CS4961 Parallel Programming

Lecture 2: Introduction to Parallel Algorithms

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Homework 1 - Due 9:10 AM, Thursday, Sept. 3

• To submit your homework:
  - Submit a PDF file
  - Use the "handin" program on the CADE machines
  - Use the following command:
    "handin cs4961 hw1 <prob1file>"

• Problem 1:
  - What are your goals after this year and how do you anticipate this class is going to help you with that? Some possible answers, but please feel free to add to them. Also, please write at least one sentence of explanation.
    - A job in the computing industry
    - A job in some other industry where computing is applied to real-world problems
    - As preparation for graduate studies
    - Intellectual curiosity about what is happening in the computing field
    - Other

Homework 1

• Problem 2:
  - Provide pseudocode (as in the book and class notes) for a correct and efficient parallel implementation in C of the parallel sums code, based on the tree-based concept in slides 26 and 27 of Lecture 2. Assume that you have an array of 128 elements and you are using 8 processors.
  - Hints:
    - Use an iterative algorithm similar to count3s, but use the tree structure to accumulate the final result.
    - Use the book to show you how to add threads to what we derived for count3s.

• Problem 3:
  - Now show how the same algorithm can be modified to find the maximum element of an array. (problem 2 in text). Is this also a reduction computation? If so, why?

Administrative

• Homework 1 posted, due September 3 before class
• Use the "handin" program on the CADE machines
• Use the following command:
  "handin cs4961 hw1 <prob1file>"
• Waiving CS4400 prerequisite, replacing with CS3810
Today's Lecture

• Parallelism in Everyday Life
• Learning to Think in Parallel
• Aspects of parallel algorithms (and a hint at complexity!)
• Derive parallel algorithms
• Discussion

Sources for this lecture:

Is it really harder to “think” in parallel?

• Some would argue it is more natural to think in parallel...
• ... and many examples exist in daily life

Examples?

- House construction -- parallel tasks, wiring and plumbing performed at once (independence), but framing must precede wiring (dependence)
- Similarly, developing large software systems
- Assembly line manufacture - pipelining, many instances in process at once
- Call center - independent calls executed simultaneously (data parallel)
- “Multi-tasking” - all sorts of variations

Reasoning about a Parallel Algorithm

• Ignore architectural details for now
• Assume we are starting with a sequential algorithm and trying to modify it to execute in parallel
• Not always the best strategy, as sometimes the best parallel algorithms are NOTHING like their sequential counterparts
• But useful since you are accustomed to sequential algorithms
Reasoning about a parallel algorithm, cont.

- Computation Decomposition
  - How to divide the sequential computation among parallel threads/processors/computations?
- Aside: Also, Data Partitioning (ignore today)
- Preserving Dependencies
  - Keeping the data values consistent with respect to the sequential execution.
- Overhead
  - We’ll talk about some different kinds of overhead

Key Control Concept: Data Dependence

- Question: When is parallelization guaranteed to be safe?
- Answer: If there are no data dependences across reordered computations.
- Definition: Two memory accesses are involved in a data dependence if they may refer to the same memory location and one of the accesses is a write.
- Bernstein’s conditions (1966): \( I_j \) is the set of memory locations read by process \( P_j \), and \( O_j \) the set updated by process \( P_j \). To execute \( P_j \) and another process \( P_k \) in parallel,
  \[
  I_j \cap O_k = \phi \quad \text{write after read}
  
  I_k \cap O_j = \phi \quad \text{read after write}
  
  O_j \cap O_k = \phi \quad \text{write after write}
  \]

Data Dependence and Related Definitions

- Actually, parallelizing compilers must formalize this to guarantee correct code.
- Let’s look at how they do it. It will help us understand how to reason about correctness as programmers.
- Definition: Two memory accesses are involved in a data dependence if they may refer to the same memory location and one of the references is a write.

Some Definitions (from Allen & Kennedy)

- Definition 2.5:
  - Two computations are equivalent if, on the same inputs,
    - they produce identical outputs
    - the outputs are executed in the same order
- Definition 2.6:
  - A reordering transformation
    - changes the order of statement execution
    - without adding or deleting any statement executions.
- Definition 2.7:
  - A reordering transformation preserves a dependence if
    - it preserves the relative execution order of the dependences’ source and sink.
Fundamental Theorem of Dependence

- **Theorem 2.2:**
  - Any reordering transformation that preserves every dependence in a program preserves the meaning of that program.

Simple Example 1: "Hello World" of Parallel Programming

- Count the 3s in `array[]` of `length` values
- Definitional solution ... Sequential program

```
count = 0;
for (i=0; i<length; i++) {
    if (array[i] == 3)
        count += 1;
}
```

Can we rewrite this to a parallel code?

Computation Partitioning

- Block decomposition: Partition original loop into separate "blocks" of loop iterations.
  - Each "block" is assigned to an independent "thread" in t0, t1, t2, t3 for t=4 threads
  - Length = 16 in this example

```
int block_length_per_thread = length/t;
int start = id * block_length_per_thread;
for (i=start; i<start+block_length_per_thread; i++) {
    if (array[i] == 3)
        count += 1;
}
```

Correct? Preserve Dependences?

Data Race on Count Variable

- Two threads may interfere on memory writes

```
Thread 1
load count
count = 0
increment count
store count
```
```
Thread 2
load count
count = 1
increment count
store count
```
```
Thread 3
load count
count = 1
increment count
store count
```
```
Thread 1
load count
count = 1
increment count
store count
```
```
Thread 2
load count
count = 2
increment count
store count
```
```
Thread 3
load count
count = 2
increment count
store count
```
```
Thread 1
load count
count = 0
increment count
store count
```
```
Thread 2
load count
count = 1
increment count
store count
```
```
Thread 3
load count
count = 2
increment count
store count
```
What Happened?

- Dependence on count across iterations/threads
  - But reordering ok since operations on count are associative
- Load/increment/store must be done \textit{atomically} to preserve sequential meaning
- Definitions:
  - Atomicity: a set of operations is atomic if either they all execute or none executes. Thus, there is no way to see the results of a partial execution.
  - Mutual exclusion: at most one thread can execute the code at any time

Try 2: Adding Locks

- Insert mutual exclusion (mutex) so that only one thread at a time is loading/incrementing/storing count atomically

```c
int block_length_per_thread = length/t;
mutex m;
int start = id * block_length_per_thread;
for (i=start; i<start+block_length_per_thread; i++) {
    if (array[i] == 3) {
        mutex_lock(m);
        count += 1;
        mutex_unlock(m);
    }
}
```

Correct now. Done?

Performance Problems

- Serialization at the mutex
- Insufficient parallelism granularity
- Impact of memory system

Lock Contention and Poor Granularity

- To acquire lock, must go through at least a few levels of cache (locality)
  - Local copy in register not going to be correct
- Not a lot of parallel work outside of acquiring/releasing lock
Try 3: Increase “Granularity”

• Each thread operates on a private copy of count
• Lock only to update global data from private copy

mutex m;
int block_length_per_thread = length/t;
int start = id * block_length_per_thread;
for (i=start; i<start+block_length_per_thread; i++) {
    if (array[i] == 3) {
        private_count[id] += 1;
    }
    mutex_lock(m);
    count += private_count[id];
    mutex_unlock(m);
}

Try 4: Force Private Variables into Different Cache Lines

• Simple way to do this?
• See textbook for authors' solution

Parallel speedup when <t = 2>:
time(1)/time(2) = 0.91/0.51
    = 1.78 (close to number of processors!)

Much Better, But Not Better than Sequential

• Subtle cache effects are limiting performance

Discussion: Overheads

• What were the overheads we saw with this example?
  - Extra code to determine portion of computation
  - Locking overhead: inherent cost plus contention
  - Cache effects: false sharing
Interestingly, this code represents a common pattern in parallel algorithms.

A reduction computation
- From a large amount of input data, compute a smaller result that represents a reduction in the dimensionality of the input.
- In this case, a reduction from an array input to a scalar result (the count).

Reduction computations exhibit dependences that must be preserved.
- Looks like \( \text{result} = \text{result} \circ \ldots \)
- Operation \( \circ \) must be associative so that it is safe to reorder them.

Aside: Floating point arithmetic is not truly associative, but usually ok to reorder.

Parallel Summation:
- Adding a sequence of numbers \( A[0], \ldots, A[n-1] \)

Standard way to express it
\[
\text{sum} = 0;
\text{for (i=0; i<n; i++) { sum += A[i]; } }
\]
Semantics require:
\[(\ldots((\text{sum}+A[0])+A[1])+\ldots)+A[n-1]\]
That is, sequential.
Can it be executed in parallel?

Generalizing from this example

Simple Example 2:
Another "Hello World" Equivalent

Computation Decomposition: Pairwise Additions
- add pairs of values producing 1st level results,
- add pairs of 1st level results producing 2nd level results,
- sum pairs of 2nd level results ...

Graphical Depiction of Sum Code

Which decomposition is better suited for parallel execution.
Summary of Lecture

• How to Derive Parallel Versions of Sequential Algorithms
  - Computation Partitioning
  - Preserving Dependences and Reordering
  - Transformations
  - Reduction Computations
  - Overheads

Next Time

• A Discussion of parallel computing platforms
• Questions about first written homework assignment