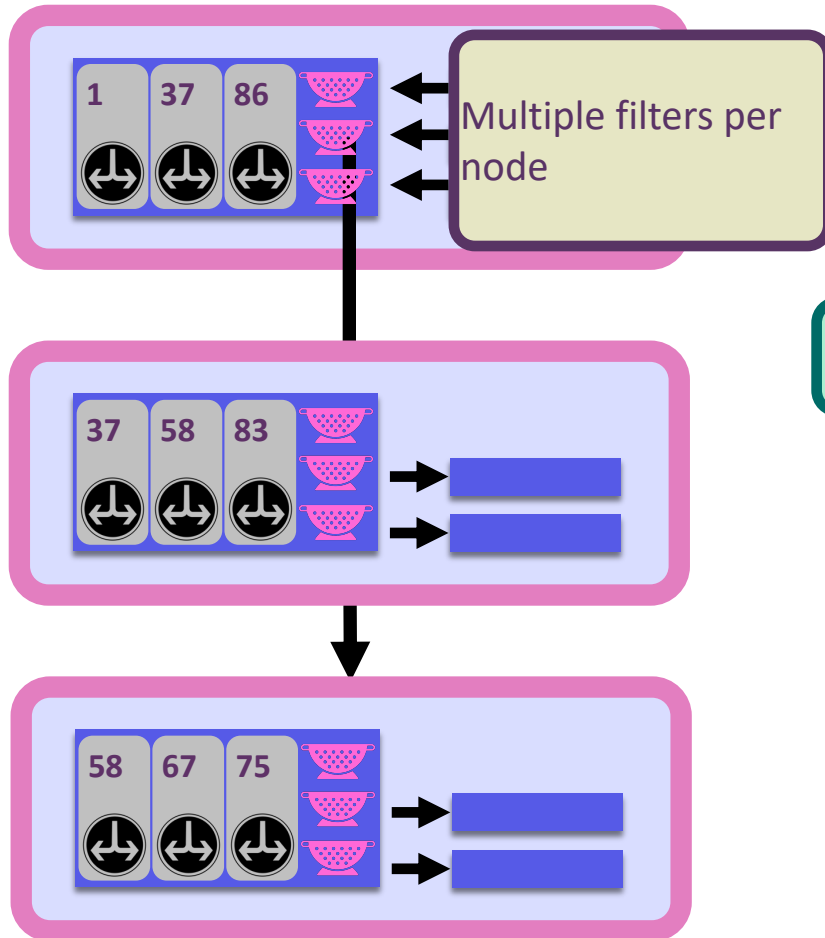
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High Memory/Hot Queries

No IO, performance limited by CPU

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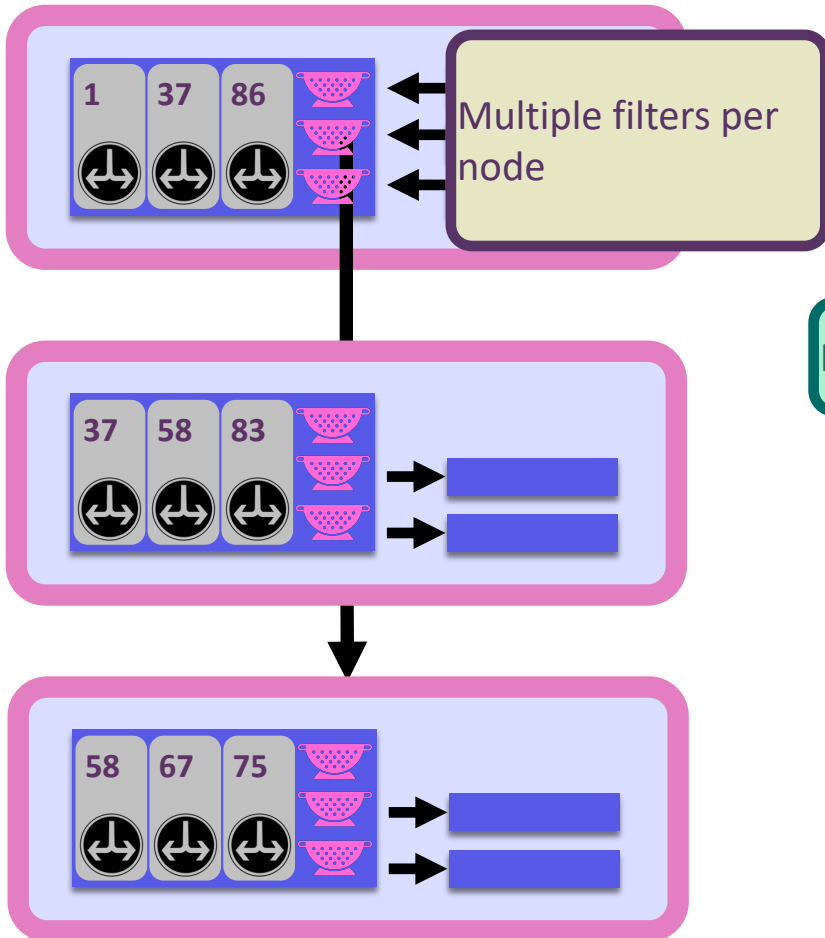
High Memory/Hot Queries

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Medium Memory

1 IO per query,
CPU cost of filter lookups ⇒ more threads

Root-to-leaf path



Really Fixing Lookups in Size-Tiered B^ϵ -Trees

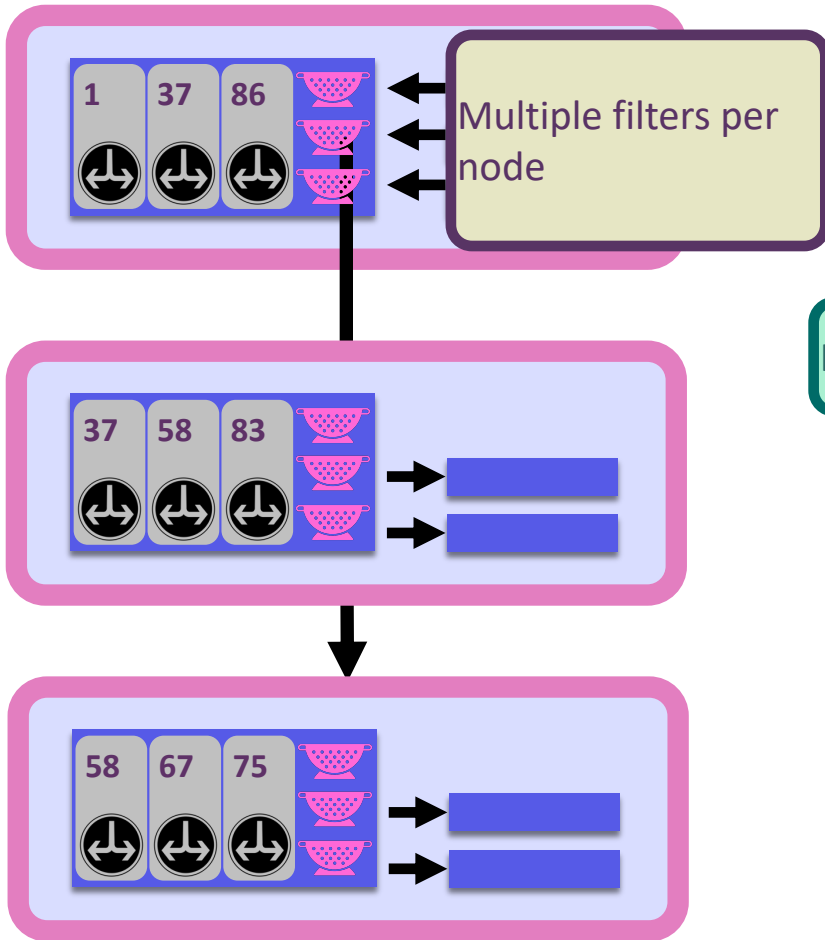
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High Memory/Hot Queries

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Medium Memory

1 IO per query,
CPU cost of filter lookups \Rightarrow more threads

Low Memory

Filters paged out to storage,
Lookup performance degrades

Maplets

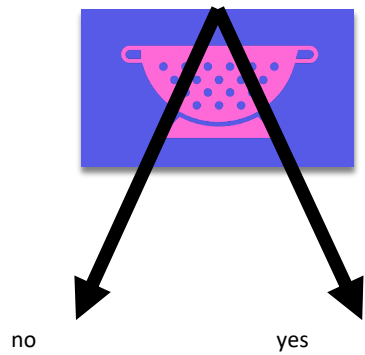
Maplets

A maplet is a filter which can also store small values

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Is X in the set?



Filter

Maplets

A maplet is a filter which can also store small values

Is X in the set?



no

yes

Filter

Is X in the set?



no

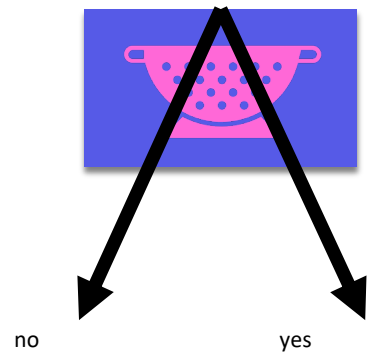
yes, 4

Maplet

Maplets

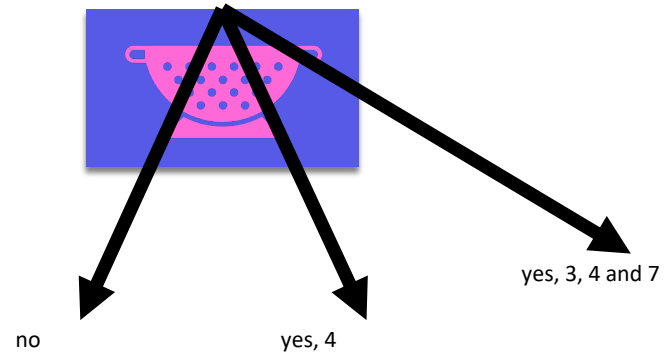
A maplet is a filter which can also store small values

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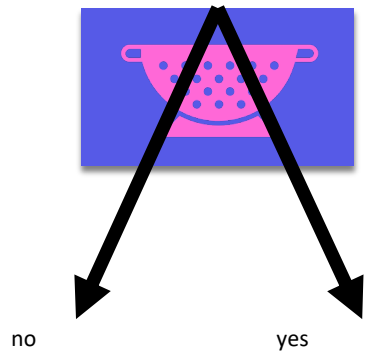


Maplet

Maplets

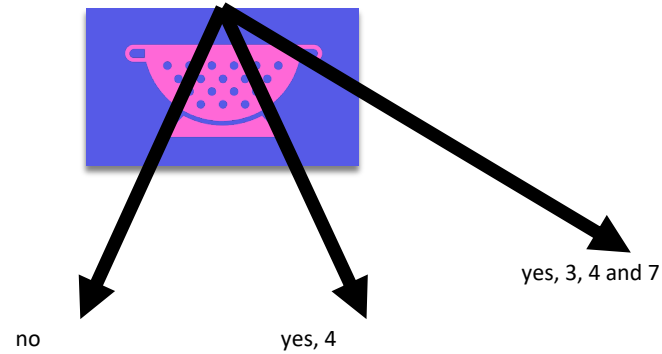
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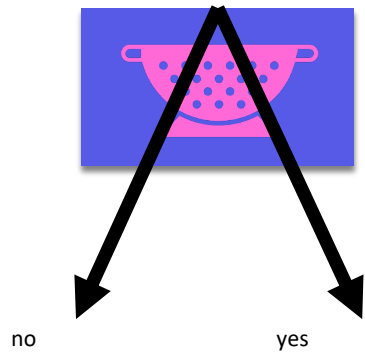
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No false negatives, same false positive guarantee

Maplets

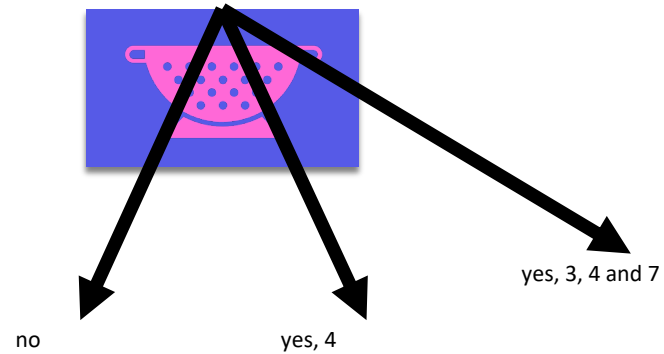
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Is X in the set?



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Maplet

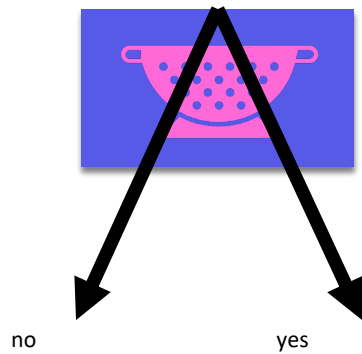
No false negatives, same false positive guarantee

Same memory footprint as multiple filters

Maplets

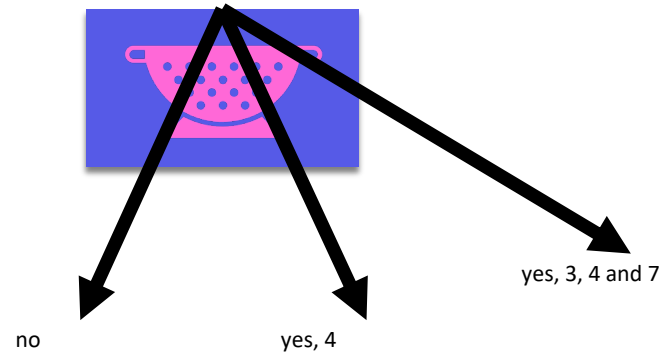
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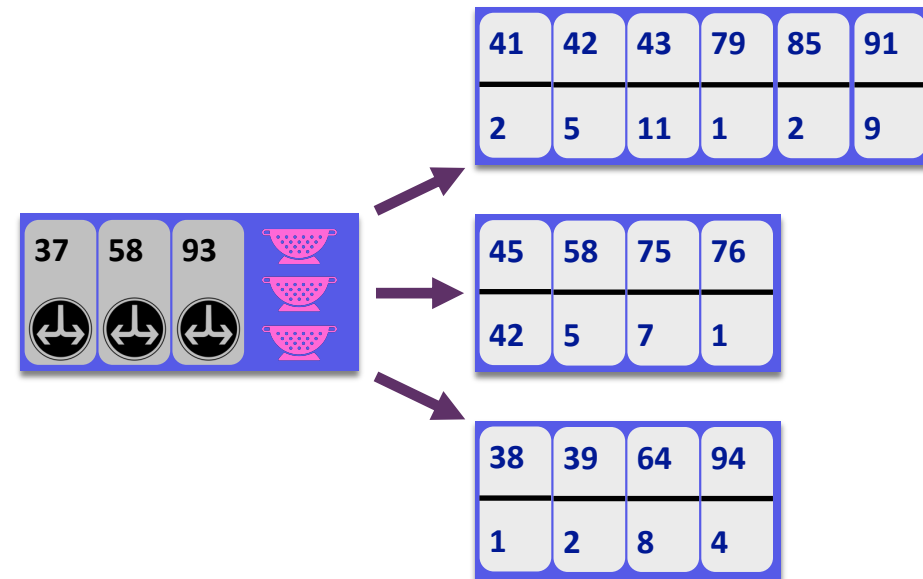
Lookups same cost as 1 quotient filter:
2 cache line misses
1 IO

Mapped B^ϵ -Trees

SplinterDB and Maplets: Improving the Trade-Offs in LSM Compaction Policy
Conway, Farach-Colton, Johnson,
SIGMOD 2023

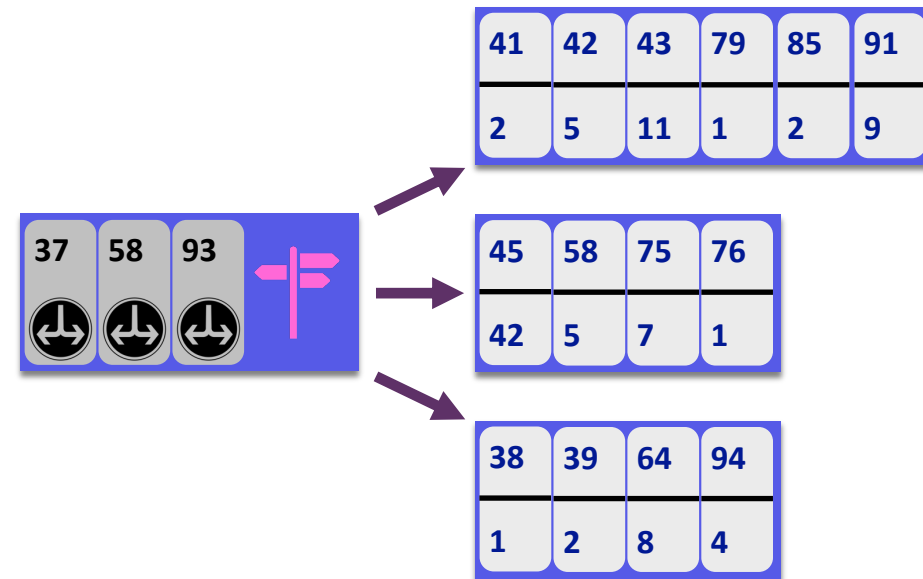
Mapped B^ϵ -Trees

Replace individual filters with a single maplet



Mapped B^ϵ -Trees

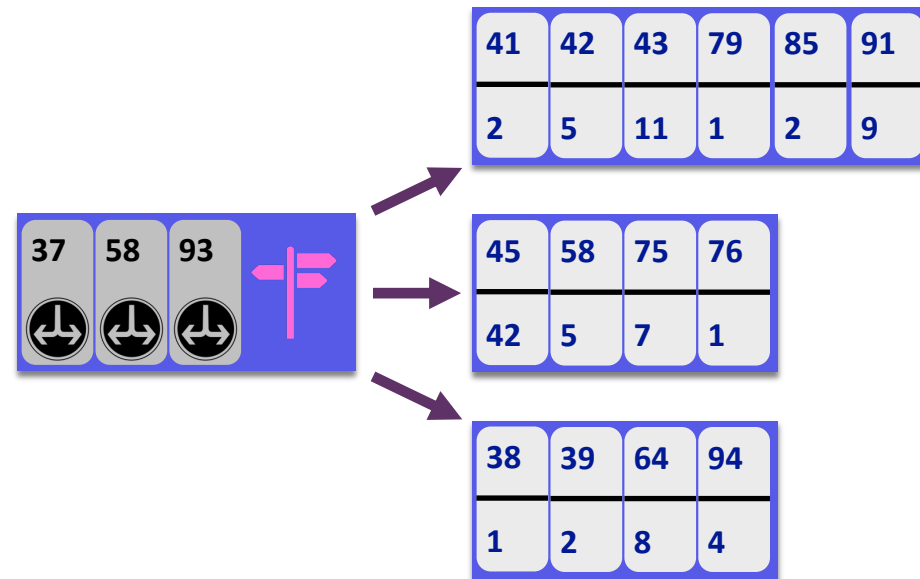
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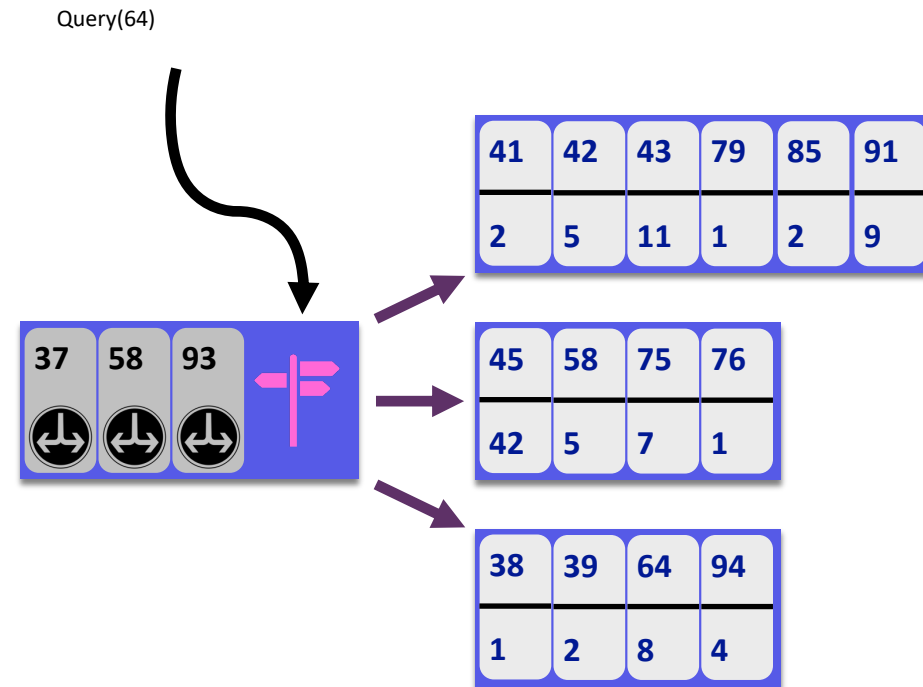
Use the values to store which buffers contain matching keys



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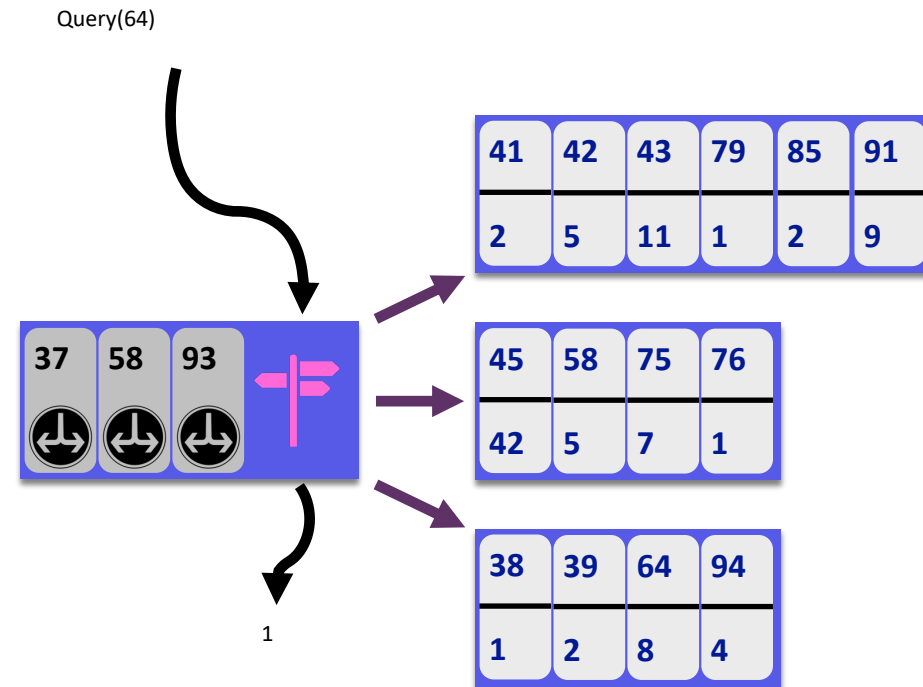
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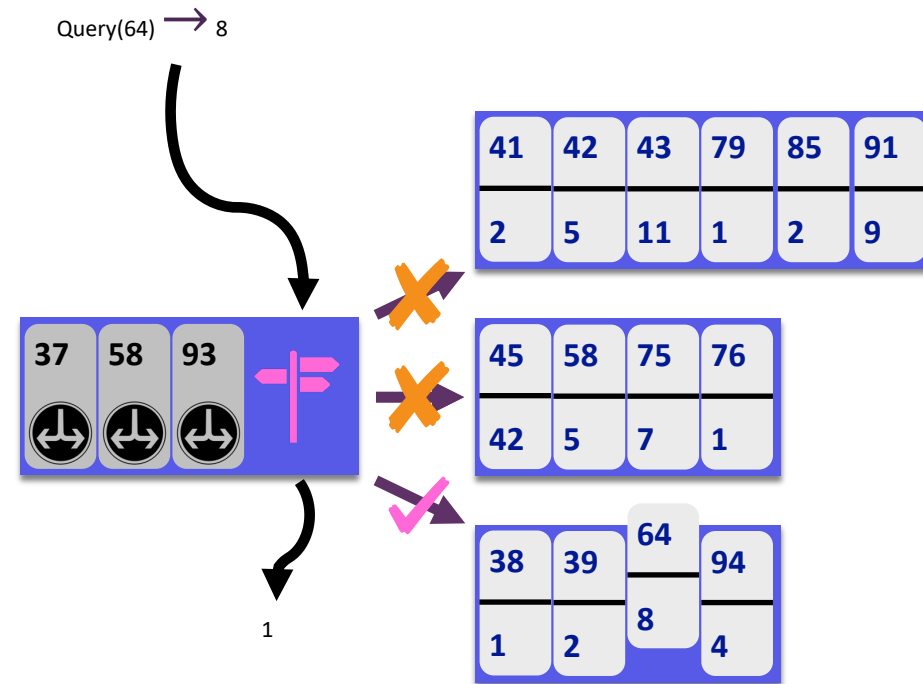
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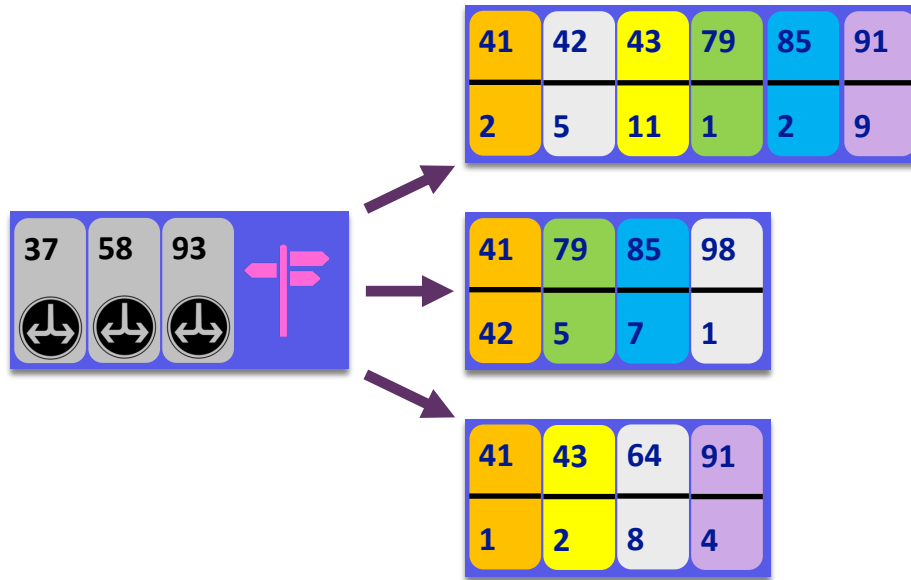
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Using Maplets to Manage Space

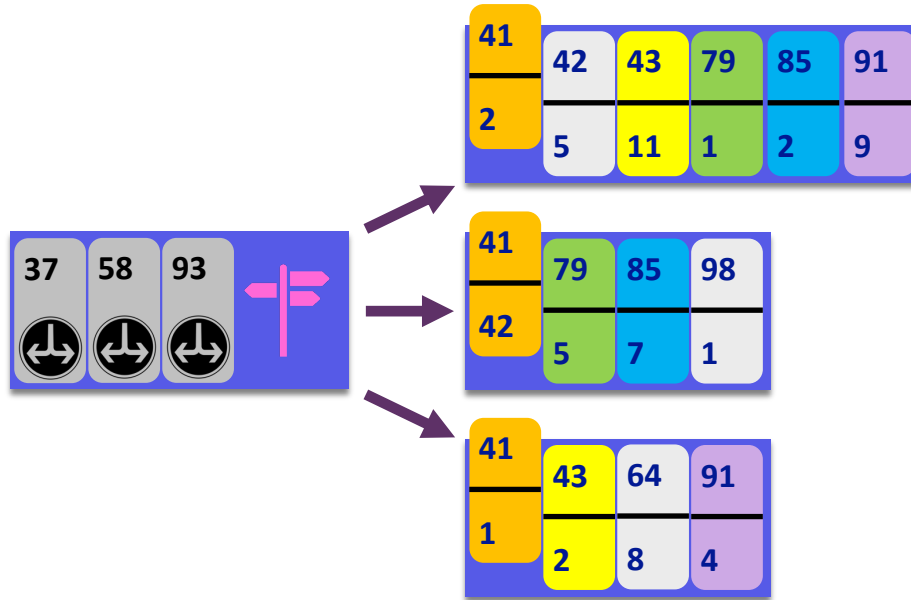
Using Maplets to Manage Space

Size-tiering can lead to redundant data, wasting space



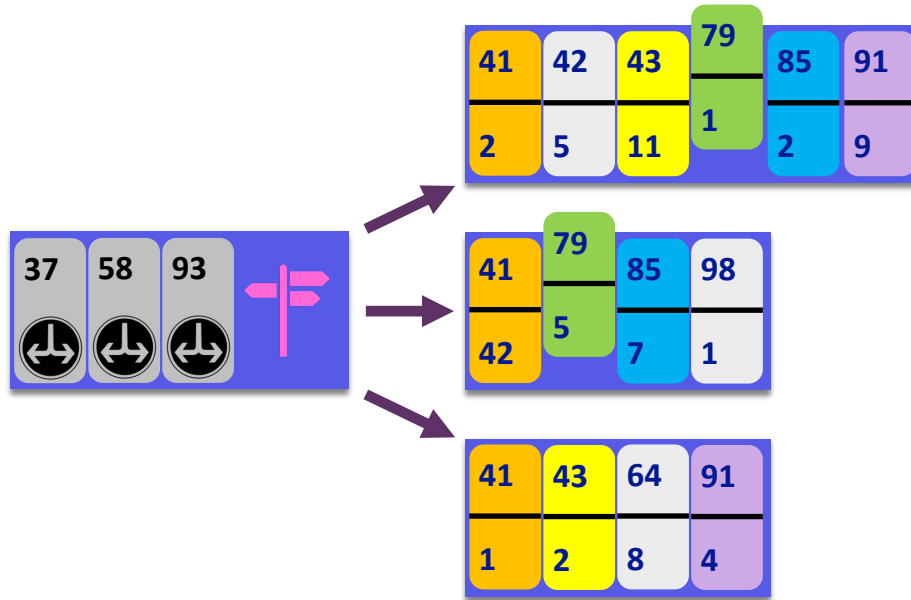
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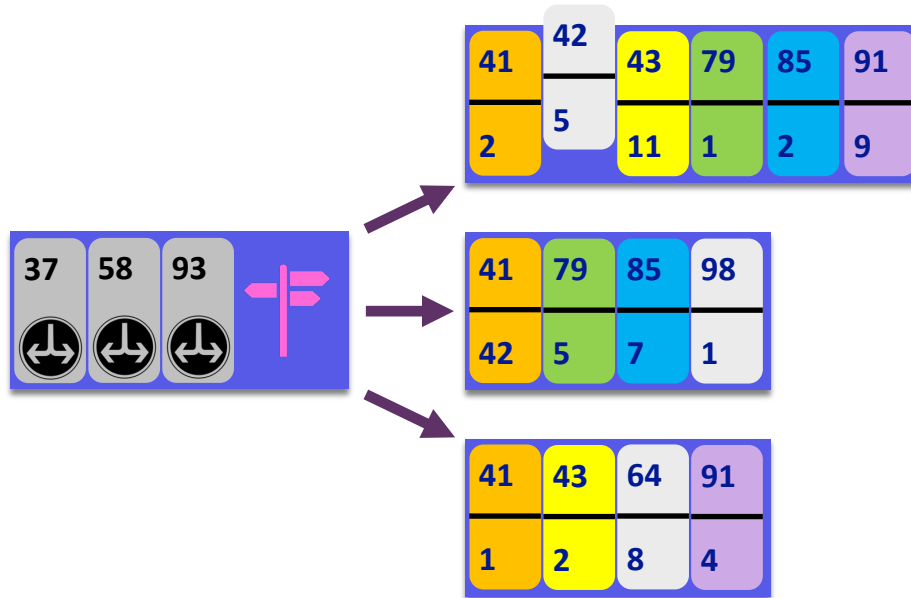
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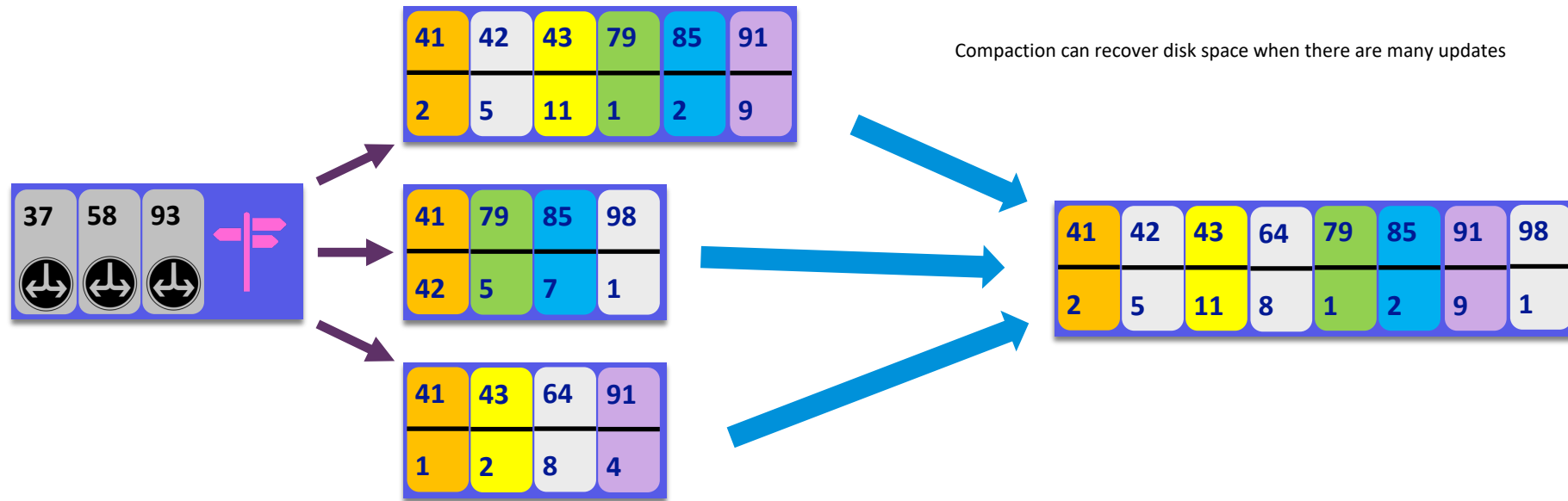
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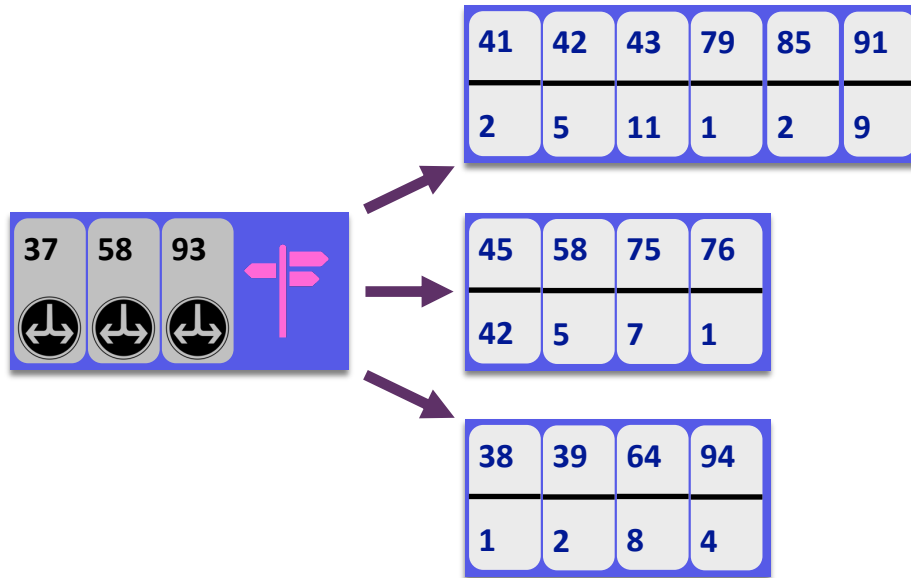
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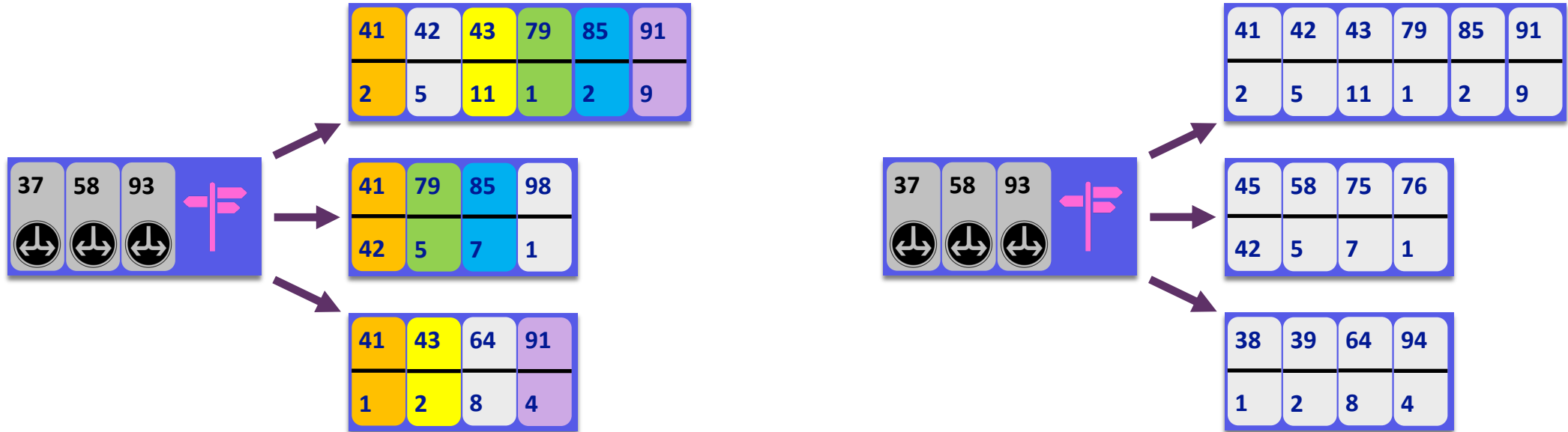
Compaction saves little space when there is little redundant data



So we don't want to waste time compacting branches with few updates

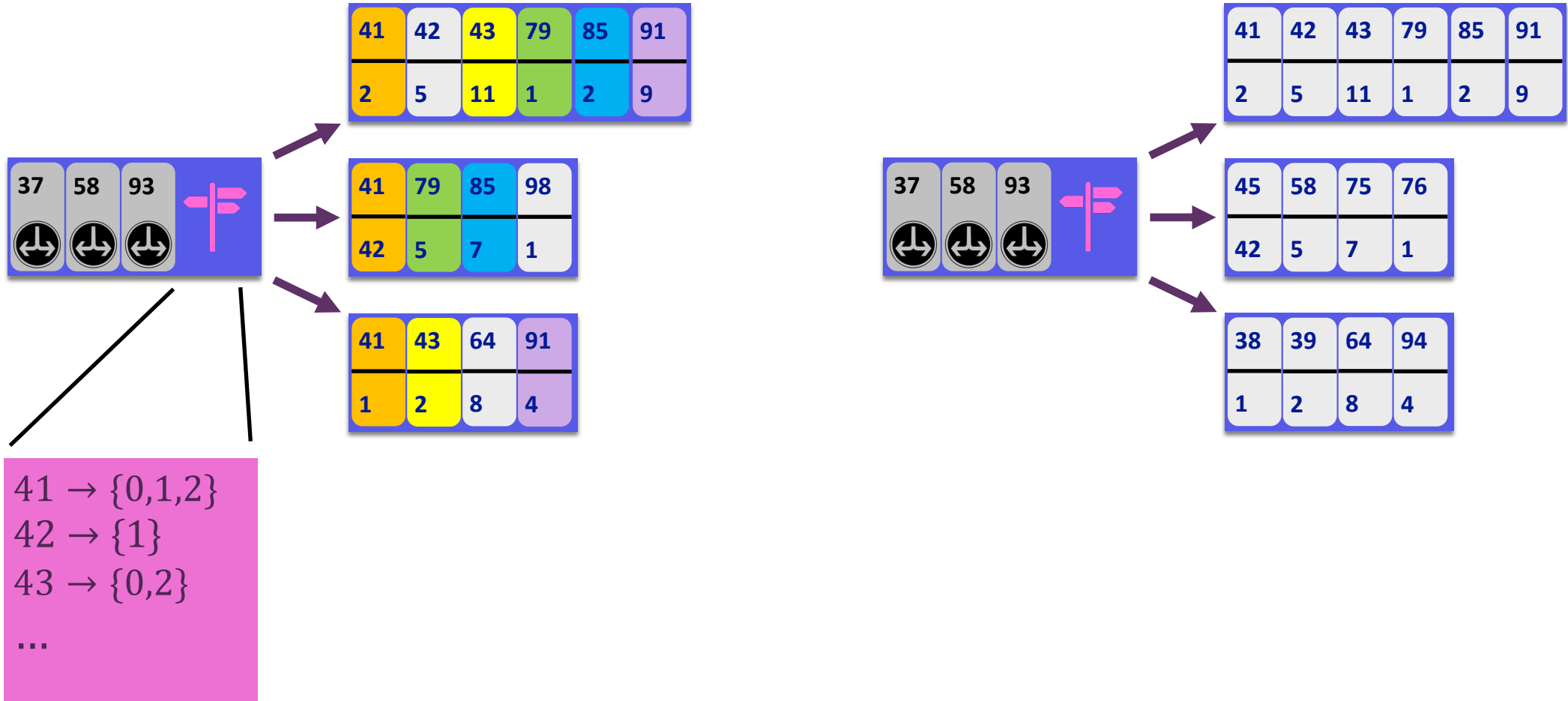
Using Maplets to Manage Space

Maplets can tell us how much redundant data there is



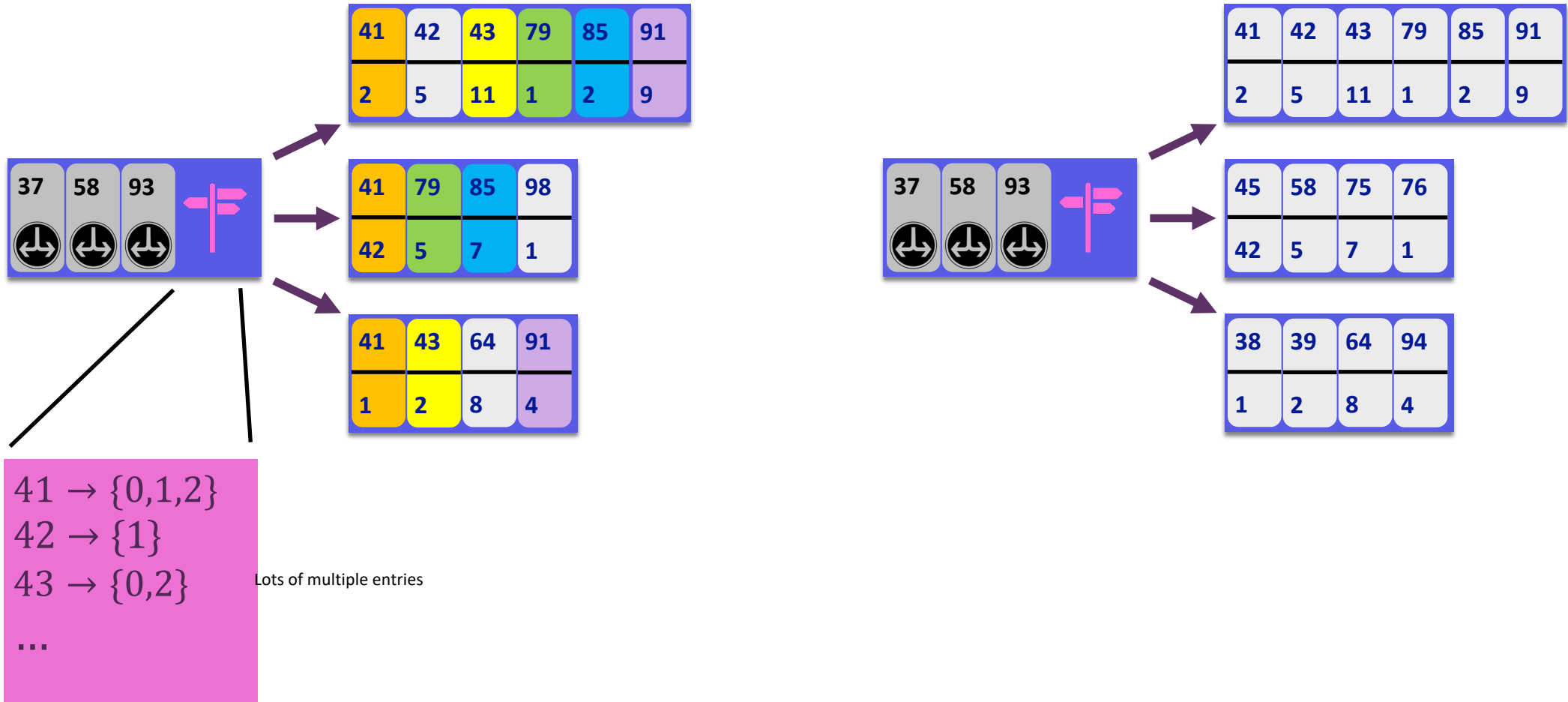
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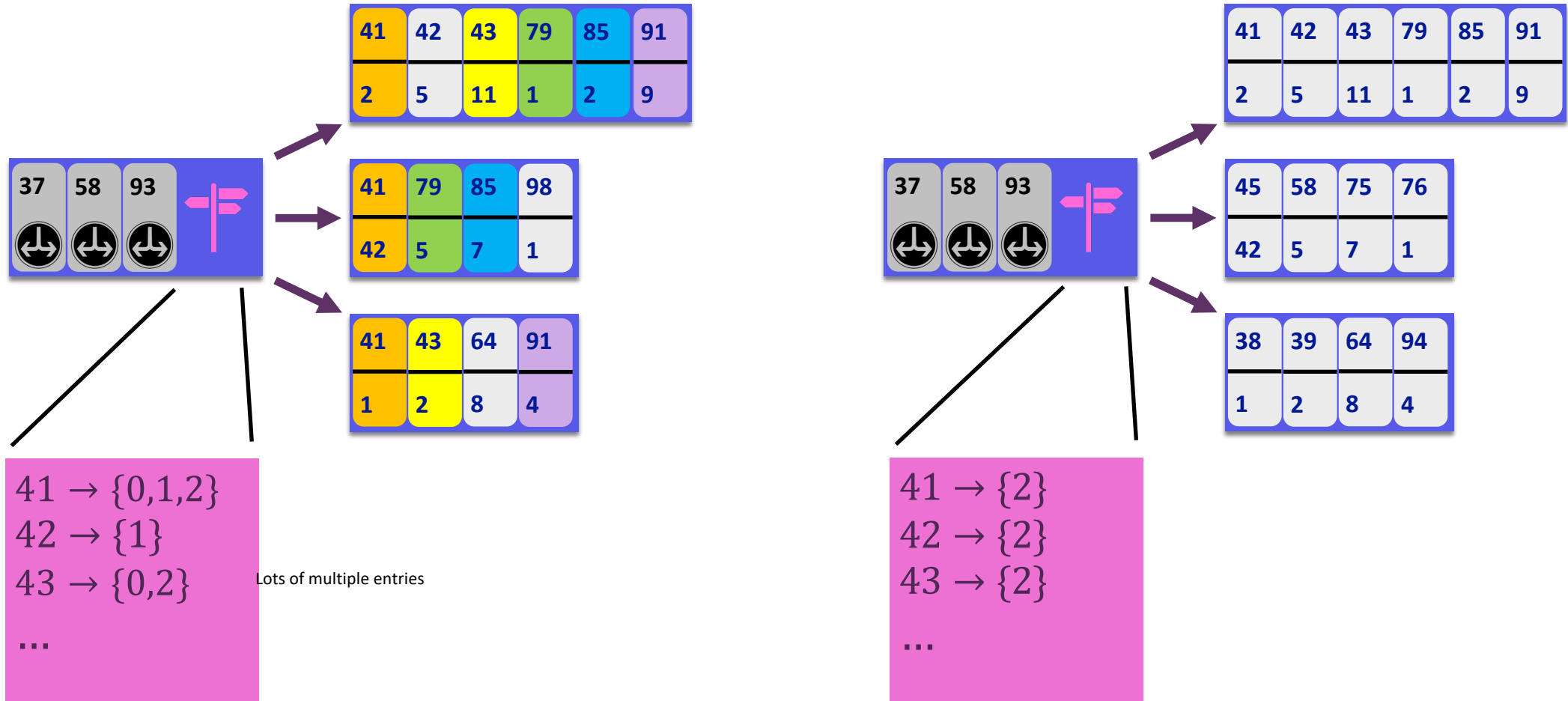
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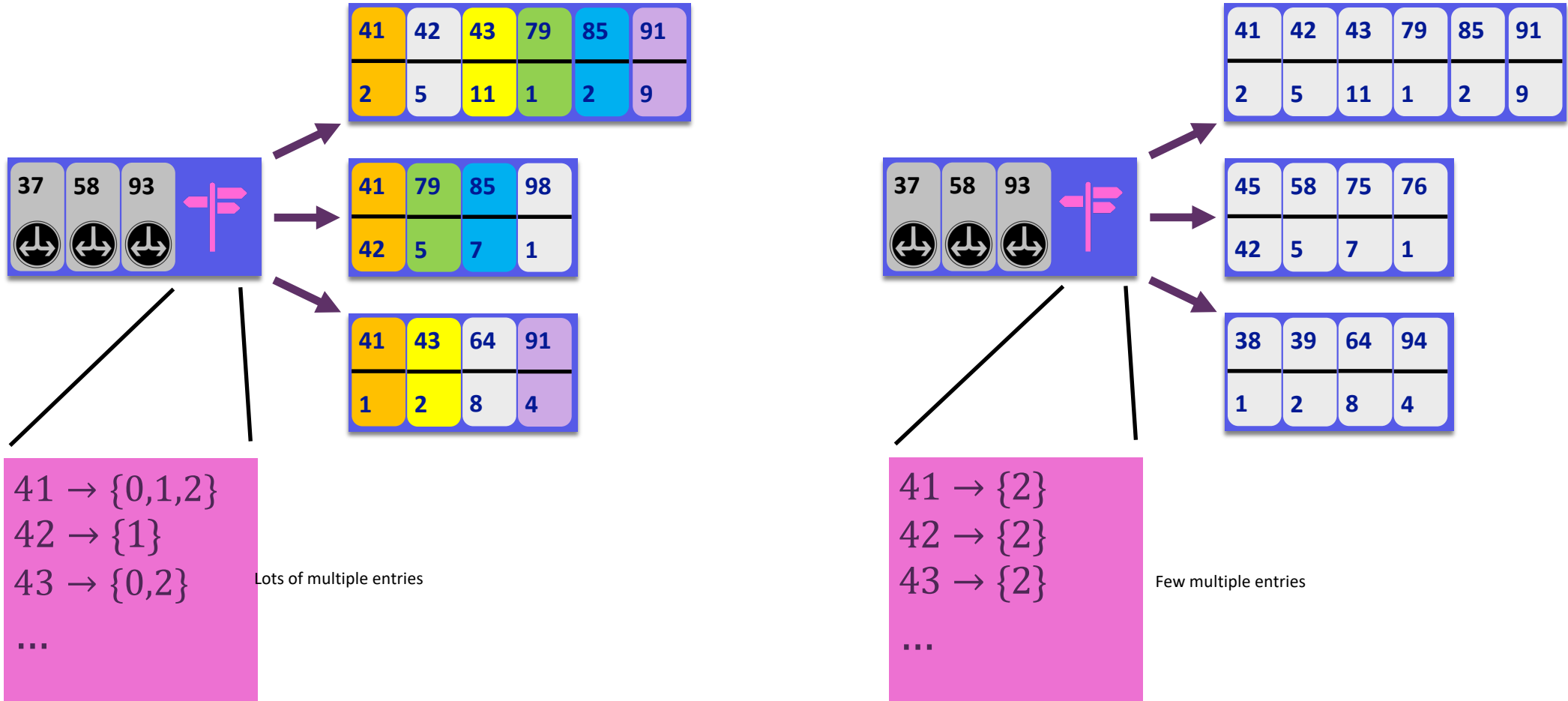


Lots of multiple entries

Maplet

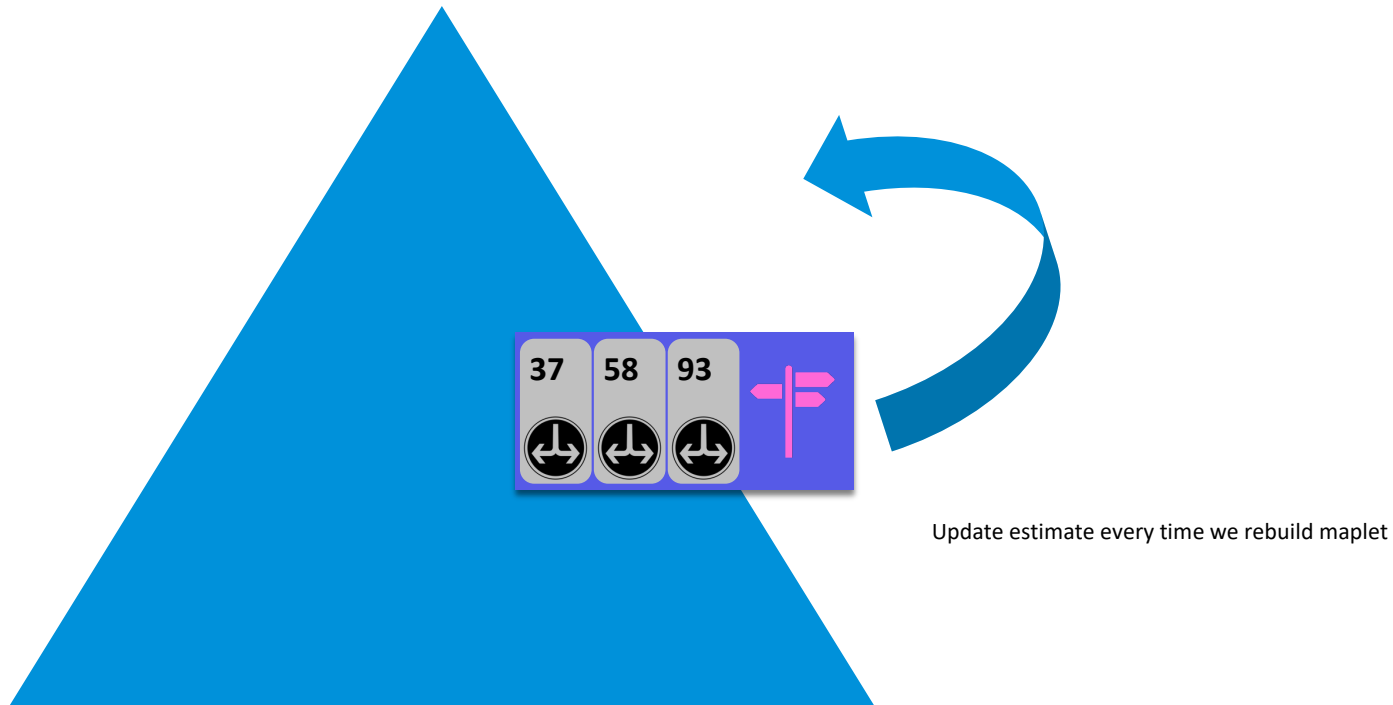
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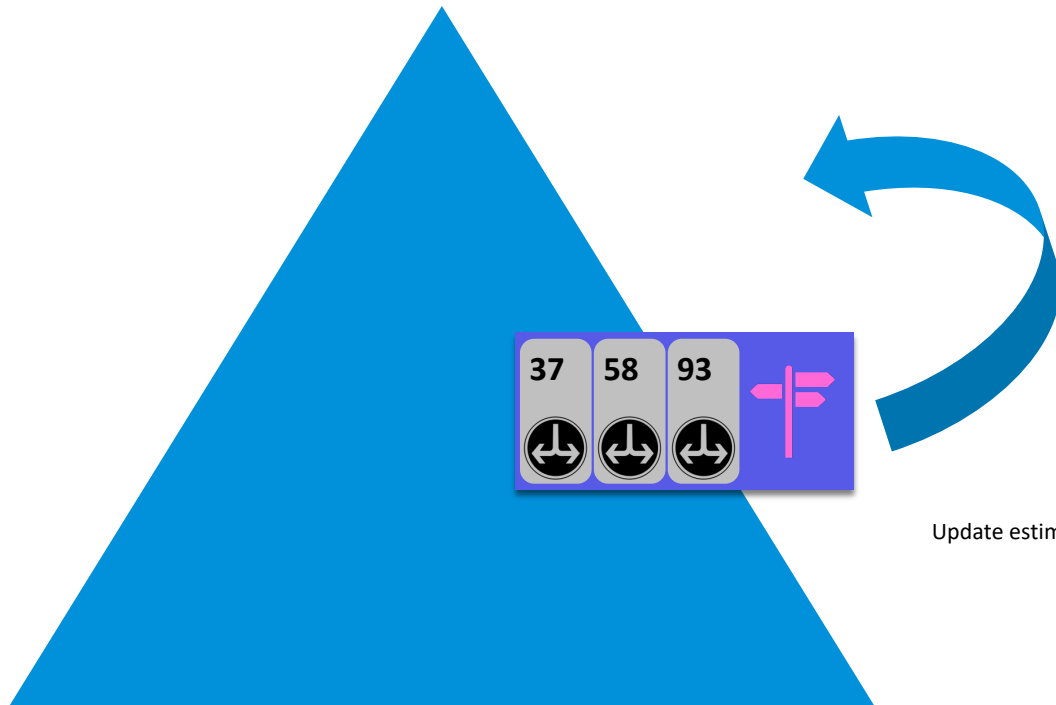
SplinterDB Adaptive Space Reclamation

SplinterDB maintains a heap of trunk nodes, sorted by estimated amount of redundant data

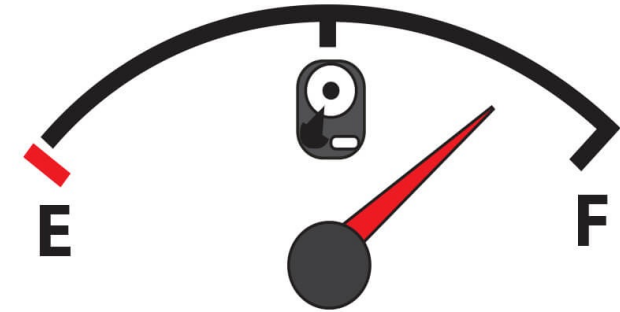


SplinterDB Adaptive Space Reclamation

SplinterDB maintains a heap of trunk nodes, sorted by estimated amount of redundant data



Update estimate every time we rebuild maplet



Whenever disk usage gets too high, SplinterDB initiates compaction on top node of the heap.

Goal: maximal gains, minimal pains

SplinterDB

28 2Ghz cores

Intel Optane 905P

24B keys 100B values

25GiB RAM
80GiB dataset

● SplinterDB+Maplets ■ SplinterDB ▲ RocksDB

Updates/Second

1M 2M 3M



60%

80%

100%

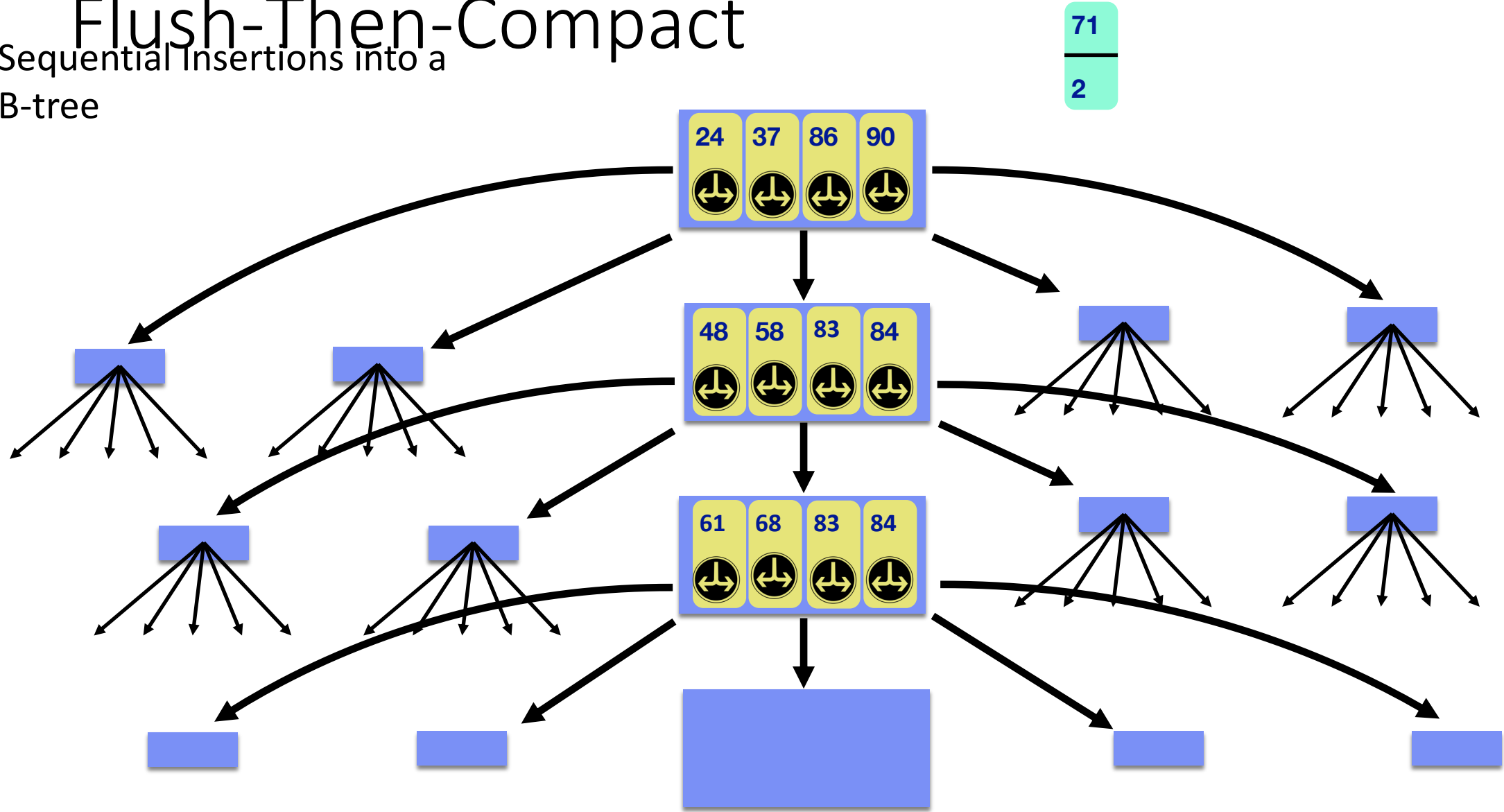
Space Efficiency

100% uniform updates

Flush-Then-Compact

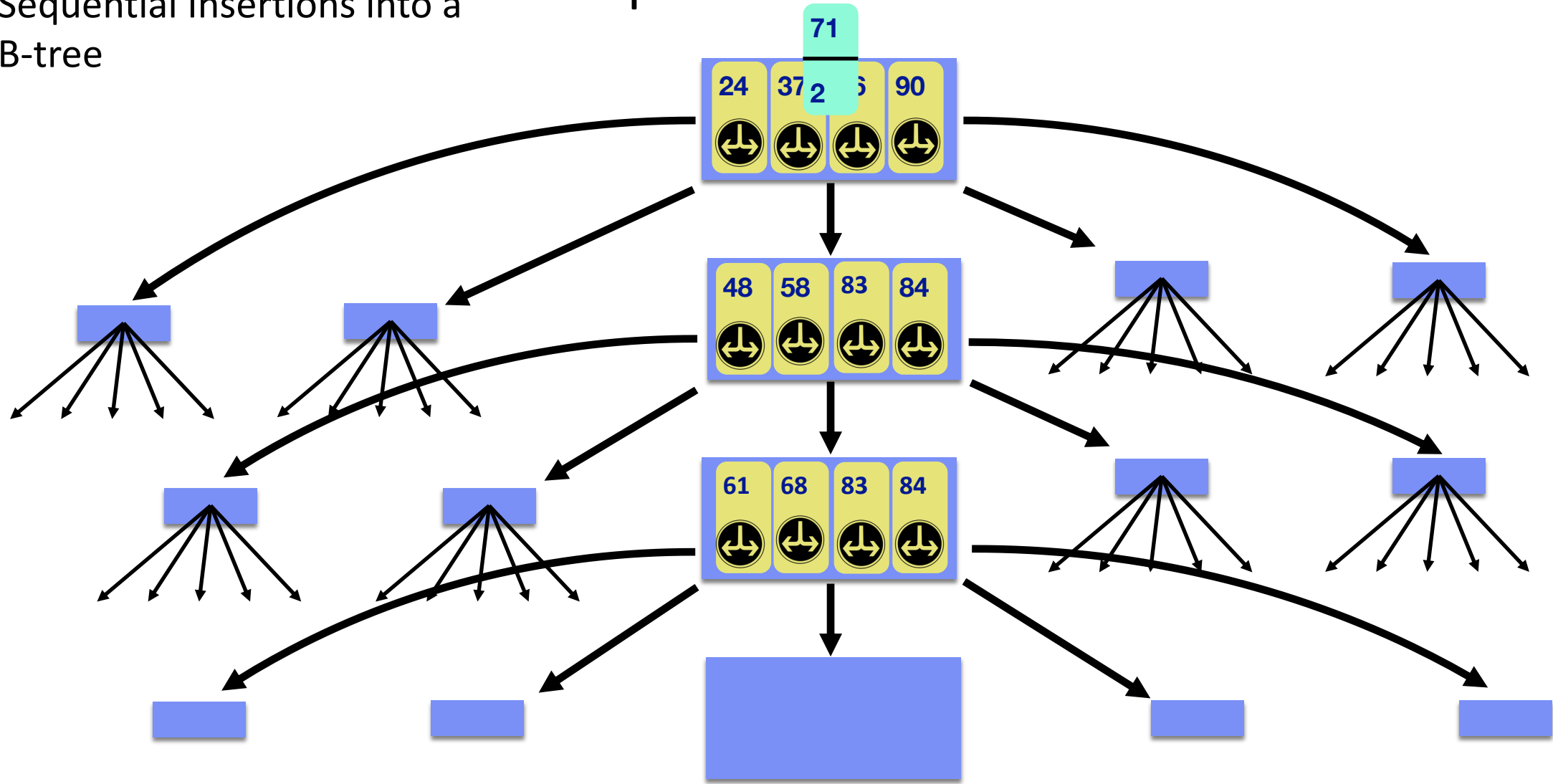
Flush-Then-Compact

Sequential Insertions into a B-tree



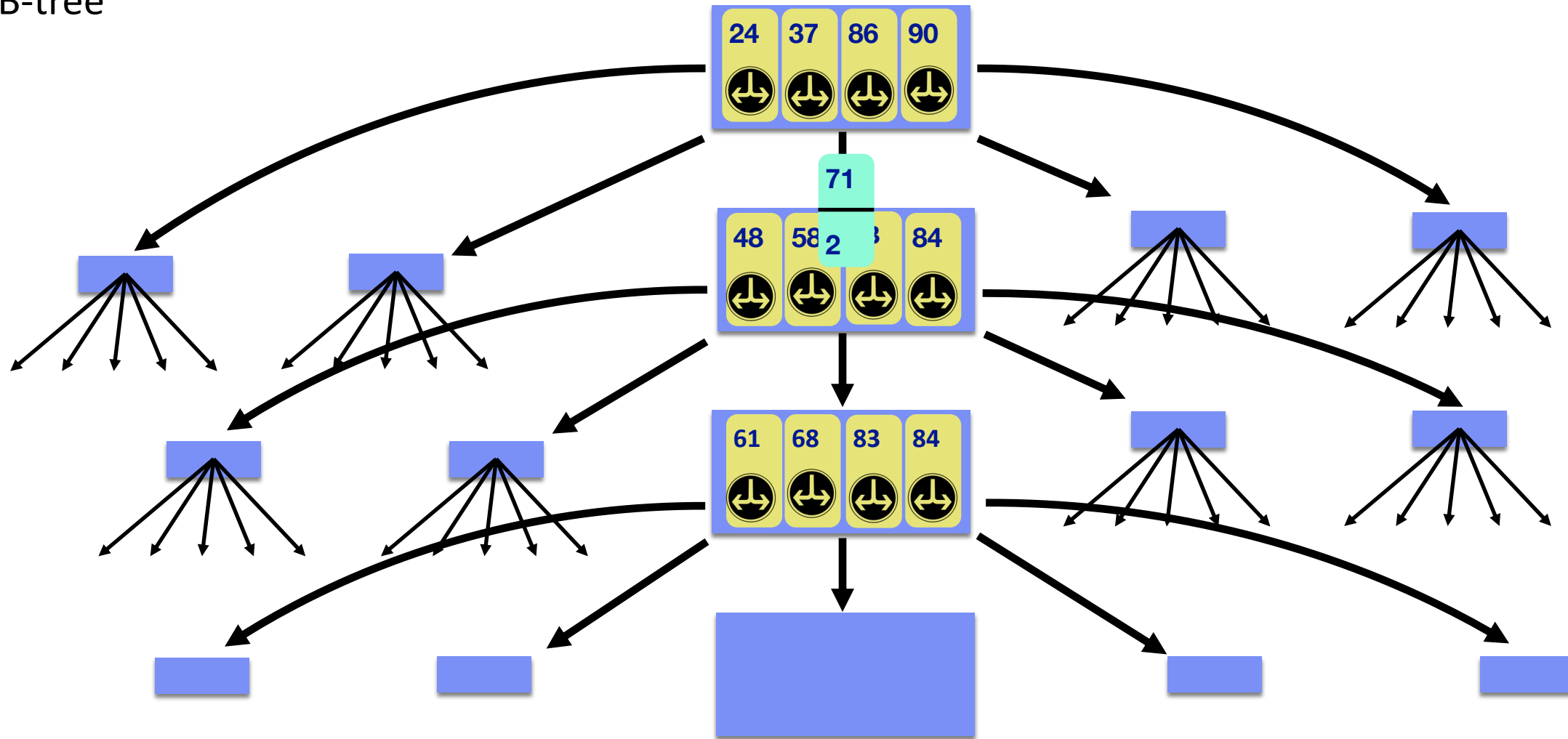
Flush-Then-Compact

Sequential Insertions into a B-tree



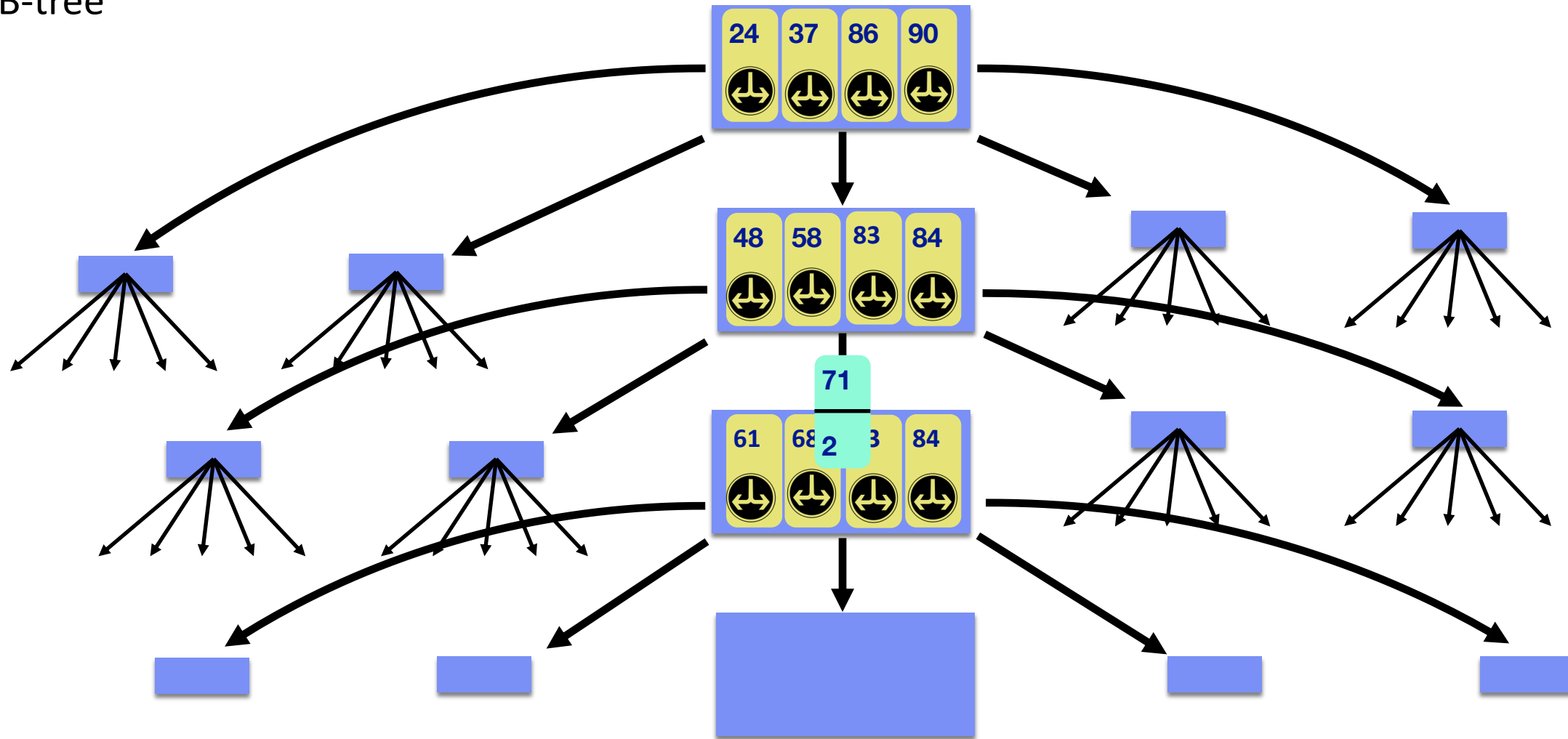
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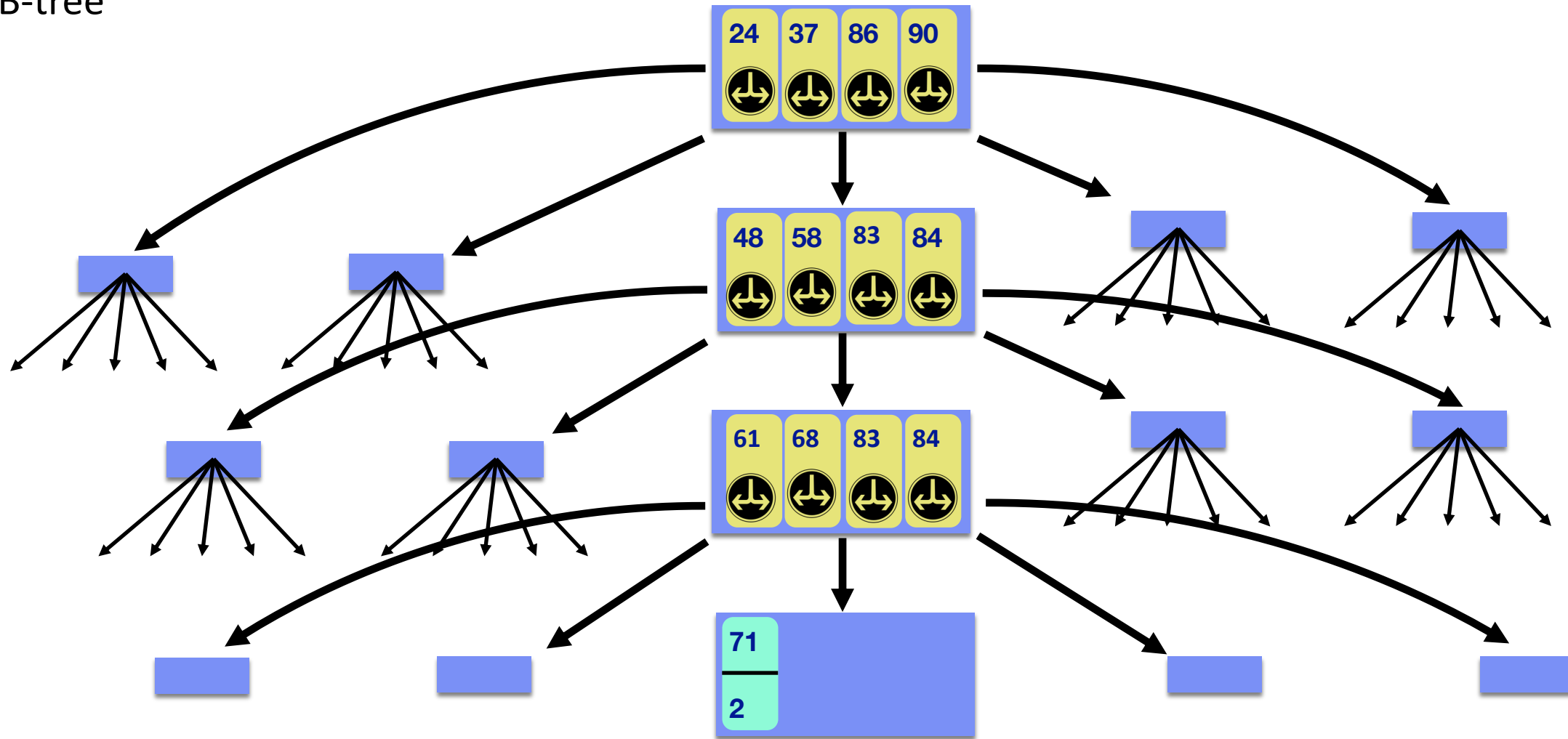
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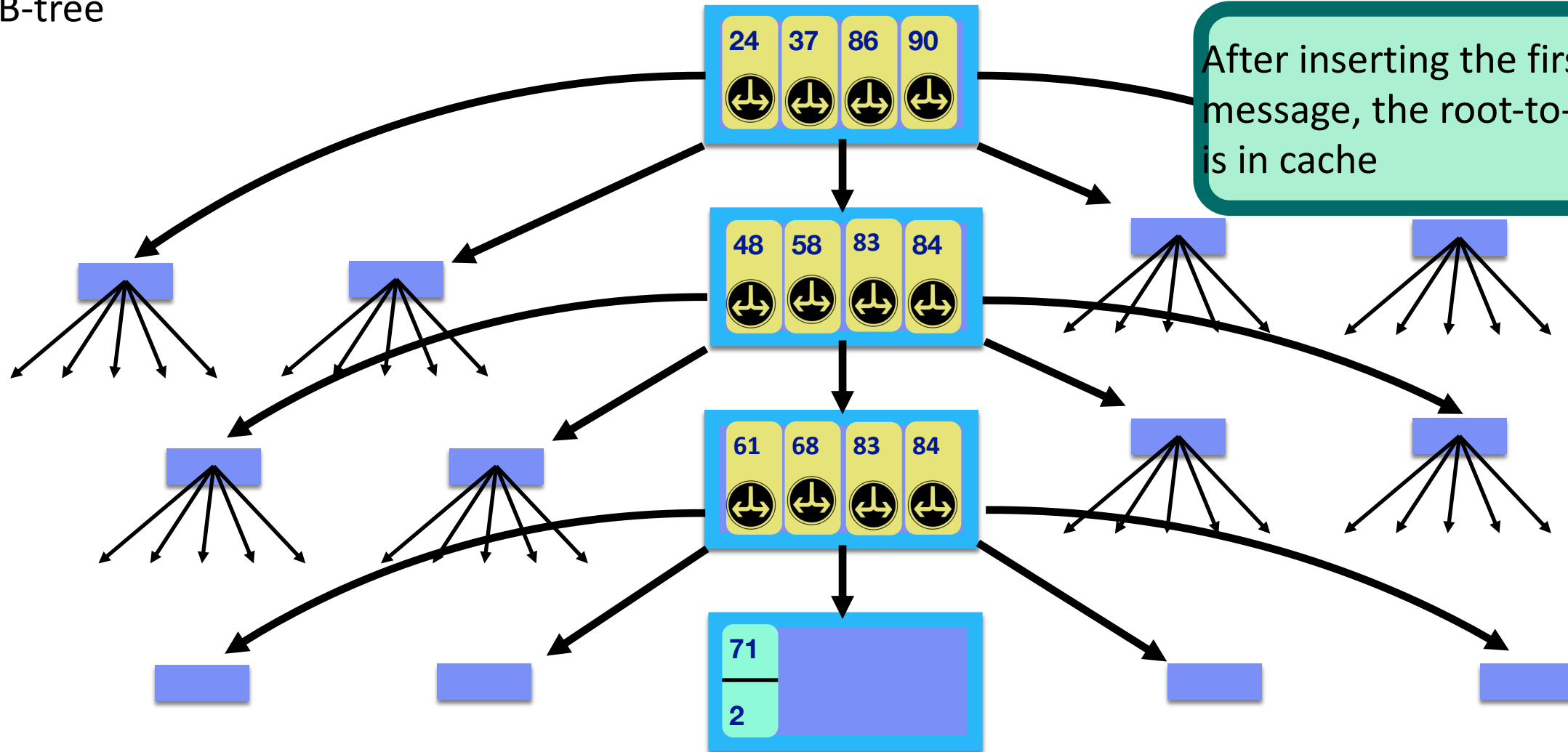
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Flush-Then-Compact

Sequential Insertions into a B-tree



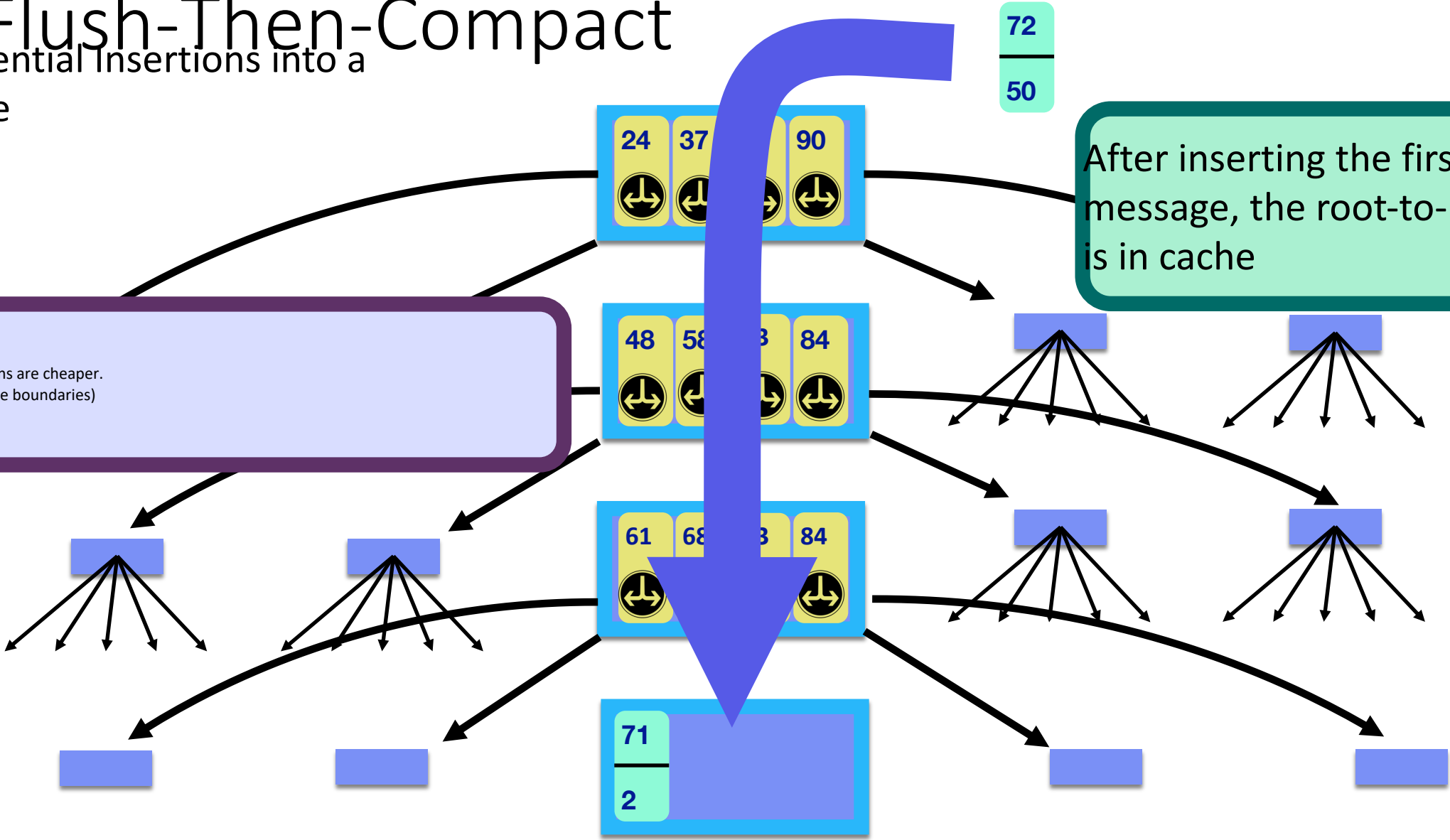
Flush-Then-Compact

Sequential Insertions into a B-tree

72
50

After inserting the first message, the root-to-leaf path is in cache

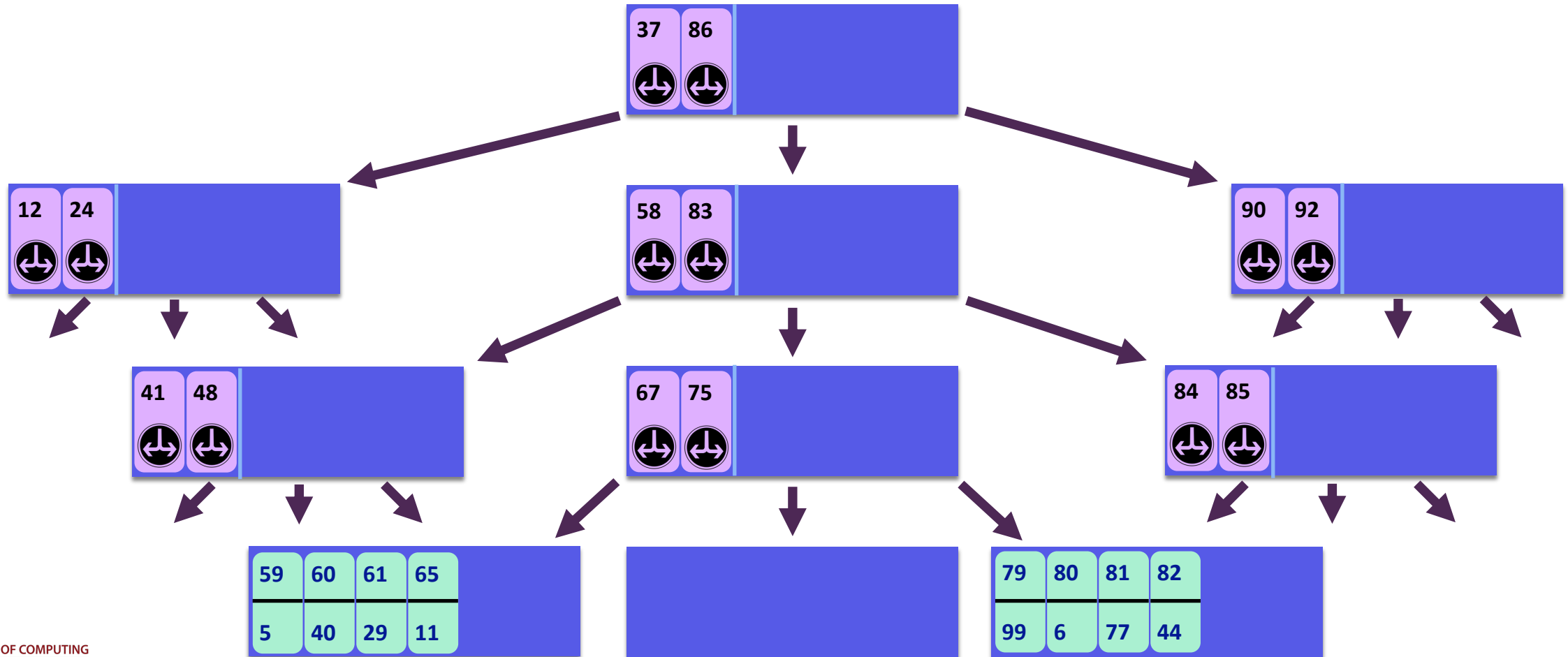
Subsequent insertions are cheaper. (only incur IO at node boundaries)



Flush-Then-Compact

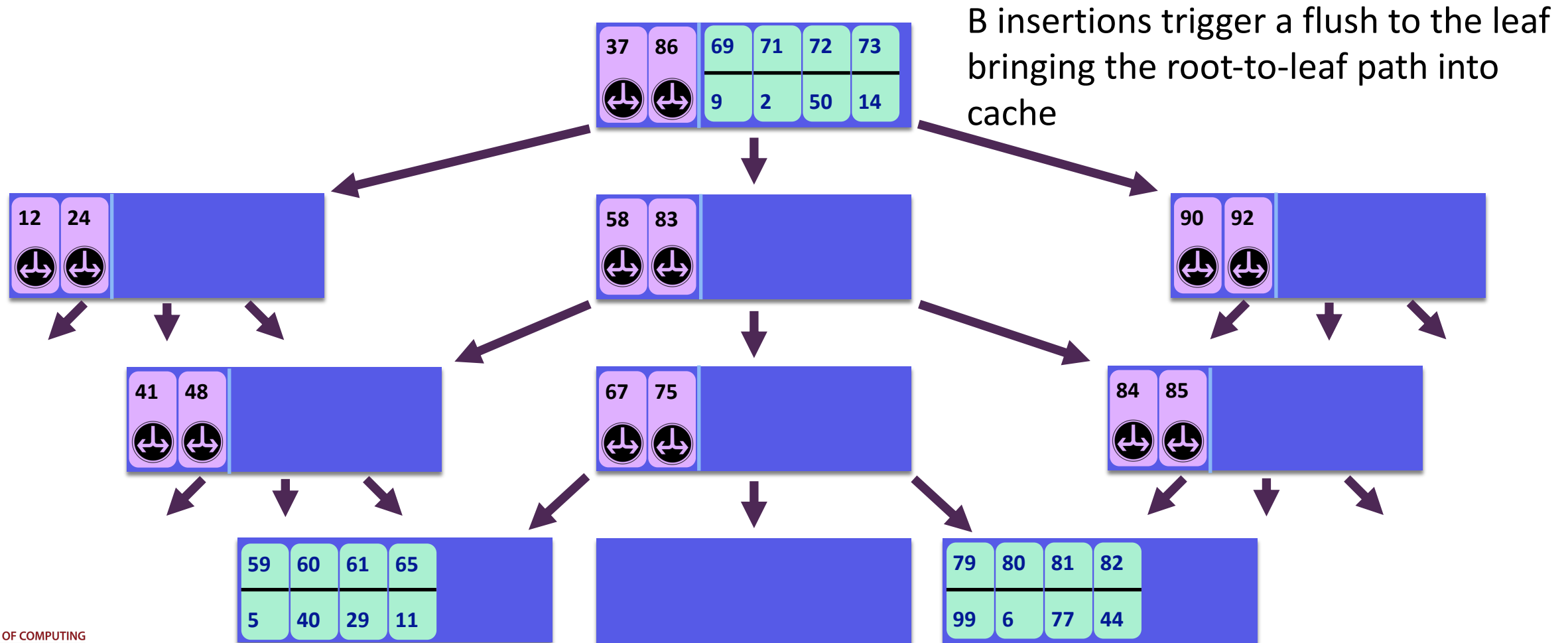
Sequential Insertions into a B^ε-tree

69	71	72	73
9	2	50	14



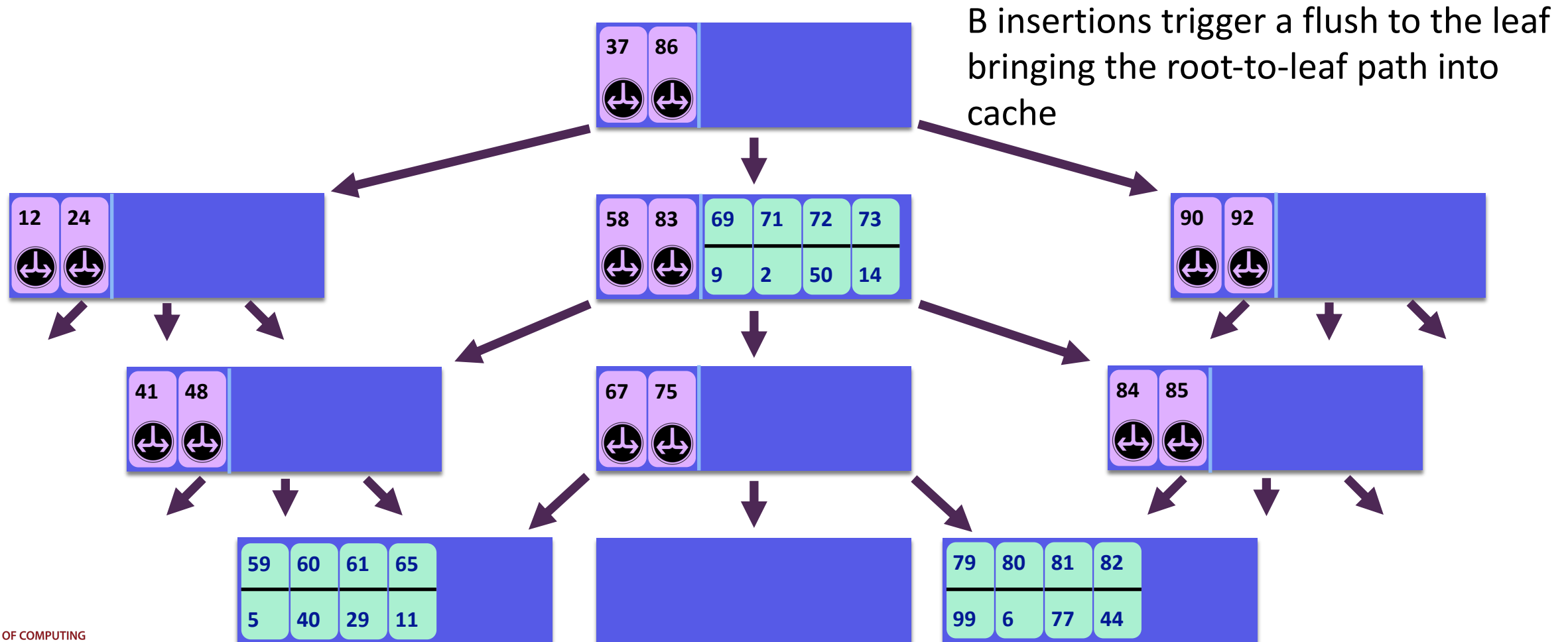
Flush-Then-Compact

Sequential Insertions into a B^E -tree



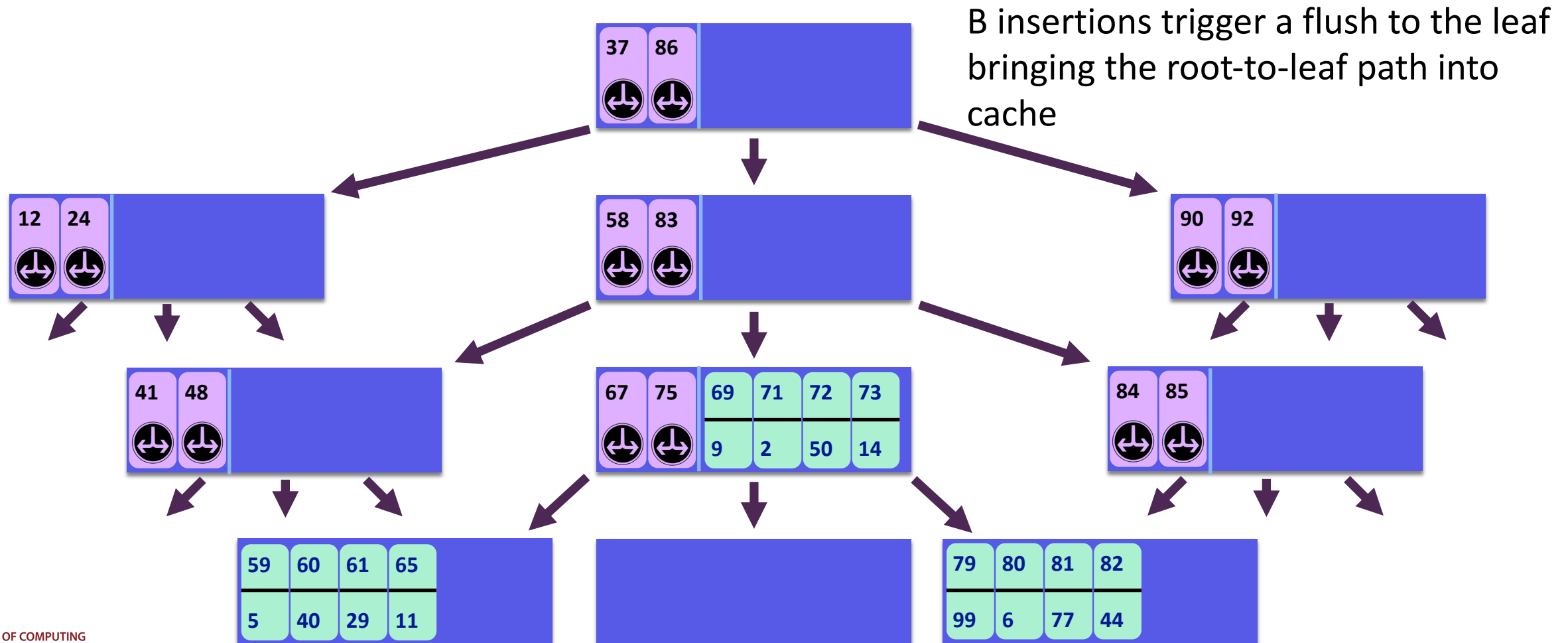
Flush-Then-Compact

Sequential Insertions into a
B^ε-tree



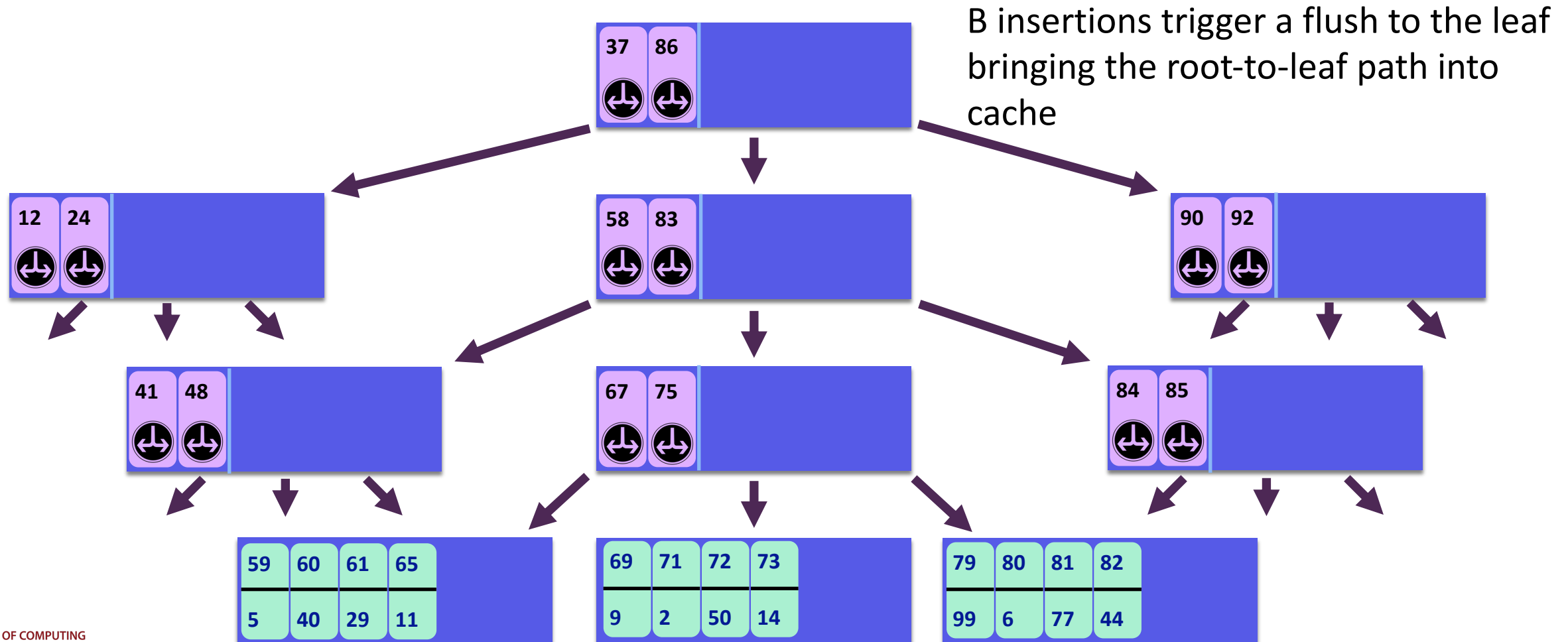
Flush-Then-Compact

Sequential Insertions into a B^E -tree



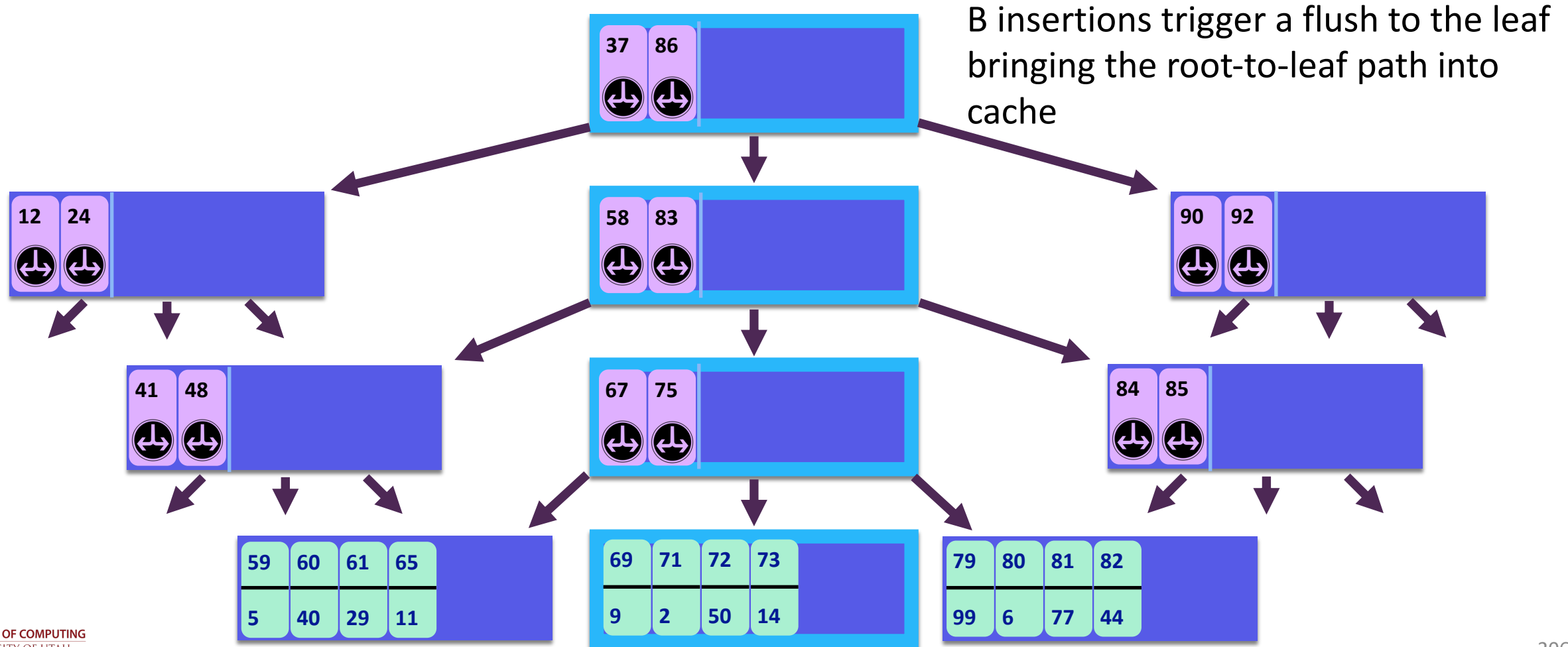
Flush-Then-Compact

Sequential Insertions into a B^E -tree



Flush-Then-Compact

Sequential Insertions into a B^E -tree



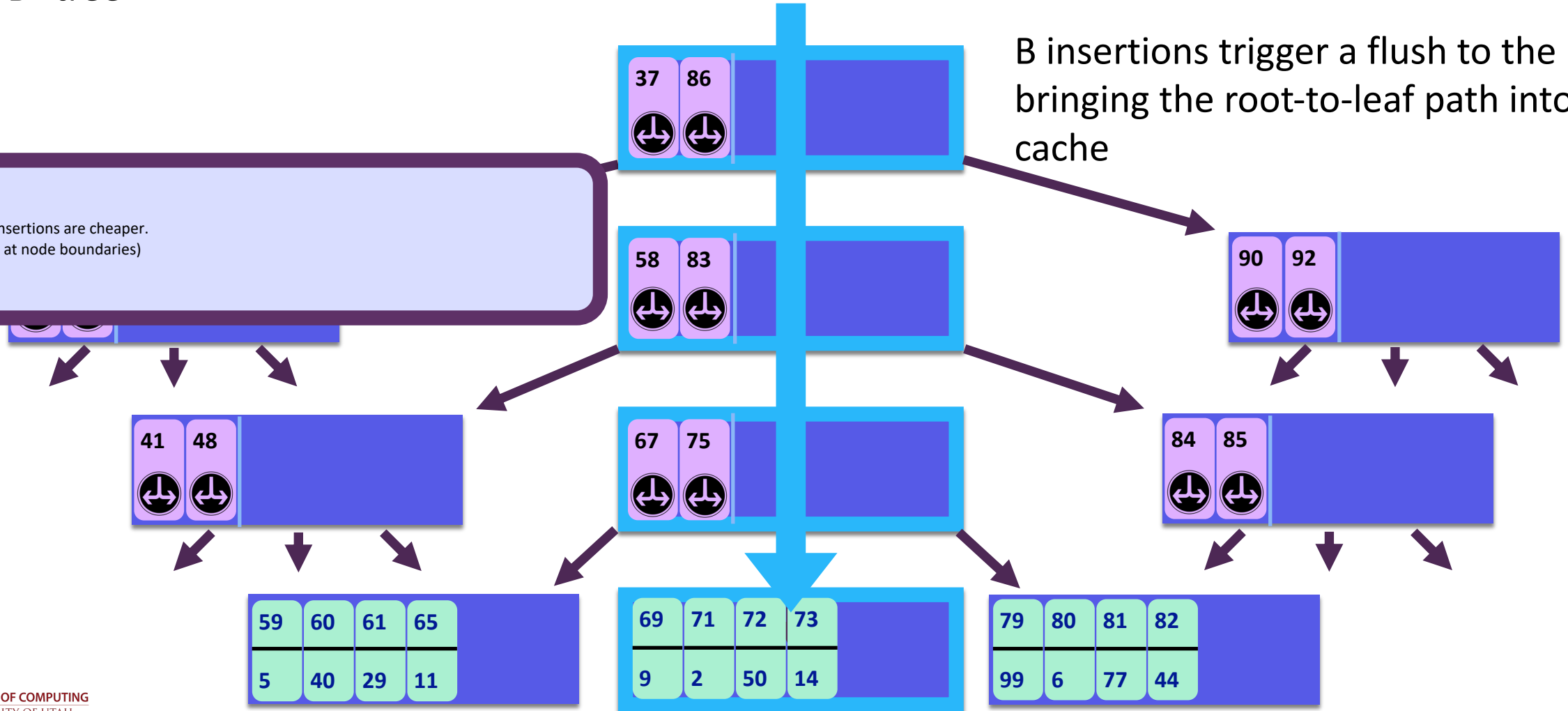
Flush-Then-Compact

Sequential Insertions into a B^E -tree

74	75	76	77
1	2	3	4

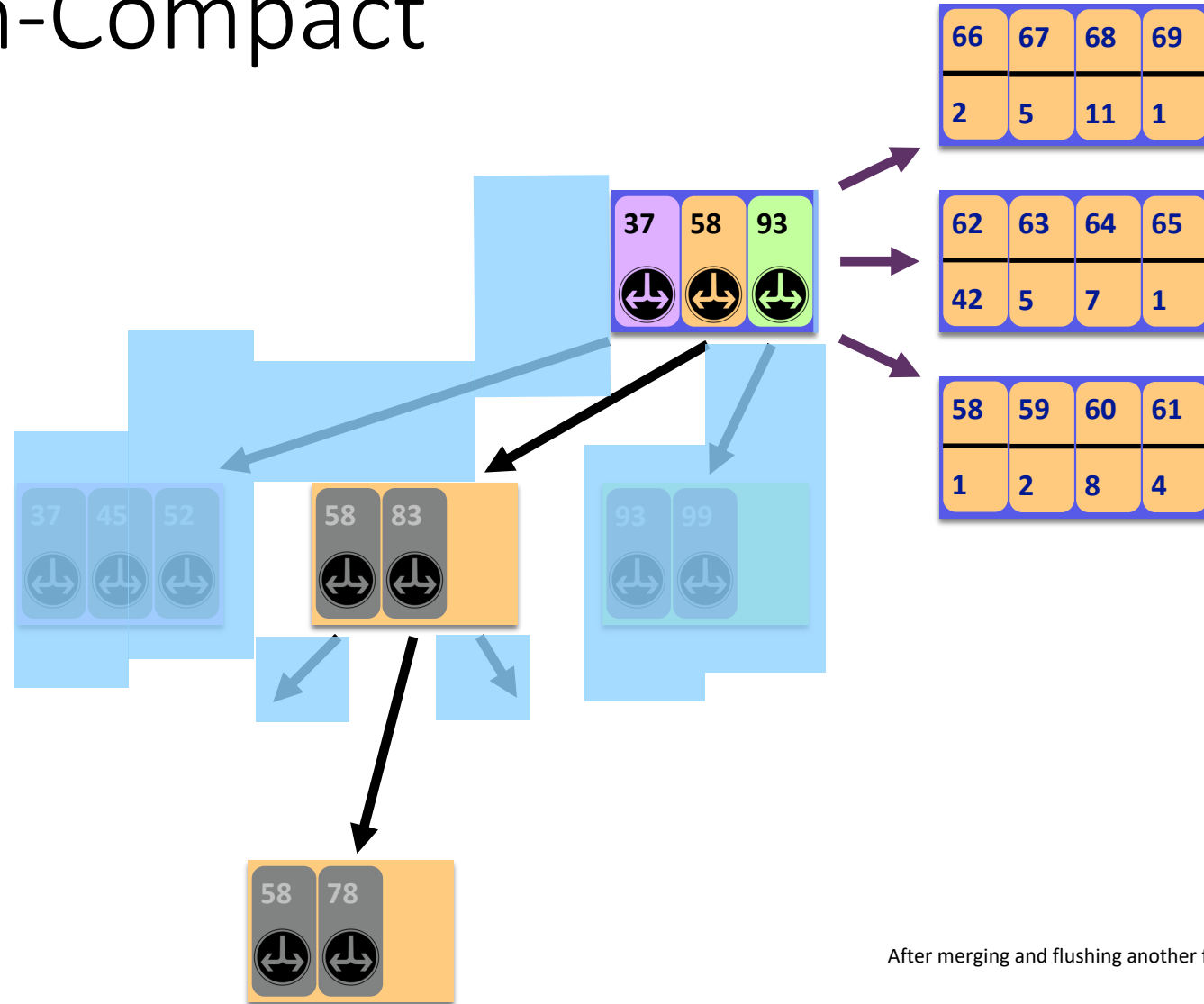
B insertions trigger a flush to the leaf bringing the root-to-leaf path into cache

Subsequent insertions are cheaper. (only incur IO at node boundaries)



Flush-Then-Compact

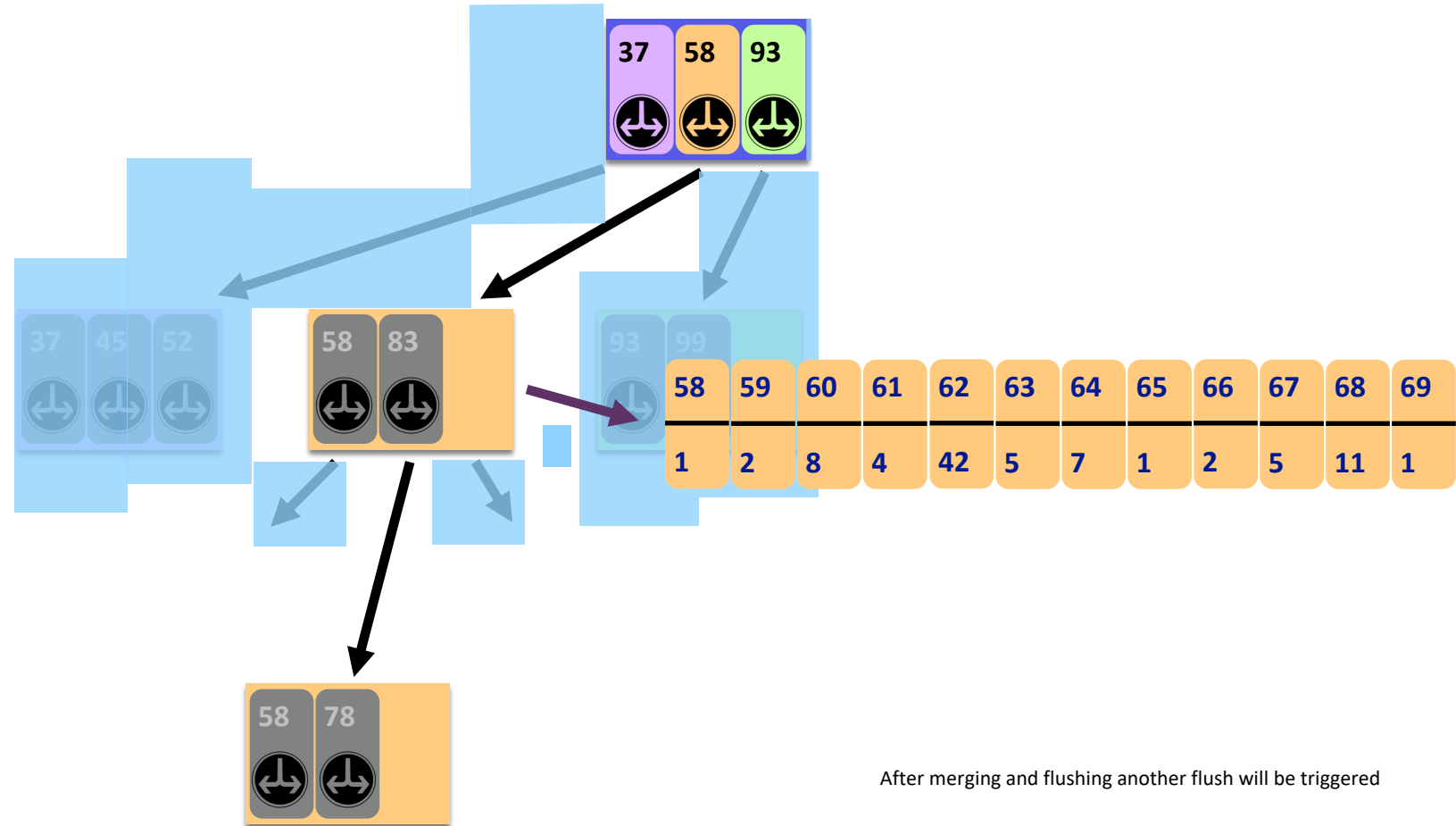
Want:
Cheap sequential insertions



After merging and flushing another flush will be triggered

Flush-Then-Compact

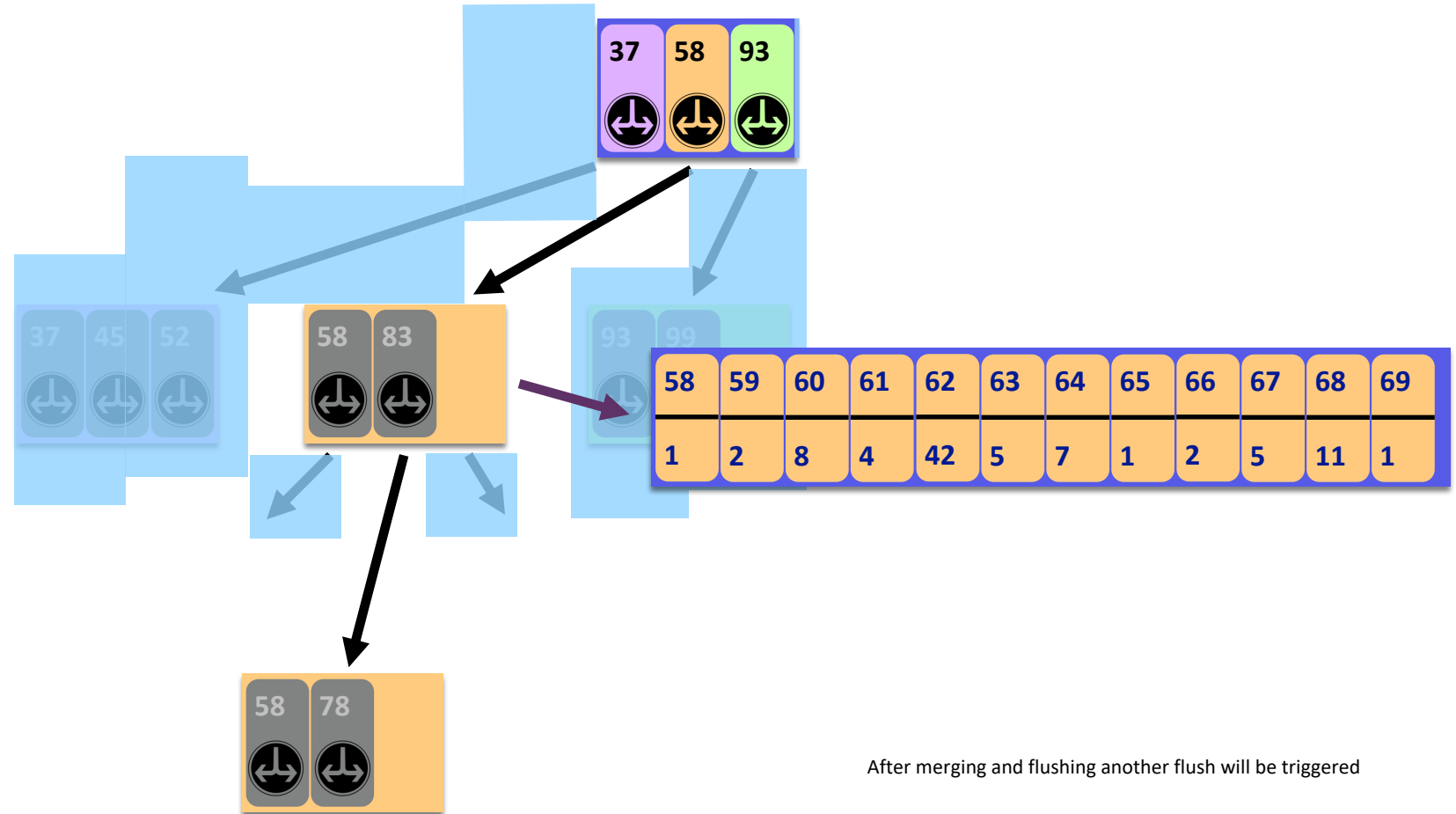
Want:
Cheap sequential insertions



After merging and flushing another flush will be triggered

Flush-Then-Compact

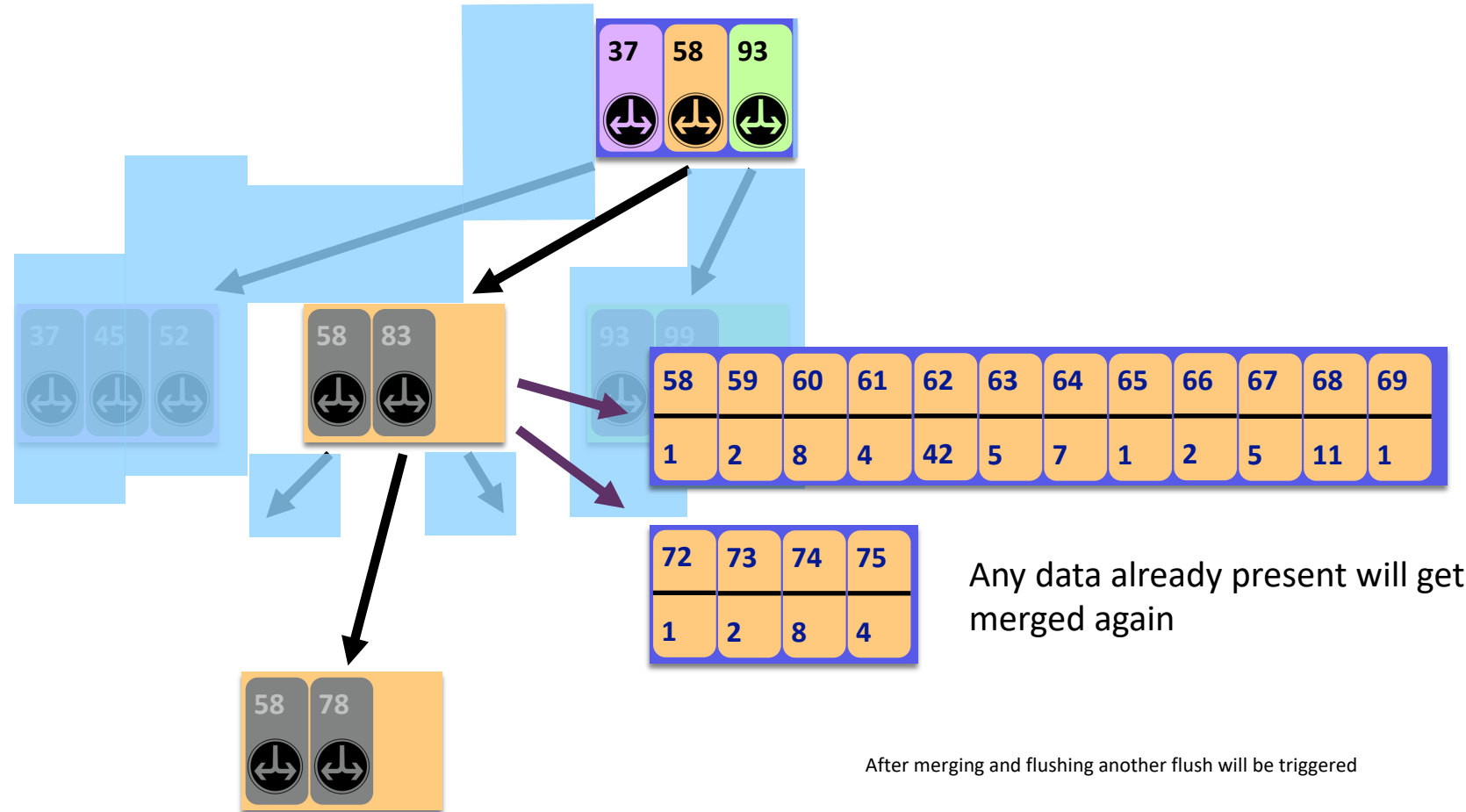
Want:
Cheap sequential insertions



After merging and flushing another flush will be triggered

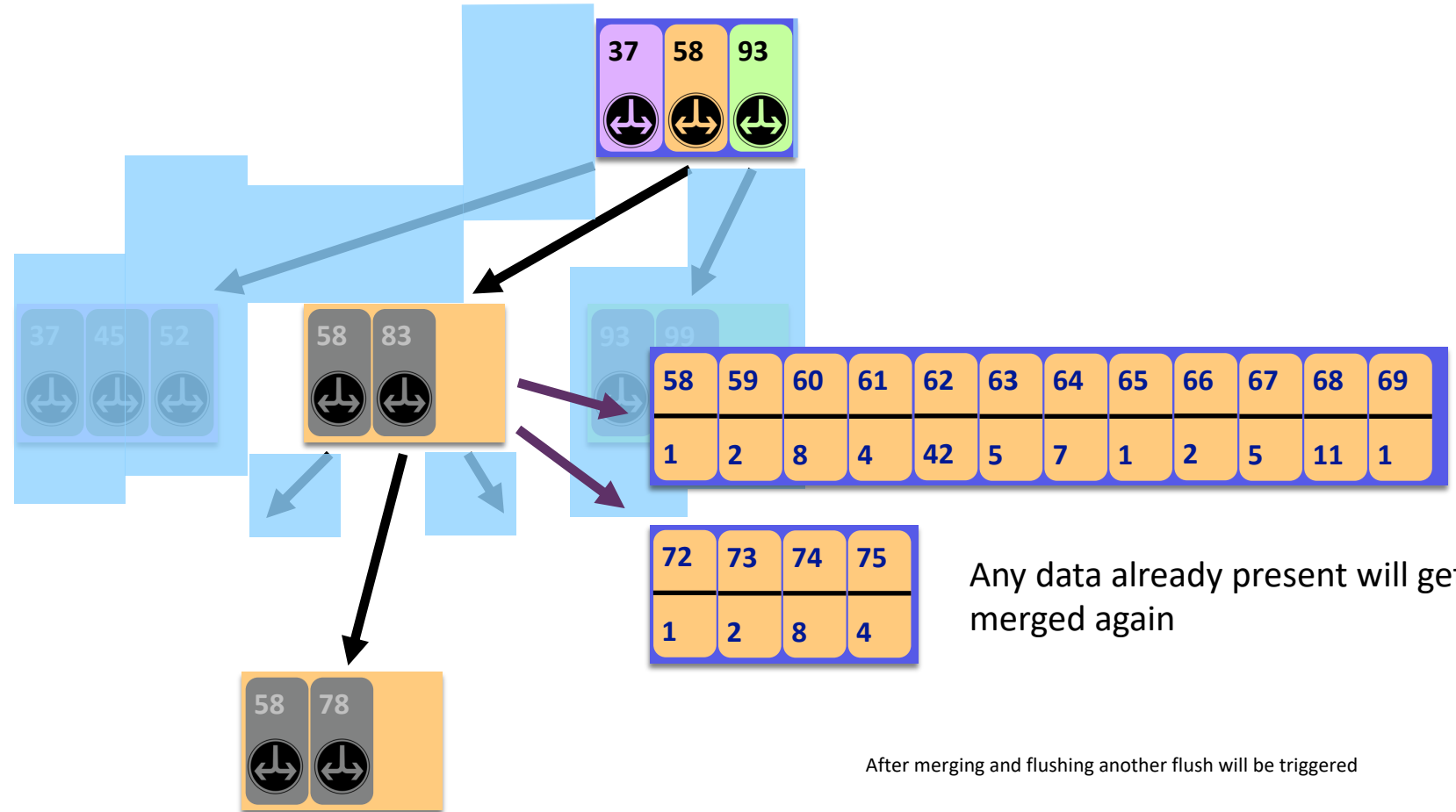
Flush-Then-Compact

Want:
Cheap sequential insertions



Flush-Then-Compact

Want:
Cheap sequential insertions



Can still end up merging on each level

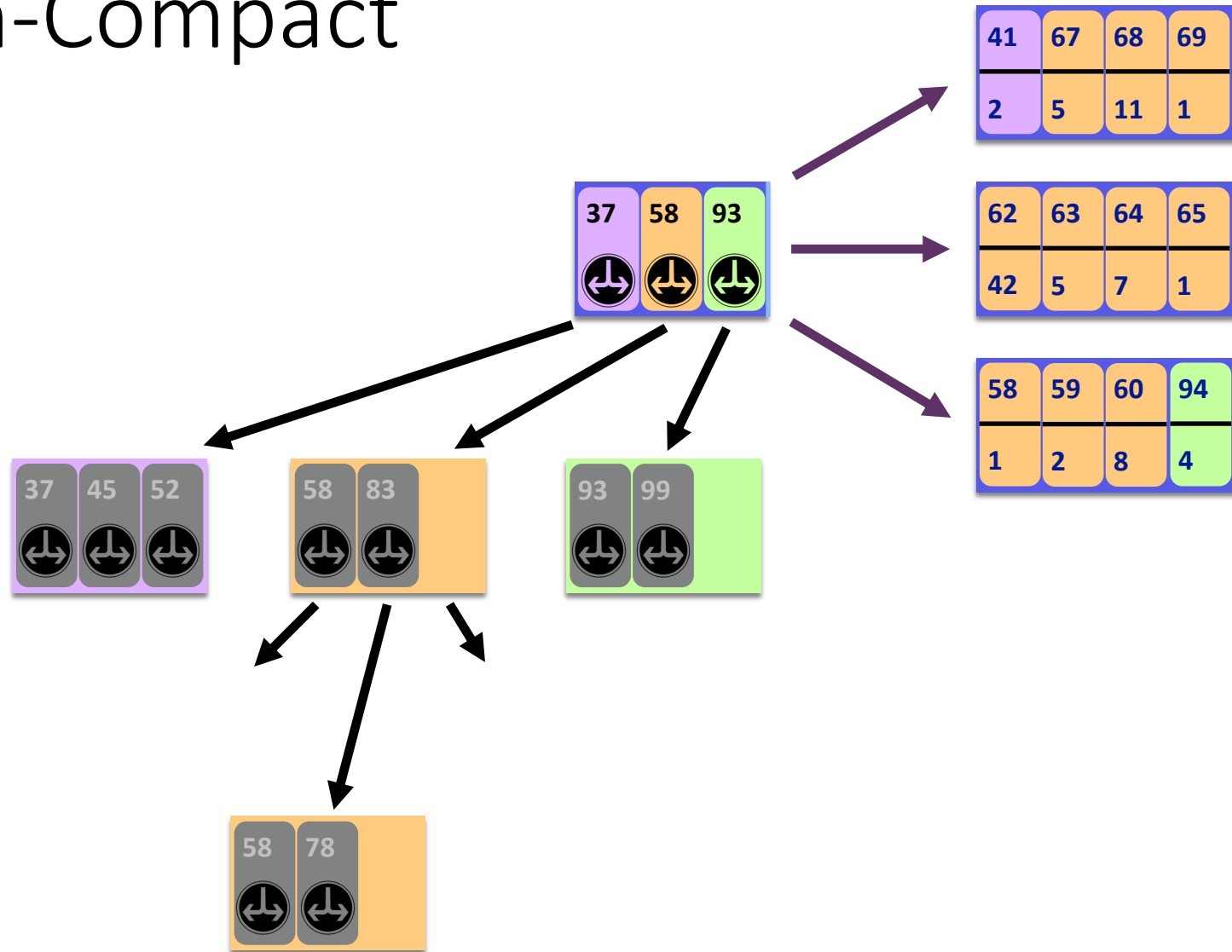
Any data already present will get merged again

After merging and flushing another flush will be triggered

Flush-Then-Compact

Want:
Cheap sequential insertions

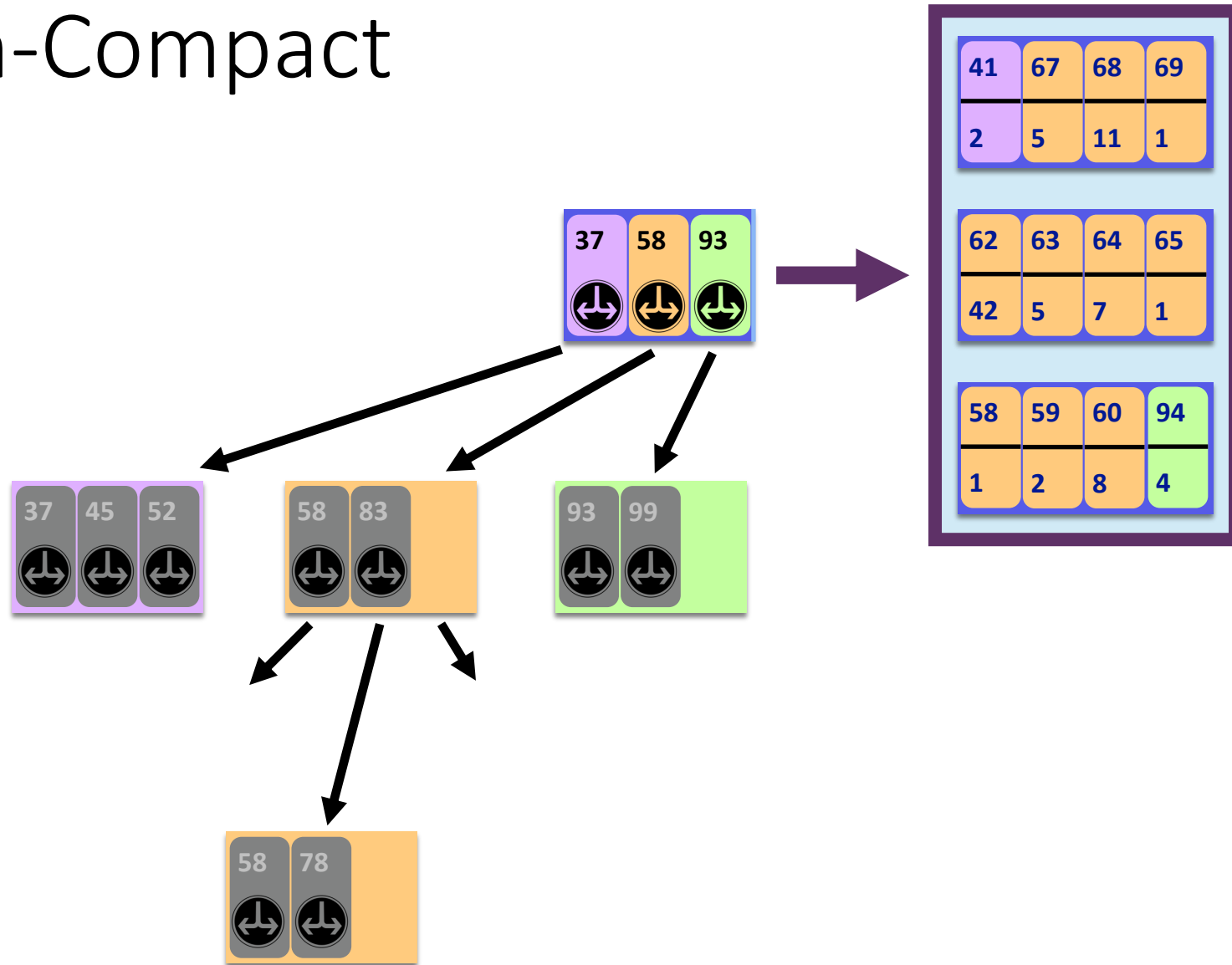
Idea: Flush-then-compact



Flush-Then-Compact

Want:
Cheap sequential insertions

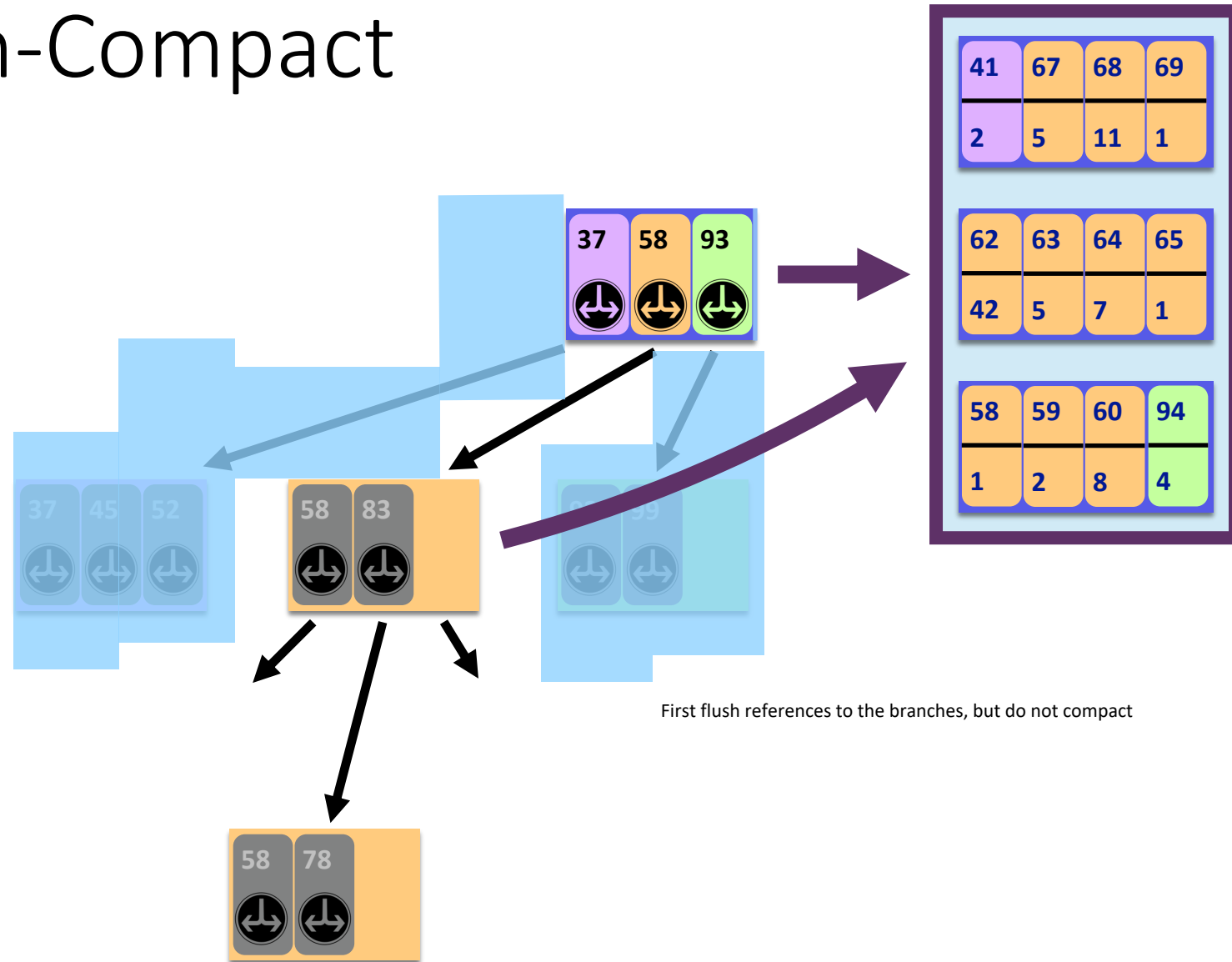
Idea: Flush-then-compact



Flush-Then-Compact

Want:
Cheap sequential insertions

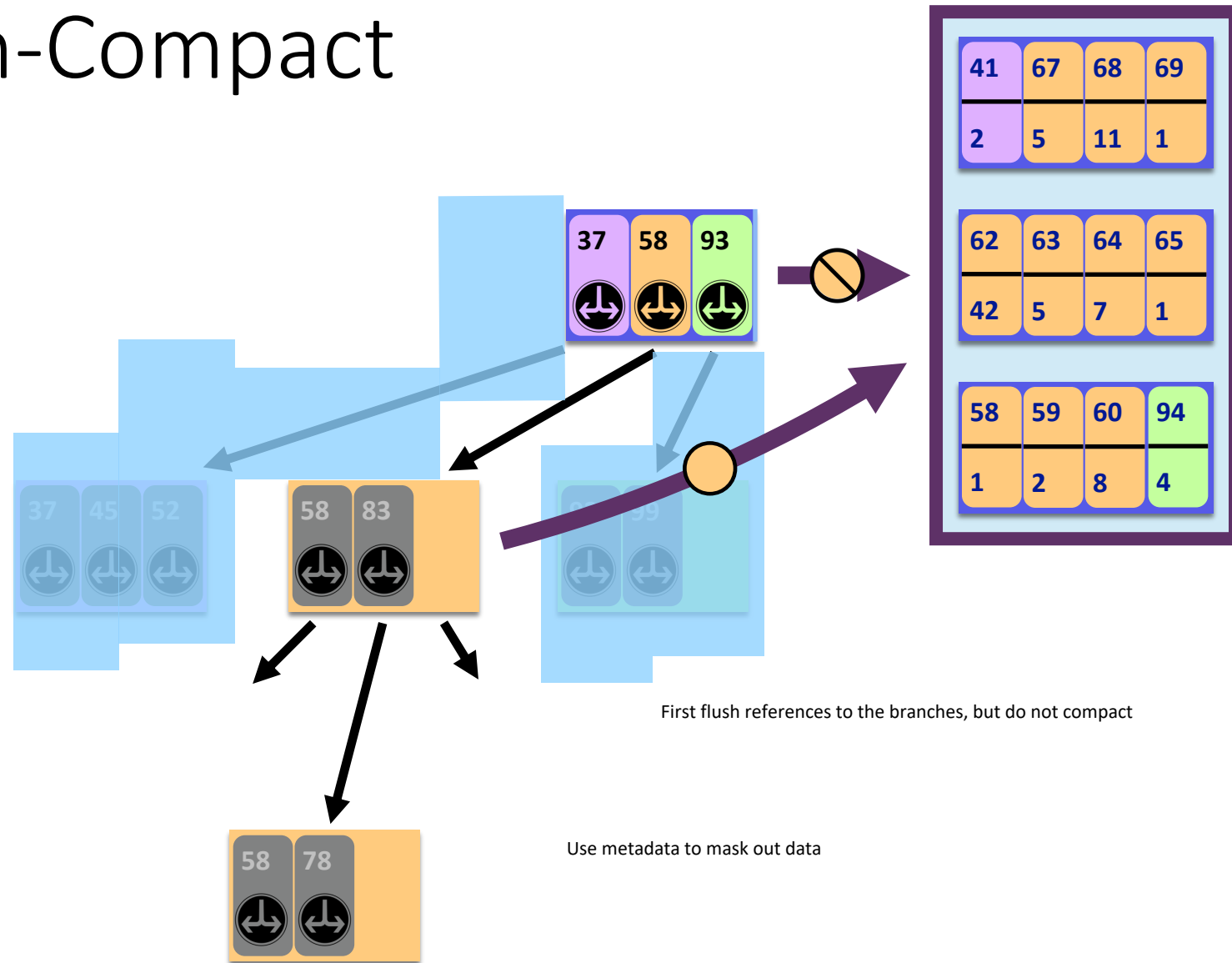
Idea: Flush-then-compact



Flush-Then-Compact

Want:
Cheap sequential insertions

Idea: Flush-then-compact

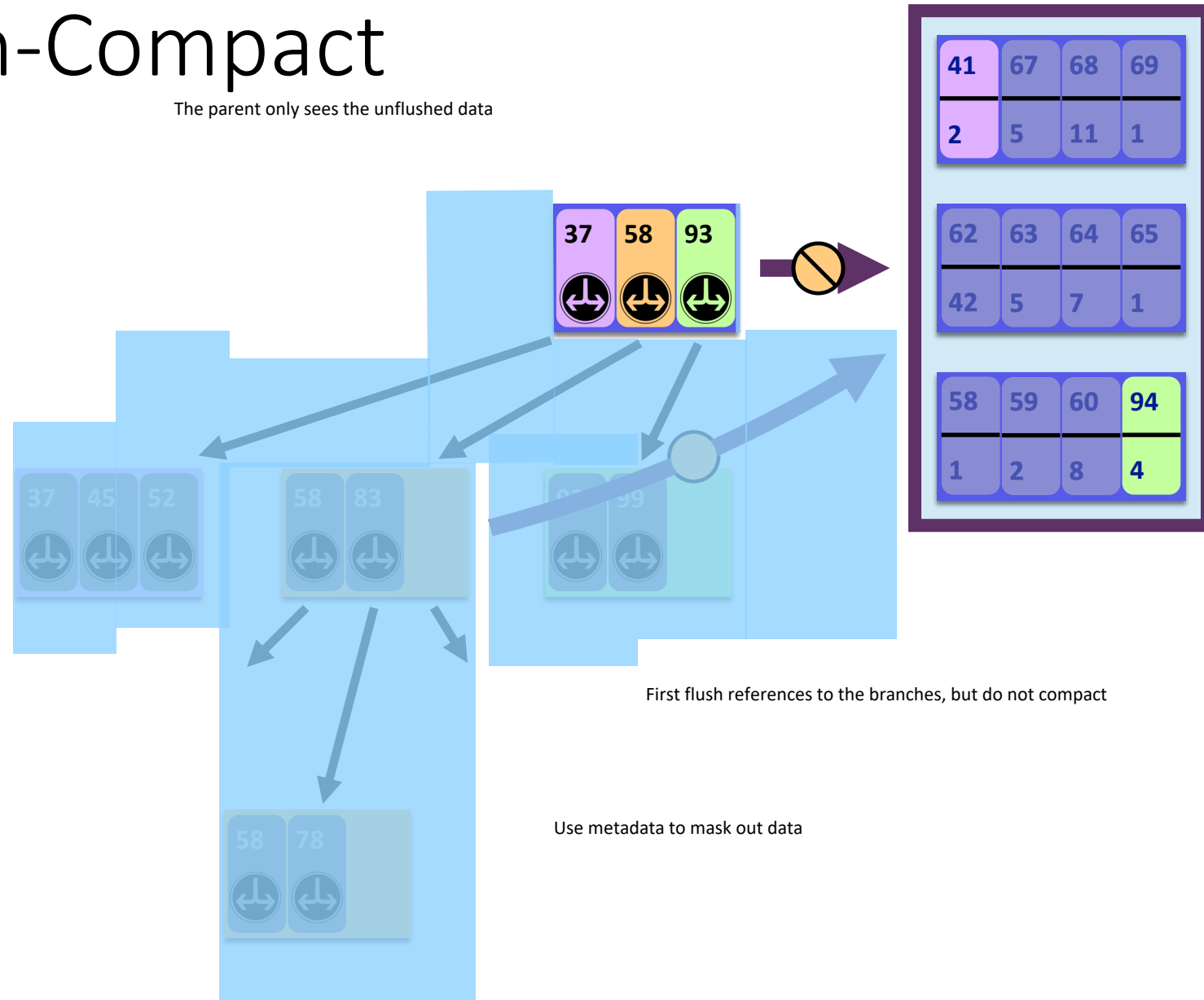


Flush-Then-Compact

The parent only sees the unflushed data

Want:
Cheap sequential insertions

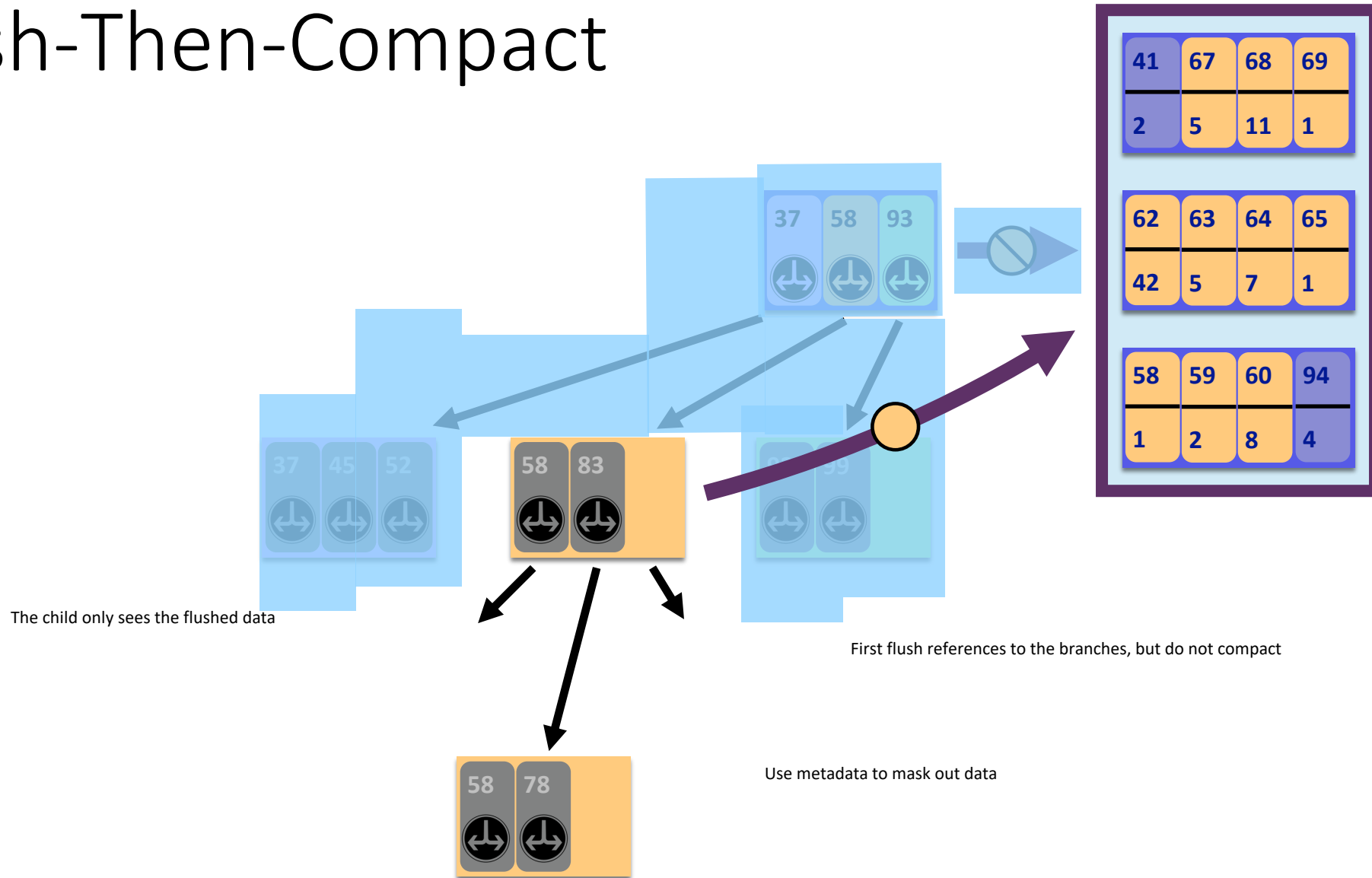
Idea: Flush-then-compact



Flush-Then-Compact

Want:
Cheap sequential insertions

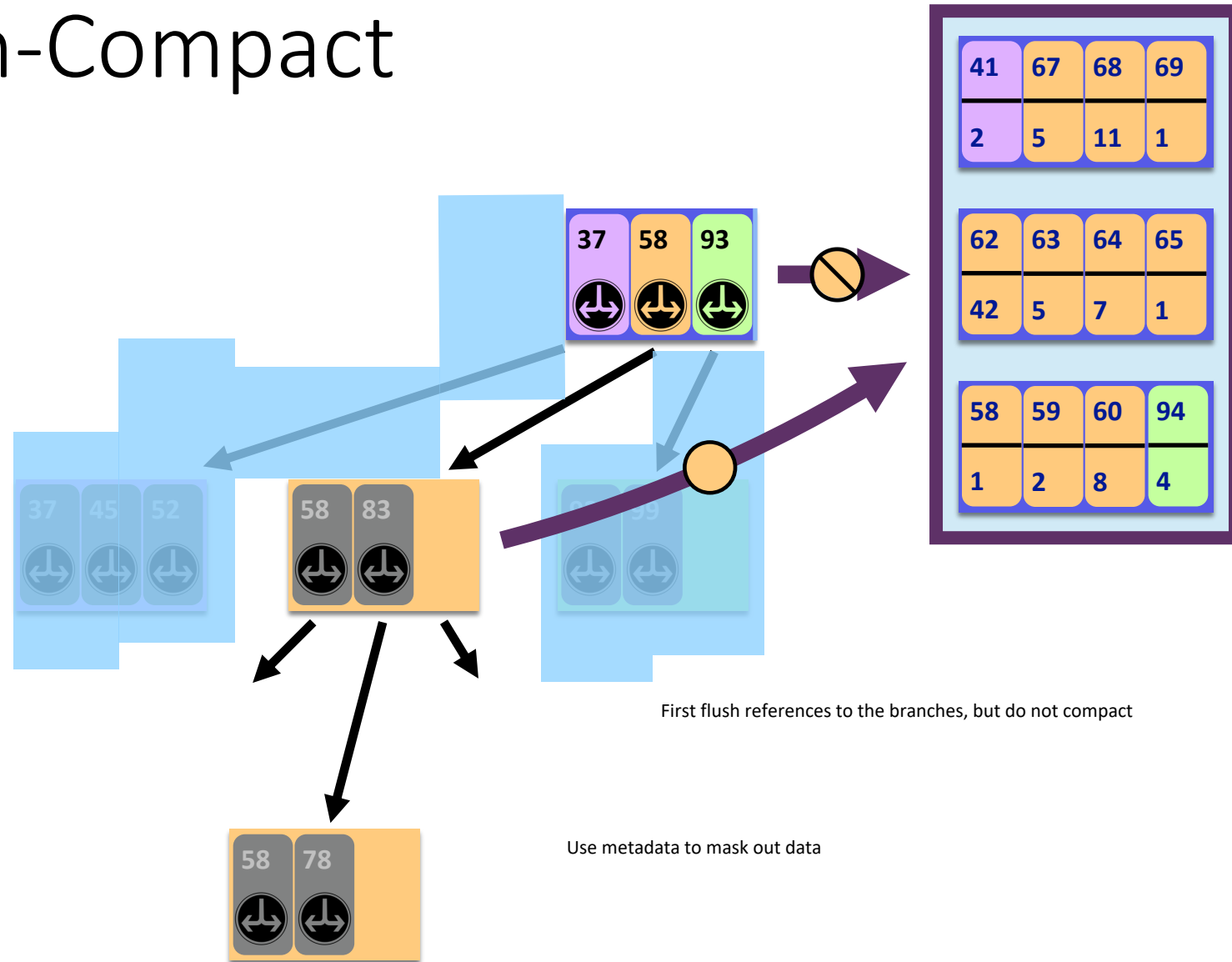
Idea: Flush-then-compact



Flush-Then-Compact

Want:
Cheap sequential insertions

Idea: Flush-then-compact



Then can flush again

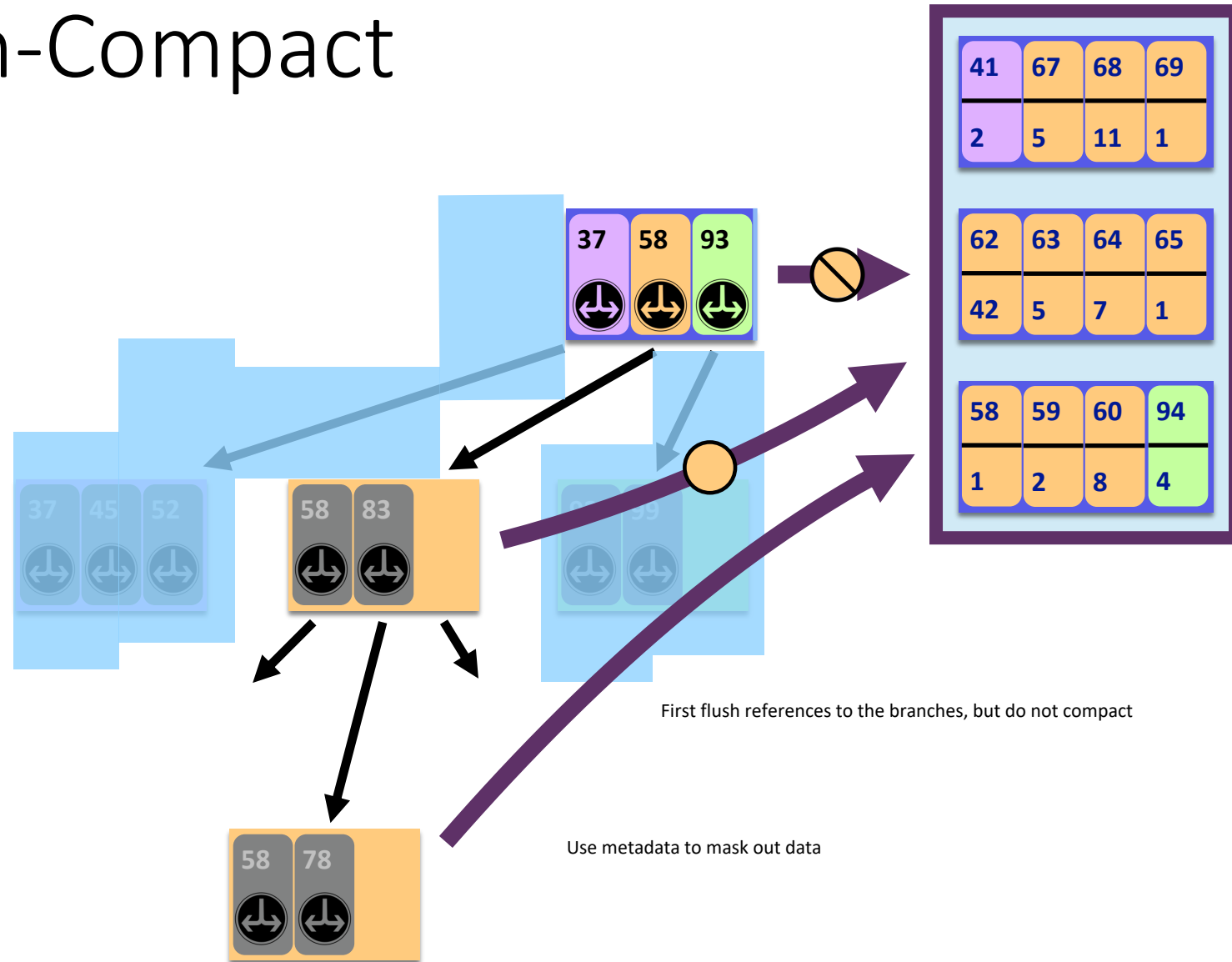
First flush references to the branches, but do not compact

Use metadata to mask out data

Flush-Then-Compact

Want:
Cheap sequential insertions

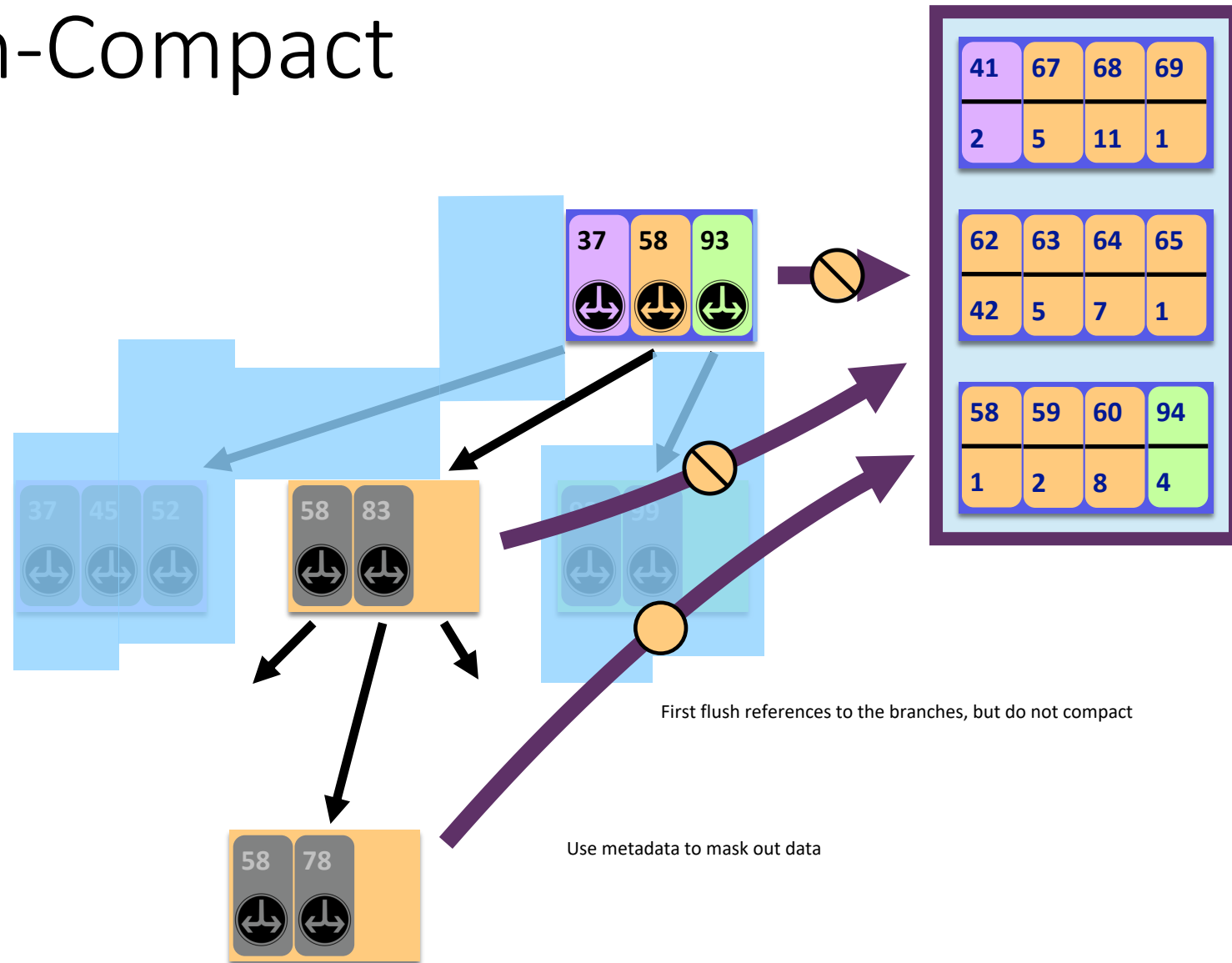
Idea: Flush-then-compact



Flush-Then-Compact

Want:
Cheap sequential insertions

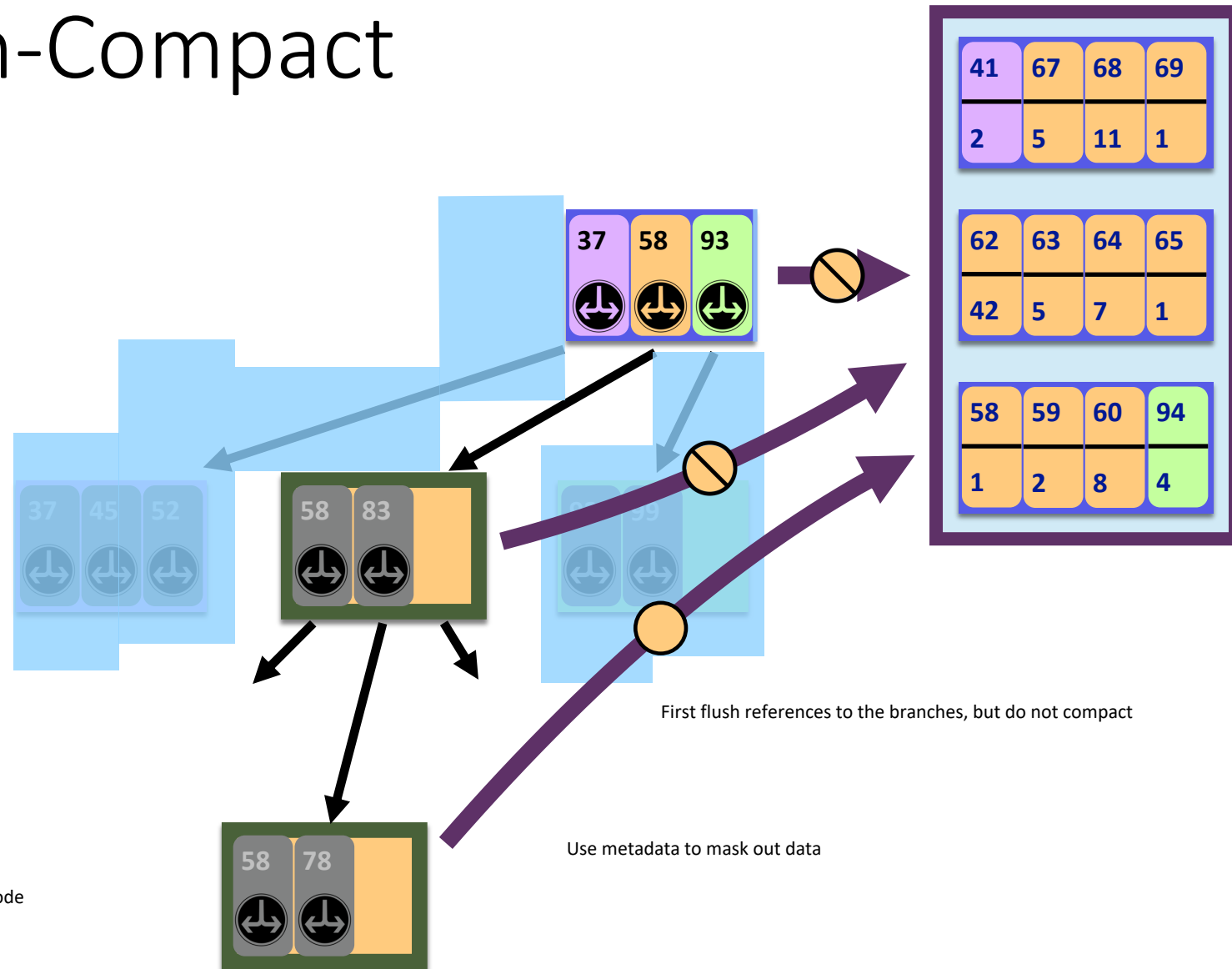
Idea: Flush-then-compact



Flush-Then-Compact

Want:
Cheap sequential insertions

Idea: Flush-then-compact



Then can flush again

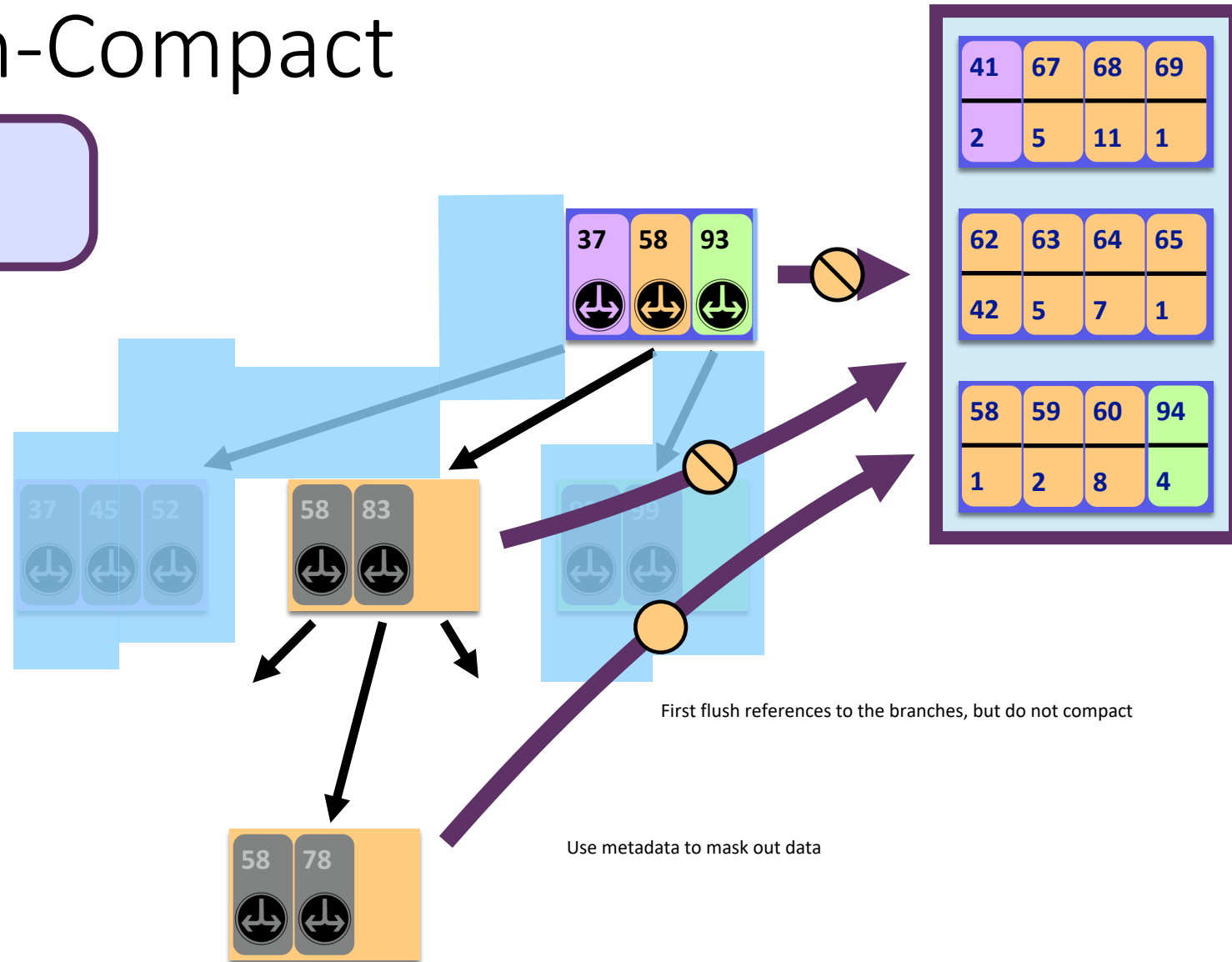
First flush references to the branches, but do not compact

Use metadata to mask out data

Finally, asynchronously compact the flushed buffers in each node

Flush-Then-Compact

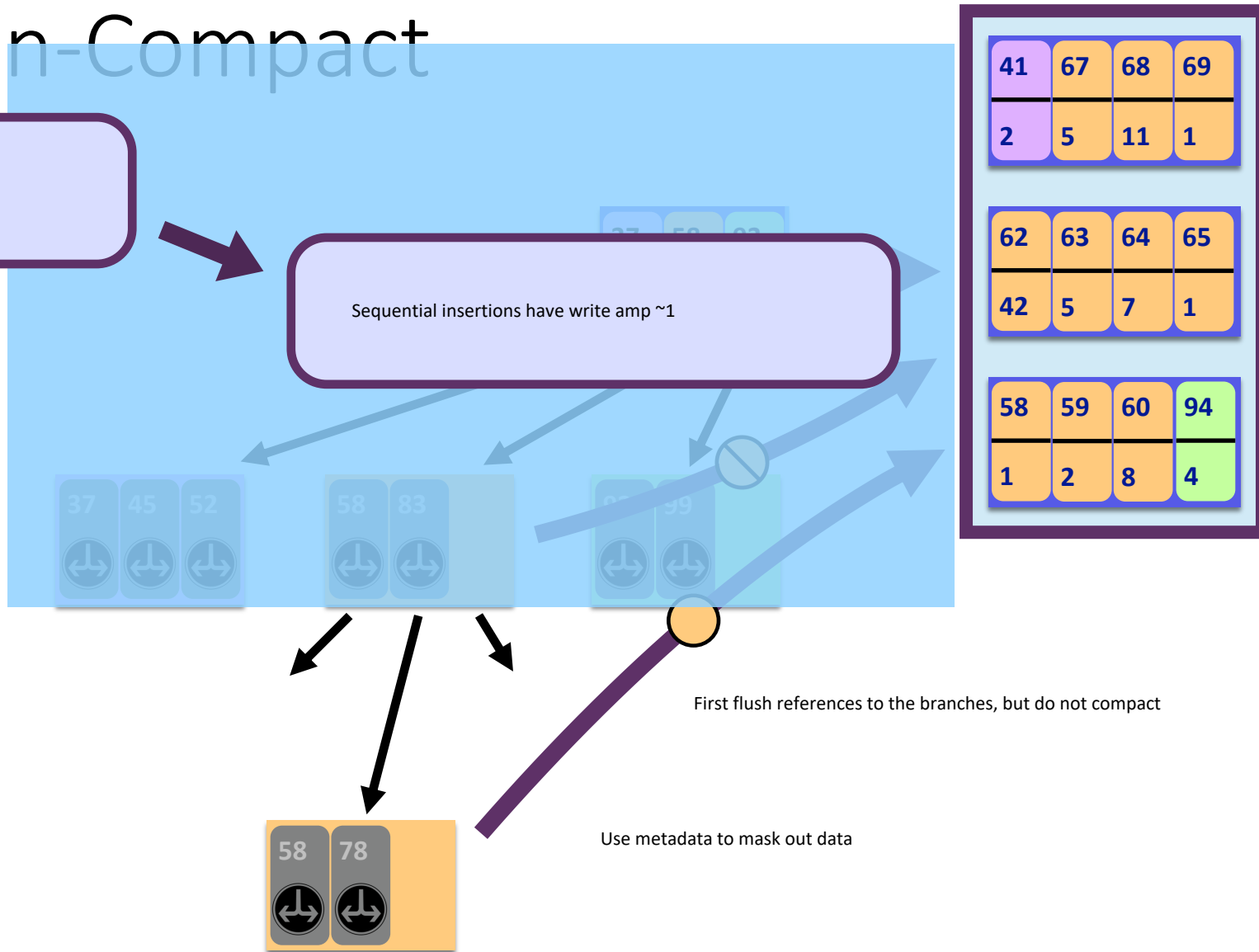
No work on immediately flushed data



Flush-Then-Compact

No work on immediately flushed data

Sequential insertions have write amp ~ 1



41	67	68	69
2	5	11	1
62	63	64	65
42	5	7	1
58	59	60	94
1	2	8	4

Flush-Then-Compact

No work on immediately flushed data

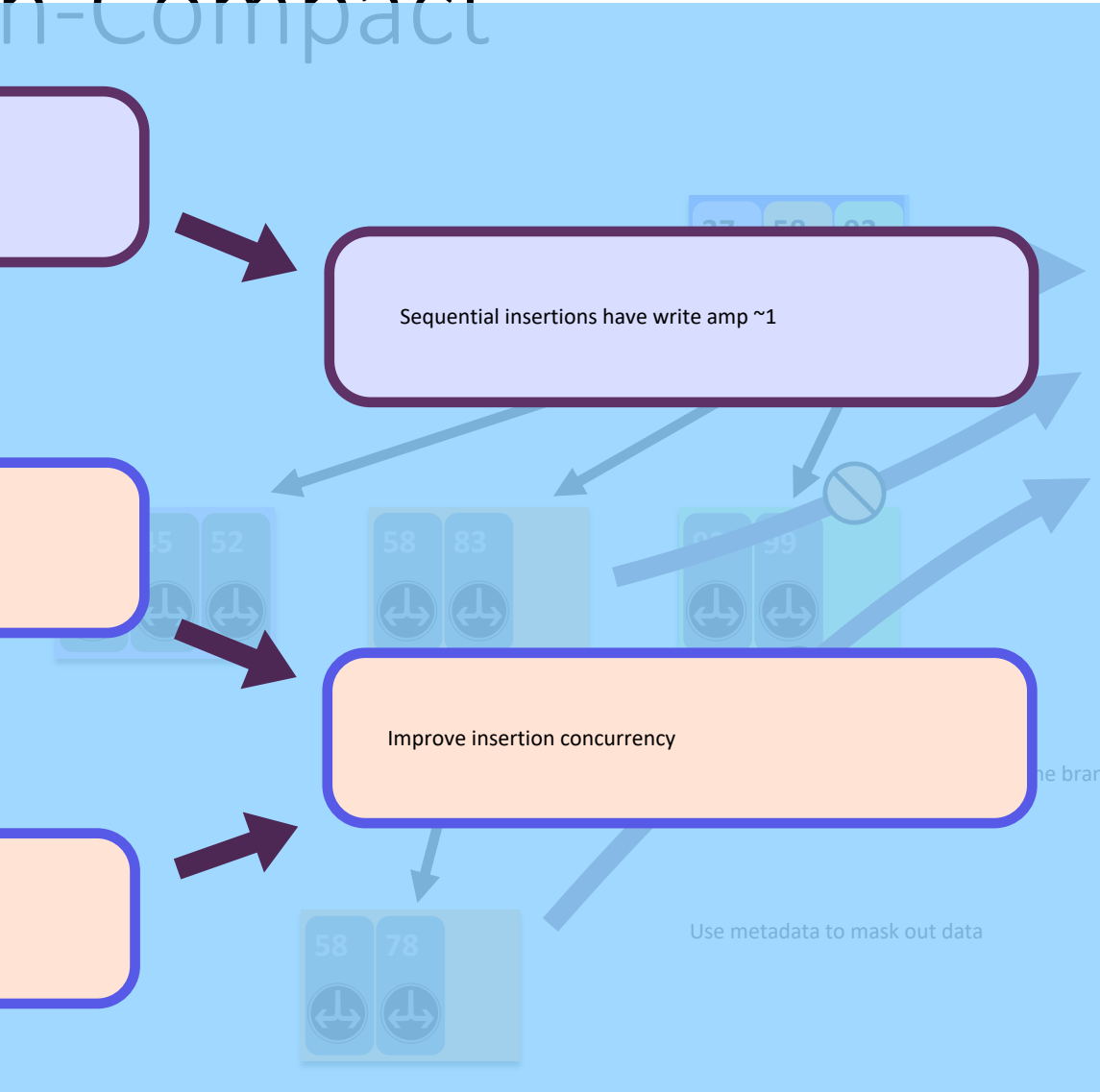
Sequential insertions have write amp ~ 1

Break a serial chain of compactions into parallel

Improve insertion concurrency

Concurrent compactions in trunk nodes

41	67	68	69
2	5	11	1
62	63	64	65
42	5	7	1
58	59	60	94
1	2	8	4

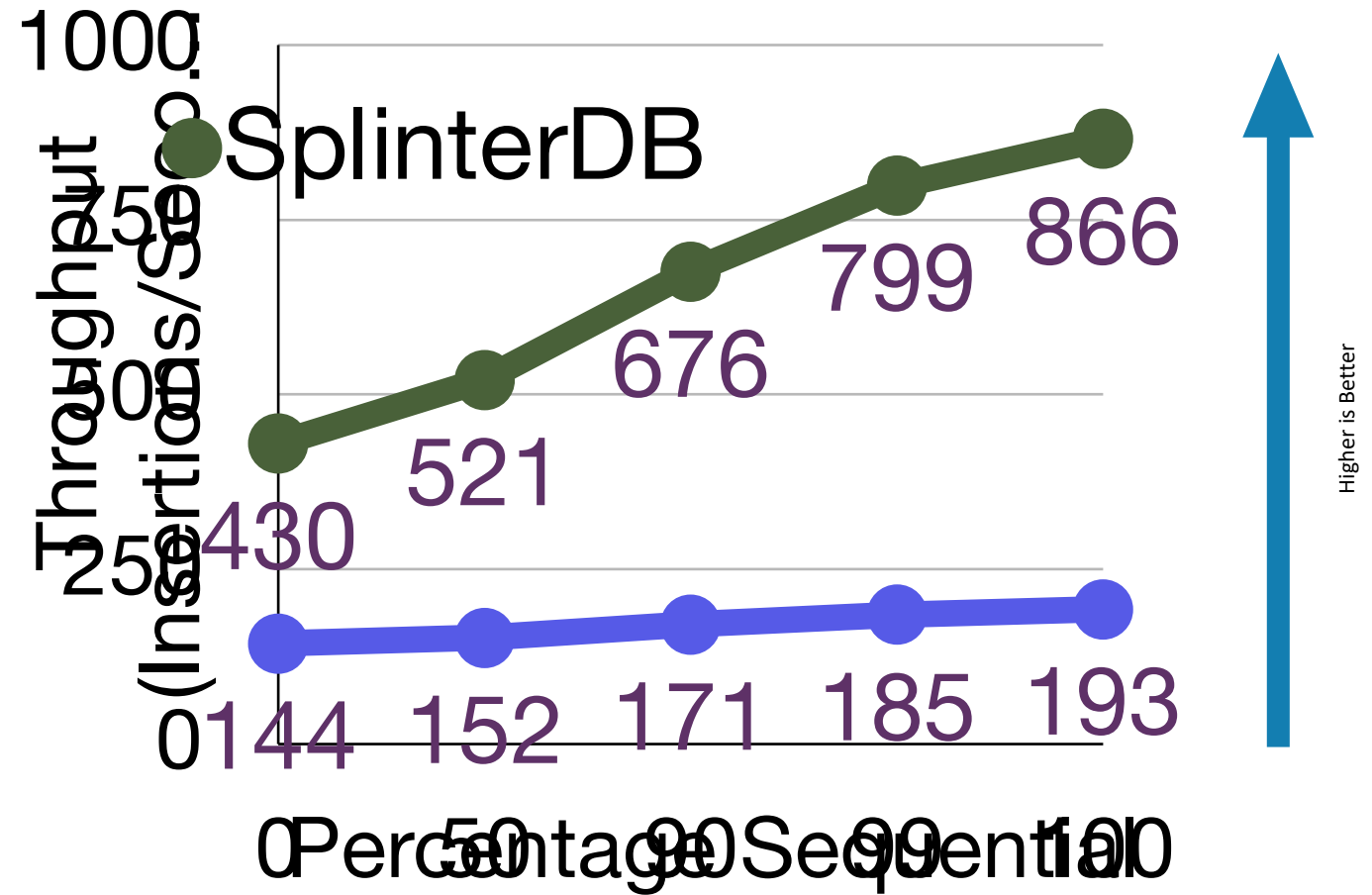


Use metadata to mask out data

Use metadata to mask out data

Flush-Then-Compact

Run a single-threaded workload with a percentage sequential insertions and the rest random

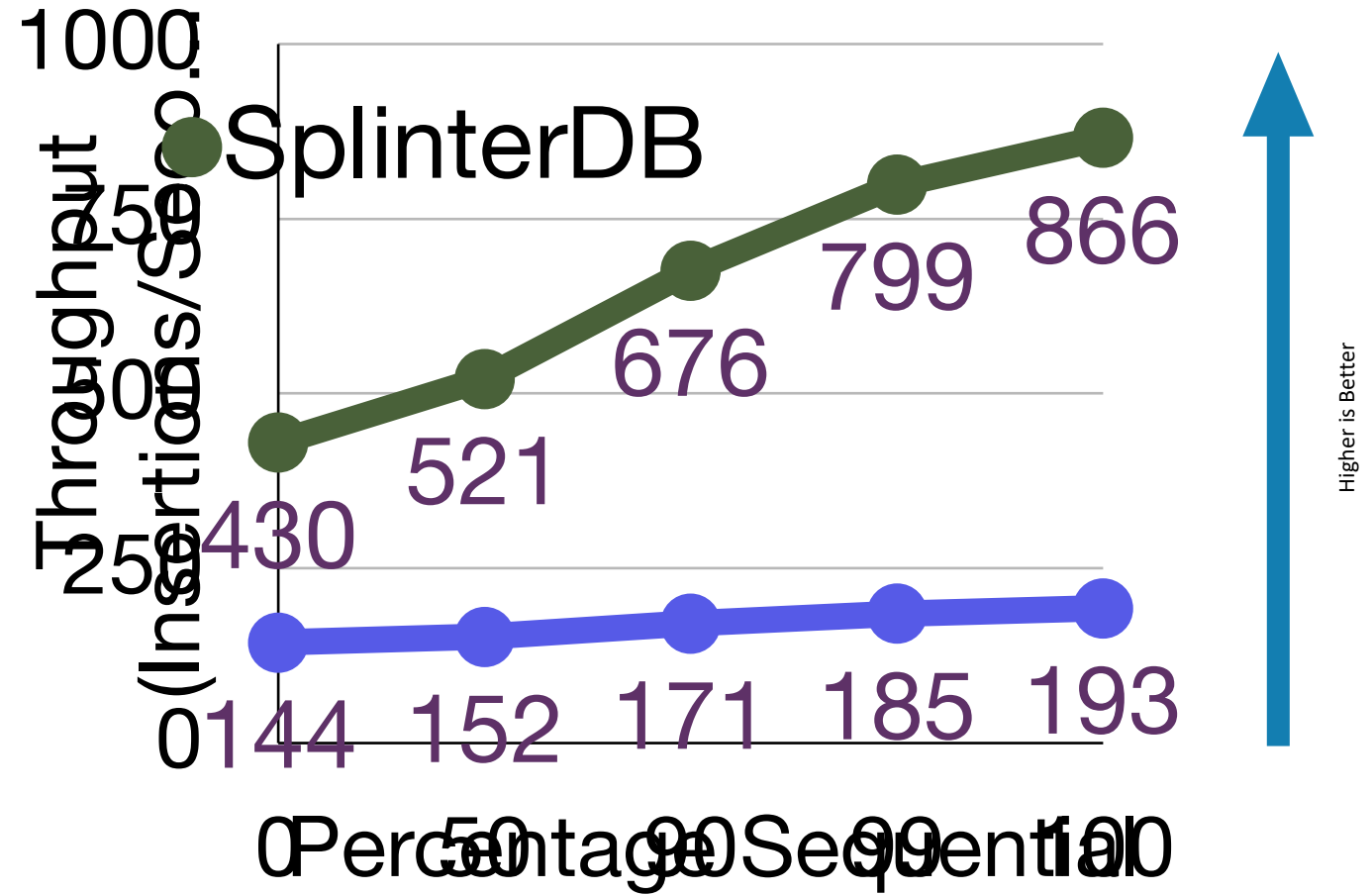


X-axis not to scale

Flush-Then-Compact

Run a single-threaded workload with a percentage sequential insertions and the rest random

Because of flush-then-compact, SplinterDB smoothly increases throughput as the workload gets more sequential



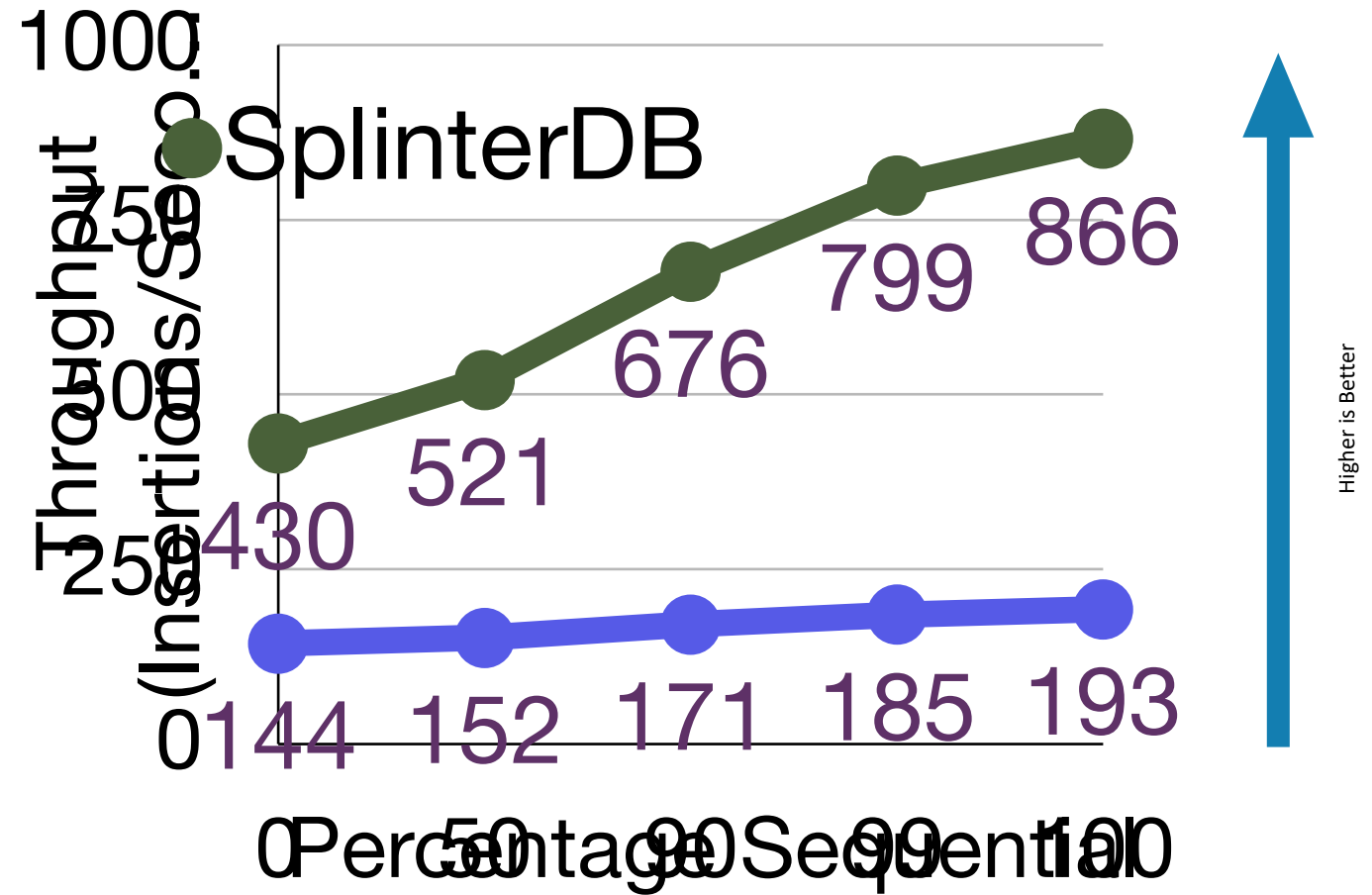
X-axis not to scale

Flush-Then-Compact

Run a single-threaded workload with a percentage sequential insertions and the rest random

Because of flush-then-compact, SplinterDB smoothly increases throughput as the workload gets more sequential

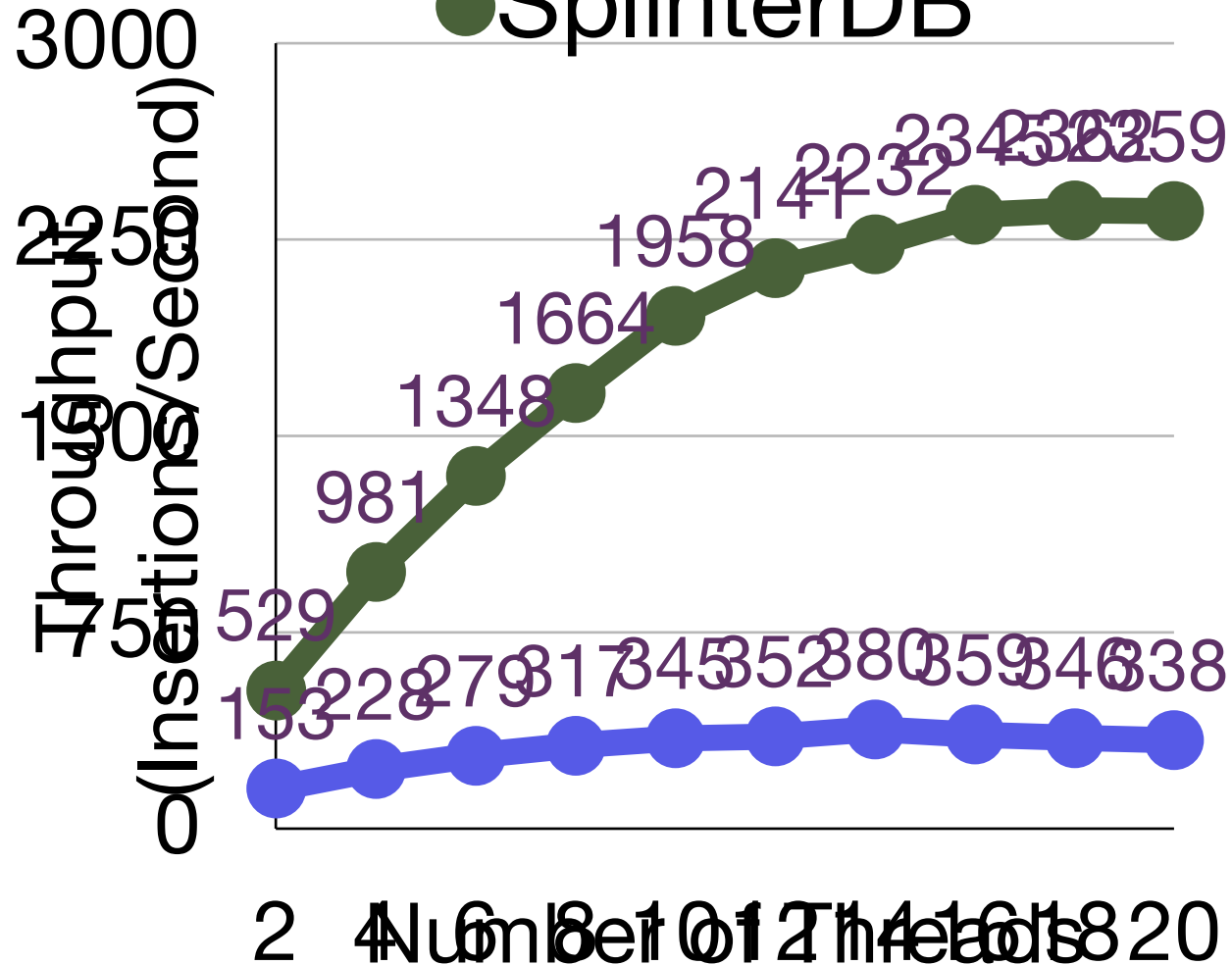
RocksDB improves, but at a much lower rate



X-axis not to scale

Flush-then-Compact

● SplinterDB

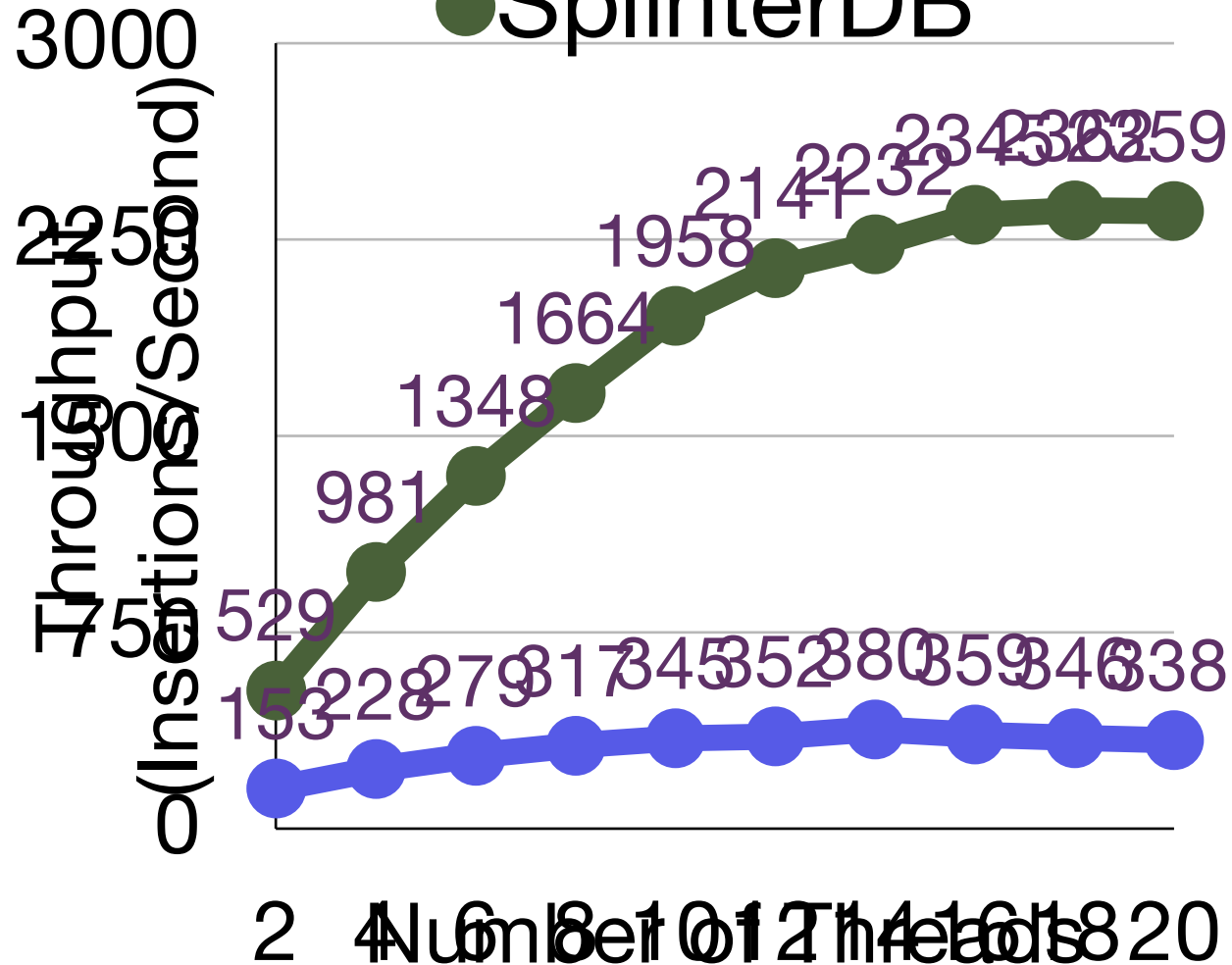


Insertions in SplinterDB scale well

Higher is Better

Flush-then-Compact

● SplinterDB



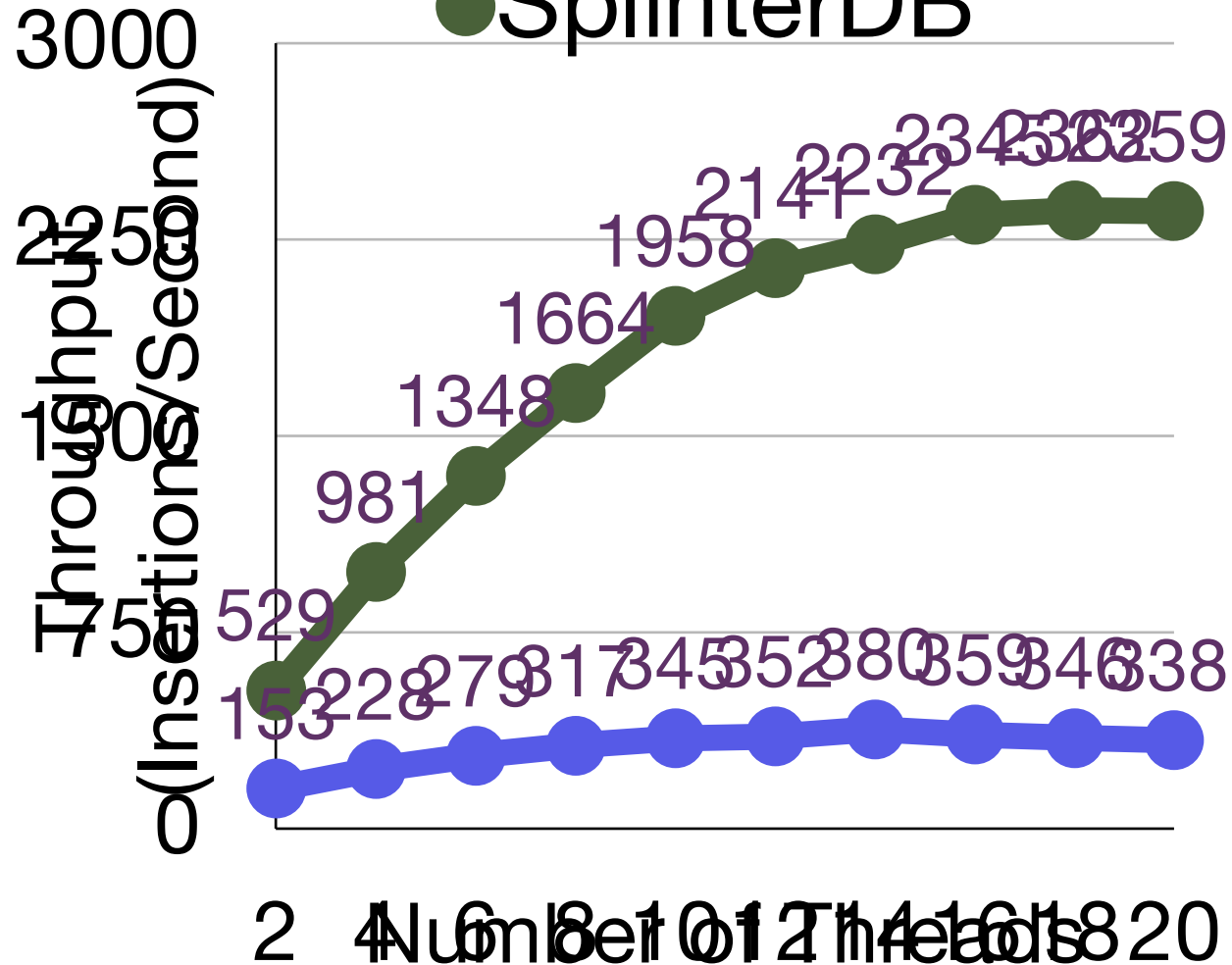
Insertions in SplinterDB scale well

At 12 threads, SplinterDB has 7x the throughput of 1 thread

Higher is Better

Flush-then-Compact

● SplinterDB



Insertions in SplinterDB scale well

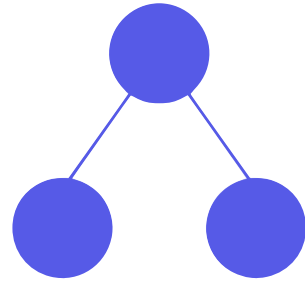
At 12 threads, SplinterDB has 7x the throughput of 1 thread

At 12+ threads, SplinterDB uses 85%+ of the device bandwidth

Higher is Better

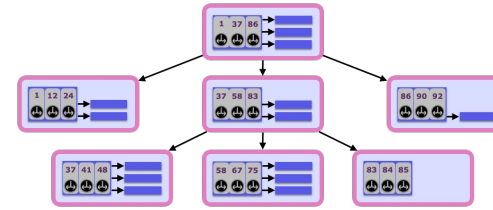
Conclusion

Model the problem:
external memory dictionary



Theory
Systems

Mapped B^ϵ -tree



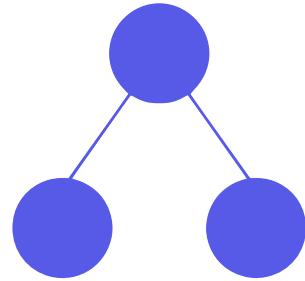
vSAN needed a new way of storing metadata



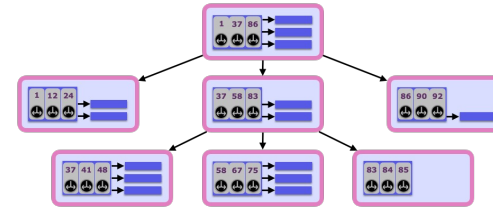
SplinterDB

Conclusion

Model the problem:
external memory dictionary



Mapped B^ϵ -tree



Theory
Systems



SplinterDB is in vSAN 8.0



vSAN needed a new way of storing metadata

Open-source at
<https://github.com/vmware/splinterdb>

SplinterDB

