Symbols

Filtering Symbols

Our favorite **list-of-sym** program:

```
; eat-apples : list-of-sym -> list-of-sym
(define (eat-apples 1)
  (cond
   [(empty? 1) empty]
   [(cons? 1)
    (local [(define ate-rest (eat-apples (rest 1)))]
       (cond
        [(symbol=? (first 1) 'apple) ate-rest]
        [else (cons (first 1) ate-rest)]))]))
```

- How about **eat-bananas**?
- How about **eat-non-apples**?

We know where this leads...

; filter-syms : (sym -> bool) list-of-sym ; -> list-of-sym (define (filter-syms PRED 1) (cond [(empty? 1) empty] [(cons? 1) (local [(define r (filter-syms PRED (rest 1)))] (cond [(PRED (first 1)) (cons (first 1) r)] [else r]))]))

This looks really familiar

Last Time: Filtering Numbers

; filter-nums : (num -> bool) list-of-num ; -> list-of-num (define (filter-nums PRED 1) (cond [(empty? 1) empty] [(cons? 1) (local [(define r (filter-nums PRED (rest 1)))] (cond [(PRED (first 1)) (cons (first 1) r)] [else r]))]))

```
How do we avoid cut and paste?
```

Filtering Lists

We know this function will work for both number and symbol lists:

```
; filter : ...
(define (filter PRED 1)
  (cond
    [(empty? 1) empty]
    [(cons? 1)
        (local [(define r
                  (filter PRED (rest 1)))]
        (cond
        [(PRED (first 1))
            (cons (first 1) r)]
        [else r]))]))
```

But what is its contract?

The Contract of Filter

The Contract of Filter

How about this?

(num-OR-sym -> bool) list-of-num-OR-list-of-sym
-> list-of-num-OR-list-of-sym

; A num-OR-sym is either

; – num

; - sym

; A list-of-num-OR-list-of-sym is either

- ; list-of-num
- ; list-of-sym

How about this?

(num-OR-sym -> bool) list-of-num-OR-list-of-sym
-> list-of-num-OR-list-of-sym

This contract is too weak to define **eat-apples**

```
; eat-apples : list-of-sym -> list-of-sym
(define (eat-apples 1)
  (filter not-apple? 1))
```

; not-apple? : sym -> bool
(define (not-apple? s)
 (not (symbol=? s 'apple)))

eat-apples must return a list-of-sym, but by its contract, filter
might return a list-of-num

The Contract of Filter

How about this?

```
(num-OR-sym -> bool) list-of-num-OR-list-of-sym
-> list-of-num-OR-list-of-sym
```

This contract is too weak to define **eat-apples**

```
; eat-apples : list-of-sym -> list-of-sym
(define (eat-apples 1)
  (filter not-apple? 1))
```

```
; not-apple? : sym -> bool
(define (not-apple? s)
  (not (symbol=? s 'apple)))
```

not-apple? only works on symbols, but by its contract filter might
give it a num

The Contract of Filter

The reason filter works is that if we give it a list-of-sym, then it returns a list-of-sym

Also, if we give filter a list-of-sym, then it calls PRED with symbols only

A better contract:

```
filter :
 ((num -> bool) list-of-num
 -> list-of-num)
OR
 ((sym -> bool) list-of-sym
 -> list-of-sym)
```

But what about a list of images, posns, or snakes?

The True Contract of Filter

The real contract is

```
filter : ((X -> bool) list-of-X -> list-of-X)
```

where x stands for any type

- The caller of filter gets to pick a type for x
- All xs in the contract must be replaced with the same type

Data definitions need type variables, too:

- ; A list-of-X is either
- ; empty
- ; (cons X empty)

Using Filter

The filter function is so useful that is't built in

New solution for HW 4 that works in Intermediate:

(define (eat-apples 1)
 (local [(define (not-apple? s)
 (not (symbol=? s 'apple)))]
 (filter not-apple? 1)))

Looking for Other Built-In Functions

```
Recall inflate-by-4%:
```

Is there a built-in function to help?

Yes: map

Using Map

```
(define (map CONV 1)
 (cond
  [(empty? 1) empty]
  [else (cons (CONV (first 1))
                                (map CONV (rest 1)))]))
```

```
(define (inflate-by-4% l)
  (local [(define (inflate-one n)
                     (* n 1.04))]
  (map inflate-one l)))
```

```
; negate-colors : list-of-col -> list-of-col
(define (negate-colors 1)
  (map negate-color 1))
```

The Contract for Map

```
Another function from HW 4:
         (define (map CONV 1)
            (cond
                                                                             ; distances : list-of-posn -> list-of-num
              [(empty? 1) empty]
              [else (cons (CONV (first 1))
                                                                                (cond
                             (map CONV (rest 1)))]))
• The 1 argument must be a list of x
• The CONV argument must accept each x
• If CONV returns a new x each time, then the contract for map is
                                                                        distances-to-0 is
          map : (X -> X) list-of-X -> list-of-X
                                                                        not
                   The True Contract of Map
Despite the contract mismatch, this works!
                  (define (distances 1)
                     (map distance-to-0 1))
The true contract of map is
          map : (X \rightarrow Y) list-of-X -> list-of-Y
                                                                        . . .
The caller gets to pick both \mathbf{x} and \mathbf{y} independently
                                                                          (map rob-car 1))
                                                                        . . .
```

Posns and Distances

```
(define (distances 1)
        [(empty? 1) empty]
        [(cons? 1) (cons (distance-to-0 (first 1))
                          (distances (rest 1))))))
The distances function looks just like map, except that
                      posn -> num
                      posn -> posn
                   More Uses of Map
; modernize : list-of-pipe -> list-of-pipe
(define (modernize 1)
  ; replaces 4 lines:
  (map modern-pipe 1))
; modern-pipe : pipe -> pipe
; rob-train : list-of-car -> list-of-car
(define (rob-train 1)
  ; replaces 4 lines:
; rob-car : car -> car
```

Folding a List

How about sum?

sum : list-of-num -> num

Doesn't return a list, so neither filter nor map help

But recall combine-nums...

```
; combine-nums : list-of-num num
; (num num -> num) -> num
(define (combine-nums l base-n COMB)
  (cond
    [(empty? l) base-n]
    [(cons? l)
    (COMB
    (first l)
    (combine-nums (rest l) base-n COMB))]))
```

The Foldr Function

```
; foldr : (X Y -> Y) Y list-of-X -> Y
(define (foldr COMB base 1)
  (cond
    [(empty? 1) base]
    [(cons? 1)
      (COMB (first 1)
          (foldr COMB base (rest 1)))]))
```

Useful for HW 5:

```
; total-blue : list-of-col -> num
(define (total-blue 1)
  (local [(define (add-blue c n)
                    (+ (color-blue c) n))]
        (foldr add-blue 0 1)))
```

The Foldr Function

```
; foldr : (X Y -> Y) Y list-of-X -> Y
(define (foldr COMB base 1)
  (cond
    [(empty? 1) base]
    [(cons? 1)
      (COMB (first 1)
         (foldr COMB base (rest 1)))]))
```

The sum and product functions become trivial:

```
(define (sum 1) (foldr + 0 1))
(define (product 1) (foldr * 1 1))
```

The Foldr Function

```
; foldr : (X Y -> Y) Y list-of-X -> Y
(define (foldr COMB base 1)
  (cond
    [(empty? 1) base]
    [(cons? 1)
       (COMB (first 1)
            (foldr COMB base (rest 1)))]))
```

In fact,

The Foldr Function	The Source of Foldr
<pre>; foldr : (X Y -> Y) Y list-of-X -> Y (define (foldr COMB base 1) (cond [(empty? 1) base] [(cons? 1) (COMB (first 1) (foldr COMB base (rest 1)))]))</pre>	How can foldr be so powerful?
Yes, filter too: (define (filter f l) (local [(define (check i r) (cond [(f i) (cons i r)] [else r]))] (foldr check empty l)))	
The Source of Foldr	Other Built-In List Functions
Template:	More specializations of foldr:
<pre>(define (func-for-loX 1) (cond [(empty? 1)] [(cons? 1) (first 1) (func-for-loX (rest 1))])) Fold: (define (foldr COMB base 1) (cond [(empty? 1) base] [(cons? 1) (COMB (first 1) (foldr COMB base (rest 1)))]))</pre>	<pre>ormap : (X -> bool) list-of-X -> bool andmap : (X -> bool) list-of-X -> bool Examples: ; got-milk? : list-of-sym -> bool (define (got-milk? 1) (local [(define (is-milk? s) (symbol=? s 'milk))] (ormap is-milk? s))) ; all-passed? : list-of-grade -> bool (define (all-passed? 1) (andmap passing-grade? 1))</pre>

What about Non-Lists?

Since it's based on the template, the concept of fold is general