Detecting 3D Points of Interest Using Multiple Features and Stacked Auto-encoder

Zhenyu Shu, Shiqing Xin*, Xin Xu, Ligang Liu, and Ladislav Kavan

Abstract—Considering the fact that points of interest on 3D shapes can be discriminated from a geometric perspective, it is reasonable to map the geometric signature of a point \( p \) to a probability value encoding to what degree \( p \) is a point of interest, especially for a specific class of 3D shapes. Based on the observation, we propose a three-phase algorithm for learning and predicting points of interest on 3D shapes by using multiple feature descriptors. Our algorithm requires two separate deep neural networks (stacked auto-encoders) to accomplish the task. During the first phase, we predict the membership of the given 3D shape according to a set of geometric descriptors using a deep neural network. After that, we train the other deep neural network to predict a probability distribution defined on the surface representing the possibility of a point being a point of interest. Finally, we use a manifold clustering technique to extract a set of points of interest as the output. Experimental results show superior detection performance of the proposed method over the previous state-of-the-art approaches.

Index Terms—3D shapes, Point of interest, Multiple features, Stacked auto-encoder

1 INTRODUCTION

3D points of interest (POIs), also referred to as feature points or salient points, are distinctive points in visual perception. POIs are found to be very useful in geometry processing tasks, such as mesh segmentation [1], mesh registration [2], shape enhancement [3], shape retrieval [4], viewpoint selection [5] and visual attention guidance [6].

There is a common understanding that POIs can be discriminated from a geometric perspective but the real relationship between POIs and geometric descriptors is quite complicated [7], [8]. A number of research works [9], [10] suggest extracting a feature vector to encode the local geometry for any vertex of the input shape and then selecting a subset of representative vertices as the POIs. However, the resulting POIs are still conspicuously different from manually marked salient points, which reveals that automatically detecting POIs in coincidence with human visual perception still remains a challenging problem.

In spite of the existing challenge, it is reasonable to map the geometric signature of a point \( p \) to a probability value encoding to what degree \( p \) is a POI. However, judging whether a point is a POI or not is actually a subjective task because different people may have different understanding about POIs. Inspired by recent advances in deep learning [11], [12], we propose a novel algorithm for learning and predicting POIs on 3D shapes by using multiple feature descriptors. Our algorithm requires two separate deep regression neural networks to accomplish the task. One network is trained on the whole dataset to identify the membership of a given 3D shape, and the other network is trained on each category respectively to predict a saliency map according to the extracted geometric signature once the membership is known. Finally, we use a manifold clustering technique to extract a set of POIs as the output. Our deep learning-based method can automatically learn and detect the results in coincidence with humans’ expectation as long as the necessary training data is provided. Figure 1 shows an example of POIs detected by our approach.

We evaluate our approach on SHREC 2011 non-rigid 3D shape dataset [13], which contains 600 different 3D shapes. The ground truth data on these models are obtained from manually marked data by volunteers. Numerous experimental results show that our approach outperforms the state of the art in terms of various measures, such as False Negative Error (FNE), Weighted Miss Error (WME), False Positive Error (FPE), Area Under the ROC Curve (AUC), Normalized Scanpath Saliency (NSS) and Linear Correlation Coefficient (LCC).

Our contributions are three-fold.
We use deep neural networks to predict a saliency map for a given 3D shape, which is rather different from conventional classification problem.

We integrate various geometric descriptors into our algorithmic framework. It may achieve better detection results if some new descriptors are considered in this framework.

Our method is data-driven and users are able to obtain reliable salient points as long as there are sufficiently many labeled ground truth samples.

The remainder of the paper is organized as follows. Section 2 reviews the related work on POI detection and deep learning-based 3D shape analysis. Section 3 presents the overall detection framework followed by detailed configuration of the deep neural networks. The training/predicting techniques are detailed in Section 4. After that, we give the 3D POI detection algorithm in Section 5. In Section 6, we show extensive experimental results, as well as comparison statistics. Finally, we point out limitations and future work in Section 7 and conclude this paper in Section 8.

2 RELATED WORK
At least three topics are highly related to the theme of this paper: detection of POIs, extraction of geometric feature descriptors and deep learning based 3D shape analysis.

2.1 POI detection
POIs or salient points, originated from the area of computer vision, are widely studied in the computer graphics community. Detecting POI is useful on many occasions, for example, performing a shape-based search across distinctive regions [14] or selecting the most informative views of a given 3D model [15].

In the early stages, researchers found 3D POIs from multiple 2D projected views, such as [16], [17], [18], [19]. Since about 10 years ago, researchers turned to detect POIs directly on the input polygonal surface, measuring saliency according to the geometric property in a neighborhood. Depending on the neighborhood size, we can further classify existing methods into two kinds.

The first kind of algorithms measures saliency in a local scale. For example, Koch et al. [20] suggested that the salient regions should be distinctive from their immediate surroundings. Lee et al. [21] defined scale-dependent saliency using a center-surround operator on Gaussian-weighted mean curvatures. Gal et al. [4] constructed salient geometric features to represent the geometry of local regions of the surface by combining low-level features into a high-level one. In fact, spectral analysis techniques can also be used for this purpose. The key idea [22], [23] is to transform the spectral residual in the spectral domain back to the spatial domain.

The other kind of methods [24], [25] measures saliency in a rather different manner. They often need to evaluate global contrast differences and spatial coherence. The central idea is to set up one kind of measurement that makes the eye-catching regions stand out from a global scope. For example, Perazzi et al. [26] conducted contrast-based saliency estimation using high-dimensional Gaussian filters. In addition, priors or more visual cues on foreground or background have been shown to be helpful to saliency detection from recent research results [27], [28].

Technically speaking, detecting POIs is to automatically identify salient information that coincides with human perception. In fact, POIs are related to geometric features but it is hard to find an explicit formula to characterize the relationship between them. Motivated by this observation, in this paper, we propose a novel method based on deep learning techniques. On one hand, this new framework is able to learn from manually labeled data and predict salient points like humans do. On the other hand, it enables us to extract POIs by considering multiple geometric features, rather than only a single feature. New geometric features can be easily integrated into this framework. Finally, it is worthwhile to point out that detecting POIs is a subjective problem, i.e., different people may have different understandings. Our algorithm is data-driven and can guarantee the prediction results to match the training data to the fullest extent.

In [7], the authors also propose a data-driven method to effectively detect Schelling points on 3D mesh models. However, they employ random forests, which is a different strategy from our method, to predict the distribution of Schelling points. The comparison between their method and ours can be found in Section 6.3.

Recently, another method of detecting tactile mesh saliency, where a human is more likely to grasp, press, or touch on a 3D mesh model is proposed in [29]. By mapping a 3D model to multiple depth images, they propose a novel...
multi-view deep ranking method, which builds a regression between depth images and tactile saliency, to predict the regions where human tend to touch. It is worth to point out that not only the goal of their method, but also the regression constructed is very different from our method where a regression between geometric feature vectors and the probabilities of being POIs for all vertices is constructed. We do not present the comparison of these two methods in this paper due to the very different detection goals.

2.2 Feature descriptors

Feature descriptors are central to POI detection problem. Usually, a feature descriptor is to encode local or global geometric features for a given 3D shape. It can be typically represented by a scalar or vector field on a polygonal mesh, and then converted into a histogram before training the neural network. In recent years, numerous local feature descriptors have been proposed, such as Gaussian curvature (GC), shape diameter function (SDF) ([30]), and average geodesic distance (AGD) ([31]). Bronstein et al. [32] developed a scale-invariant heat kernel descriptor (SIHKS). The construction is based on a logarithmically sampled scale-space in which shape scaling corresponds to a translation. Aubry et al. [33] proposed a shape signature (WKS) which represents the average probability of measuring a quantum mechanical particle at a specific location and very suitable for non-rigid 3D shapes. Knopp et al. [34] presented a local 3D shape descriptor by using Hough-voting. Smeets et al. [35] proposed a four-step algorithm to generate a local shape descriptor for face recognition under expression variations and partial data. In this paper, we use 3 descriptors including SIHKS, WKS, and GC to detect POIs.

2.3 Deep learning-based 3D shape analysis

In recent years, a lot of deep learning-based research work [36], [37], [38] has been proposed to solve various problems in 3D shape analysis, such as shape retrieval, shape segmentation and even shape modeling. The design of the deep learning framework is closely related to geometric representations. Depending on this, we can divide the existing approaches into 3 categories. The first category [39], [40], [41] transforms a given 3D shape into a set of 2D views each of which has a structured representation. However, this kind of methods may suffer from information loss. Therefore, different from the first category of methods, the second category of algorithms [42], [43], [44] directly learns features from uniform or adaptive voxelized data of 3D shapes by introducing a 3D convolution operator. In practice, the voxelization resolution cannot be too high due to the limitation of current computing power. To accelerate the training process, the third category of methods [12], [45], [46], [47], [48], [49], [50] aims at learning high-level features on certain discretizations of surfaces (e.g. triangular meshes, point clouds or range scans). Some of them [12], [45], [46] learn high-level features based on conventional hand-crafted geometric features and can usually achieve desirable performance while tolerating a small amount of training data especially when it is very hard to get sufficiently many training samples. In this paper, we build our deep neural network upon multiple conventional hand-crafted features to automatically detect POIs on 3D shapes, which falls into the third category.

3 Overview

Our algorithm relies on two deep neural networks to robustly detect POIs in a supervised way, as illustrated in Figure 2. One network is to predict the membership of the given 3D model to a specific class, and the other network is to predict the probability of being a POI for any vertex according to its geometric properties. Finally, an extra step is required to extract typical POIs from the resulting saliency map. We achieve this by density peak-based clustering algorithm [51].

It is worth noting that we use deep neural networks to predict a model dependent probability field, rather than a set of labels, which is different from previous shape classification or segmentation problems. For this purpose, we transform manually labeled data to probability fields by constructing a biharmonic distance field. At the same time, we need to extract POIs from probability fields by clustering techniques. This is the key to adapting conventional deep neural networks to the POI detection problem.

4 Background

In this section, we detail the architecture of the two deep neural networks, one used to detect the POIs and the other to predict the class of the target 3D shape. Both of them have four layers in total, concatenated stacked auto-encoders (SAE) [52] and contain a softmax layer, as shown in Figure 3. For the neural network of predicting POIs, the numbers of neurons are experimentally set to 120-40-10-1. For the other neural network, the corresponding setting is 320-160-80-30.

4.1 Auto-encoders

Just as its name implies, SAE is a neural network composed of multiple layers of sparse auto-encoders. As shown in Figure 4, the auto-encoder we used consists of an input layer, a hidden layer, and an output layer. It is able to automatically learn latent features of the input by minimizing the discrepancy between the input features and the reconstruction ones.

In Figure 4, the top mapping represents the stage of the encoder, while the bottom mapping represents that of the decoder. Let $N_L$ and $N_G$ be the numbers of units in
and the Equation 4 can be redefined as follows:

$$\text{reconstruction error of the cost function:}$$

$$H \left( x \right) = \frac{1}{2} \sum_{i=1}^{m} \left\| x_{(i)} - y_{(i)} \right\|_{2}^{2} + \lambda \left\| \theta \right\|_{2}^{2},$$

where $$\lambda$$ is the weight decay parameter, $$\theta = \{ W, b \}$$, $$W$$ and $$b$$ represent the weights and the biases of the auto-encoder respectively.

To further prevent the auto-encoder from learning some useless information from the training feature vectors, we apply a sparsity constraint on the hidden layer based on the Kullback-Leibler (KL) divergence [54] in this paper. To this end, the optimization problem can be formulated as follows:

$$\arg \min \theta \left( \mathbf{D} \left( \mathbf{X}, \mathbf{Y}^{1}, \theta \right) + \tau \sum_{i=1}^{N_{G}} KL \left( \rho \mid \mid \hat{\rho}_{i} \right), \right)$$

where

$$KL \left( \rho \mid \mid \hat{\rho}_{i} \right) = \rho \log \frac{\rho}{\hat{\rho}_{i}} + (1 - \rho) \log \frac{1 - \rho}{1 - \hat{\rho}_{i}},$$

$$\tau$$ is the weight of sparsity penalty term, $$\rho$$ is the sparsity parameter, $$\hat{\rho}_{i} = \frac{1}{m} \sum_{j=1}^{m} (g_{i,j})$$ is the average activation of the hidden unit $$g_{i}$$ (averaged over the all the input training feature vectors), and $$\left( g_{i,j} \right)$$ represents the corresponding activation of the hidden unit $$g_{i}$$ of the $$i$$th input training feature vector. From problem (6), we can see that the sparsity penalty term will vanish if $$\hat{\rho}_{i} = \rho$$. So the closer $$\hat{\rho}_{i}$$ and $$\rho$$ are, the sparser the hidden layer will be.

With this formulation, we use the back propagation algorithm [55] and the gradient descent approach to train the auto-encoder by optimizing the cost function with respect to $$\theta$$.

### 4.2 Stacked auto-encoders

To further learn high-level features, multiple layers of sparse auto-encoders (SAE) are stacked up, where the latent feature vectors learned in the previous auto-encoder are used as the input of the next auto-encoder. The whole training process is carried out in a greedy layer-wise way [56] and better parameters are generated for deep neural networks and desirable results are produced [57]. After training each auto-encoder using the method described in Section 4.1, the outputs $$\mathbf{W}_{j}^{2}$$ and $$\mathbf{y}_{j}^{1}$$ of the auto-encoder are discarded and the latent features $$\mathbf{g}_{j}^{1}$$ of the auto-encoder are used to feed the next auto-encoder.

To predict the membership of a 3D model, we add an extra softmax layer to the end of SAE for the neural network of 3D model classification. The predicted membership for each 3D model is obtained by finding the index of the maximal element of the output vector $$\mathbf{v}$$. For the neural network of predicting POIs, we add an extra layer with sigmoid activation function to the end of SAE. Given the output feature vector $$\mathbf{g}_{j}^{1}$$ of the SAE, the output value $$v = \frac{1}{1 + e^{-\mathbf{W}_{j}^{1} \mathbf{g}_{j}^{1} + b_{j}}}$$ is the predicted probability of each vertex being a POI.

### 5 POI detection using deep neural network

#### 5.1 Training data preparation

Our training data is obtained from manual labeling. For SHREC 2011 dataset, we developed a small and simple application for visually labeling the POIs on training 3D shapes. 5 volunteers were then asked to mark POIs on these models. We adopt the strategies proposed in [7] to avoid and filter possible bad data. The volunteers are asked to select points on the surface of a 3D model likely to
In the experimental setting, we select three widely known feature descriptors: SHHKs, WKS, and GC, although other feature descriptors can be integrated into our algorithmic framework. These feature descriptors are deemed to have a capability of characterizing the geometric properties well from different perspectives and therefore are widely used for vertex classification, such as in mesh segmentation and other related problems [59], [60], [61], [62], [63].

For our POIs prediction neural network, we extract feature vectors for each vertex on the 3D shapes and feed them to the network for POI detection.

For our 3D shape classification neural network, we extract feature vectors for each 3D shape and feed the feature vectors to the network for classification. For GC that is a scalar field on each patch, it is easy to capture the feature distribution using histograms. For SHHKs and WKS that are vector fields on each patch, we extract the 1D feature distribution by using the well-known bag-of-feature (BoF) technique. The number of bins in the histograms and that of the bags for the bag-of-feature representation are both set to $B = 100$. This way, any feature descriptor can be adapted into our algorithmic framework. After that, we need to concatenate the feature vectors extracted by using different feature descriptors and take them as the input of our 3D shape classification neural network.

Once the deep neural networks are trained, the predicted results can be easily obtained by applying forward propagation to the corresponding vectors of a target 3D shape.

### 5.3 Point visualization via decision graph

Although it is hard for us to define strictly what a POI is from a mathematical point of view, the following observation is helpful. First, a POI $p$ should have high saliency. Second, points with higher saliency than $p$ are not available in $p$'s neighborhood. The two aspects are crucial to determine a POI. In fact, the clustering technique proposed in [51] inspires us to visualize the points via a decision graph.

For each data point $v_i$, we use $P_i = \hat{P}(v_i)$ to denote $v_i$'s saliency. Let $\{d_{ij}\}_{n \times n}$ be the geodesic distance matrix between data points. We use $\delta_i$ to denote the influence distance of $v_i$:

$$\delta_i = \min_{j:P_j > P_i} (d_{ij}),$$

Generally speaking, the vertices that are mapped to the upper right corner of the decision graph tend to be POIs. That is to say, it turns out that we can use $\gamma_i = P_i \delta_i$ to measure to what extent a given point is a POI. In Figure 6, we map each vertex of the Hand model (left) to the decision graph (right). We can clearly see that the five tip points are mapped to the upper right corner. However, this is not as easy as it seems. Imagine that there is a large plate with a flat hump in the middle. It’s possible that the hump is not so conspicuous to be deemed as a POI by users but may be incorrectly taken as a POI due to its large influence distance $\delta$. Therefore, a quantitative evaluation criterion of a POI is required.

### 5.4 POI selection via statistical testing

From $\{v_i\}_{i=1}^n$, it is easy to compute $\{\delta_i\}_{i=1}^n$ and $\{\gamma_i\}_{i=1}^n$. In order to select POIs via the statistical testing method, we have to make prior assumptions on $\{\delta_i\}_{i=1}^n$ and $\{\gamma_i\}_{i=1}^n$.
Our assumption is based on the following two observations. First, $\delta_i$ is non-negative. Second, $\delta_i$ of a POI is usually relatively large and the number of POIs is usually relatively smaller than the number of other points on the surface of 3D shapes. Similar to [64], we can therefore assume that $\{\delta_i\}_{i=1}^n$ follows the long-tailed distribution. Furthermore, $\{\gamma_i\}_{i=1}^n$ can also be assumed to follow the long-tailed distribution because $\delta_i$ follows the long-tailed distribution and $\rho_i$ is positive.

With the assumption that $\{\delta_i\}_{i=1}^n$ and $\{\gamma_i\}_{i=1}^n$ follow the long-tailed distribution, there exists some $\lambda > 0$, such that the cumulative density function has the following form:

$$F(x) = 1 - L_0(x) \cdot x^{-\lambda},$$

where $L_0$ is a slowly varying function (for sufficiently large $x$, $L_0$ behaves almost like a constant), and the parameter $\lambda$ denotes the tail index. The key to determining if $\nu$ is a POI is to make clear whether $\nu$ is located on the long tail or not according to the distribution of $\{\gamma_i\}_{i=1}^n$.

According to [64], [65], we can transform $\{\gamma_i\}_{i=1}^n$ into an ordered list, $\{\gamma_i\}_{i=1}^n$, such that $\gamma_1 \leq \gamma_2 \leq \cdots \leq \gamma_n$, and then select the POIs by checking $\gamma_{\hat{m}}, \gamma_{\hat{m}-1}, \cdots, \gamma_1$ one after another, where $m$ is set to $[0.1n]$ empirically. Once the point that gives $\gamma_k (k \leq m)$ is identified as a POI by the following inequality, all the points that give $\gamma_1, \gamma_2, \cdots, \gamma_k-1$ are also identified as POIs:

$$\frac{\gamma_k}{\gamma_{k+1}} \geq 1 - (1 - \alpha)^{1/m} \cdot 1/(\lambda k),$$

where $\alpha$ is the parameter to define the level of significance (5% in the default setting). The tail index $\lambda$ can be estimated with the modified Hill-type estimator suggested in [65]. The outward statistical testing method enables us to select POIs in an effective and robust manner.

## 6 Evaluation

In this section, we experimentally validate our algorithm and compare it to previous methods.

### 6.1 Experimental configuration

**Experimental dataset.** We test our method on the SHREC 2011 non-rigid 3D model dataset, which is an open dataset originally used for 3D shape classification and retrieval. The SHREC 2011 dataset contains 30 categories of 3D shapes and each category has 20 3D shapes, so that there are 600 3D shapes in SHREC 2011 dataset total. Each shape in the dataset contains about 9500 vertices. We developed a small visual tool and manually marked POIs for each 3D shape in the dataset. For each category, we randomly select 10 shapes as the training shapes, and the left shapes are regarded as test shapes. Note that our regression networks are trained on each category respectively, while our classification network is trained on the whole dataset. Some example models in SHREC 2011 dataset are shown in Figure 7. We show some representatives of our human-marked POIs in Figure 8.

**Evaluation metrics.** To evaluate our method, we adopt three metrics that are defined by [8], including False Negative Error (FNE), False Positive Error (FPE) and Weighted Miss Error (WME). Let $G$ represents the set of ground truth points, and $D$ be the set of points detected by an algorithm for a 3D shape. A point $g_i \in G$ is considered to be correctly detected if there exists a detected point $d_i \in D$ such that $d_i$ is close to $g_i$ but not closer to any other points in $G$. To measure the error of the detection results, FNE and FPE are defined as $FNE = 1 - N_C / |G|$ and $FPE = 1 - N_C / |D|$ respectively, where $N_C$ is the number of correctly detected points, and $| \cdot |$ represents the size of a set. To take the prominence of $g_i$ into account, WME is used to measure how many subjects are marked by the algorithm within a parameterized geodesic neighborhood of $g_i$. Assuming that $n_i$ subjects have marked a POI within a geodesic neighborhood of radius $r$ around the ground truth point $g_i$, WME is defined as $WME = 1 - \frac{\sum_{i=1}^{G} n_i \delta_i}{\sum_{i=1}^{G} n_i}$, where $\delta_i = 1$ if $g_i$ is correctly detected; otherwise, $\delta_i = 0$. For the three metrics, a lower score represents better performance.

We have also adopted three more recent metrics proposed in [66], which are Area Under the ROC Curve (AUC), Normalized Scanpath Saliency (NSS) and Linear Correlation Coefficient (LCC), to measure the performance of our algorithm. A receiver operating characteristic (ROC) curve is a plot illustrating the performance of a binary classifier for different threshold values. The area under the ROC curve is previously widely used to compare saliency models in the 2D case. NSS measures saliency values at points selected by users (ground truth) and defined as a weighted sum of the computational saliency at those points. LCC is the correlation coefficient between two variables. We use it to...
Fig. 8. Some example models with our human-marked POIs on SHREC 2011 dataset.

Fig. 9. Hand model POIs prediction: When the inputs are training model’s POIs which are hand-marked by human subject (a), we can use the function $P$ to get label value for each vertex (b) and then it is used as a training set for prediction neural network. The POIs for other models are finally predicted by our algorithm (c).

Fig. 10. Comparison of the hand-marked POIs and the result of POI detection for a Hand model: (a) Hand model with hand-marked POIs; (b) The predicted result of POIs by prediction neural network; (c) The POIs extracted from the prediction model.
measure the strength of the linear relationship of the two saliency distributions, which are obtained from an algorithm and the human-marked ground truth on a 3D shape respectively. For all three metrics, a higher score represents better performance.

Parameter settings. In this paper, the coefficient $\sigma$ of controlling the decreasing speed of the function $P$ is set to 0.05. The geodesic distance between vertices is relatively small, so in order to make the label value of each vertex distributed within the range of 0-1, we set $\sigma$ to be 0.05, while larger $\sigma$ will make the label values be less distinguishable. In our experiments, the dimension of the POIs prediction neural network is set to 120, where 1 dimension from GC and 19 dimensions from SIHKS and 100 dimensions from WKS. For our prediction neural network, the numbers of the neurons in each layer are set to 120-40-10-1. The corresponding setting is 300-160-80-30 for our 3D shape classification neural network.

6.2 Results

For SHREC 2011, we train the 3D model classification network and POIs prediction network respectively. To train the POIs prediction network, the hand-marked POIs are selected as ground truth and a probability field $P$ is constructed as described in Section 5.1. As shown in Figure 9, the function $P$ is used to compute the label for each vertex. These labels are then regarded as the ground truth that acts on the whole model and used as the training set for the prediction neural network. As a result, we can get the probability of being a POI for each vertex on the testing model. The detected POIs are finally extracted by employing the clustering technique described in Section 5.3 and 5.4.

Figure 10 shows the results of using the model with each vertex labeled by classification neural network and the prediction neural network to extract the POIs for a Hand model. We can see the results of extraction are fairly obvious and our algorithm gives desirable POIs. Figure 10 also shows the comparison between the human-marked ground truth of POIs (Figure 10 (a)) and our prediction results (Figure 10 (b)) for the Hand model. The comparison also exhibits the power of our algorithm because we can see that they are very similar.

Figure 11 shows the predicted probabilities of the POIs for some representative categories of 3D shapes in SHREC 2011. In some cases, although the distribution of the local probability is not very stable with our algorithm, it is enough for specifying the locations of POIs from the point of view of the overall model. The vast majority of POI detection results from our algorithm are desirable and consistent with our perception. Figure 12 shows more results of our algorithm.

Judging whether a point is a POI or not is a subjective problem. Our approach is data-driven and can naturally adapt to different training data, which is an important advantage. As shown in Figure 13, different predicted results can be obtained when different training data is provided. Regardless of the ridge points between neighboring fingers are considered as POIs or not, our approach can get desirable results as long as the corresponding training data is provided.

Figure 14 shows the results of POI detection by using our method for an Armadillo model with different resolutions. The results are obtained by directly applying our trained predicted neural network to 3D models with lower resolutions. We can see that although the 3D models are greatly simplified, the detected results are still in coincidence with humans’ visual perception.

We must point out that the POI detection quality relies on the accuracy of our classification neural network. According to the statistics shown in Table I, the classification neural network is able to accurately identify the category of the input 3D object, which enables us to predict POIs by referring to the geometrically similar objects in the same category.

6.3 Comparison

We compare our method with three other POI detection algorithms 3D-SIFT [70], 3D-Harris [71] and HKS-based POIs [8], [72] on SHREC 2011 database. For 3D-SIFT, the following strategy is used to identify the POIs on a 3D model. First, a scale space is constructed by applying different layers of 3D Gaussian filters to the voxelized model. Then, the Difference of Gaussian (DoG) for each level is obtained by subtracting the original model from the scaled model. The extrema points are selected by searching the DoG space in both spatial and scale dimensions. Their closest vertices on the original mesh are marked as final POIs. For both 3D-Harris and HKS, the local maxima are first selected by considering the neighborhood of a vertex. For HKS, 2-ring neighborhood is considered and all local maxima are then detected as POIs. However, only 1-ring neighborhood is considered and a certain number of local maxima with highest Harris response are then selected as POIs for 3D-Harris. The results of 3D-Harris and HKS-based POIs are obtained by using the implementation provided by corresponding authors. The results of 3D-SIFT are got from using our own implementation. All the algorithms are compared against human-marked POIs by 16 subjects. Figure 15 shows an example of the POI detection results by our algorithm and three other algorithms. We can see that the results from our algorithm and HKS-based POIs are better than others. We use three metrics provided by [8] for evaluation and the detailed statistics plots are shown in Figure 16, where a quantitative comparison on all models is provided. It can be seen that our POI detection algorithms outperforms the other detection approaches for all three metrics FPE, FNE and WME.

We also compare our method with the state-of-the-art method proposed in [7] (Schelling Point method, SP) on the SHREC 2007 dataset. The dataset contains 20 categories of 3D models and each category has 20 models. Schelling Point method is also data-driven but different from the strategy adopted in this paper – they use a decision tree based regression model (M5P regression trees as provided by Weka) to detect POIs on 3D models. In their work, the authors provide a human-labeled ground truth data set on the SHREC 2007 dataset, which facilitates us to directly train our neural network of predicting POIs. For each category of 3D models, 10 randomly selected models are used for training while the remaining 10 models
Fig. 11. Examples of the predicted probabilities of the POIs on some representative classes of models: (a) hand models; (b) flamingo models; (c) shark models; (d) rabbit models.

Fig. 12. Some results of our algorithm. POIs in coincidence with humans’ expectation are successfully detected by our method.

Fig. 13. Results of our method trained with different input points. The top row shows the detected results where the ridge points between neighboring fingers are considered and marked as POIs in the training data. As a comparison, the bottom row shows the detected results where the ridge points between neighboring fingers are not regarded as POIs in the training data.

Fig. 14. The results of POI detection by using our method for an Armadillo model with different resolutions.
Fig. 15. Comparison between results from our algorithm and the other three feature point detection algorithms. (a) shows the predicted probabilities of the POIs using our algorithm. The approaches used here include (b) Our algorithm; (c) 3D-SIFT; (d) 3D-Harris; (e) HKS.

Fig. 16. Comparison between our algorithm with state-of-the-art feature points detection algorithms on all models using False Negative Error, False Positive Error, and Weighted Miss Error. The data for each metric is obtained from averaging over all models on SHREC 2011 datasets.

Fig. 17. The comparison between our method and the method proposed in [7]. The top line shows some examples of detected POIs by using our method. The bottom line shows the corresponding examples of detected POIs by using the method proposed in [7].

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<th>Bird1</th>
<th>Bird2</th>
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<td>Dog2</td>
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<td>Gorilla</td>
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<tr>
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<td>100%</td>
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<td>100%</td>
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for testing. The saliency of each vertex on the testing 3D models is then predicted by applying the regression model. Figure 17 shows a comparison between the results from the two algorithms. We can see that our method is able to achieve better detection results due to the use of deep neural networks. A more detailed quantitative comparison between our algorithm and Schelling Point method on the SHREC 2007 dataset is presented in Table 2, Table 3 and Table 4. The measures used for comparison include AUC, LCC, and NSS – a higher score indicates better performance. It can be seen that our method has a superior performance for most of categories of 3D models. Besides, our method obtains better scores when averaging all the categories.

Furthermore, we compare our method with four other state-of-the-art methods including Cluster-based point set saliency (CS) [67], Saliency of large point sets (LS) [68], Mesh saliency via spectral processing (MS) [69] and PCA-based saliency (PS) [66] on SHREC 2007 dataset. The resulting AUC, LCC, and NSS metrics are respectively shown in Table 2, Table 3 and Table 4. From the comparison tables, it can be seen that our algorithm outperforms the other algorithms for most of the categories. Although our algorithm is not always the best, the average metric score of our algorithm is stably higher than the other algorithms.

We further test the performance of applying our neural network trained from SHREC 2011 dataset to SHREC 2007 non-rigid 3D models dataset. A higher score represents better performance.

### Table 2

<table>
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<tr>
<th>Algorithms</th>
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<th>SP</th>
<th>CS</th>
<th>LS</th>
<th>MS</th>
<th>PS</th>
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### Table 3

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<th>Algorithms</th>
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<th>PS</th>
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<td>0.4813</td>
<td>0.2848</td>
<td>0.3701</td>
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</table>
dataset. The results are also shown in Table 2, Table 3 and Table 4. It can be observed that comparable performances are gained. It is worth pointing out that only 10 categories of 3D shapes are selected and tested because the other categories have no geometric similarities.

### 6.4 Performance

We implemented the proposed algorithm in Matlab and C++. In average, our algorithm takes around 10 minutes to process a single model on a PC with 2.60GHz CPU and 128GB RAM. As shown in Table 5, the bottleneck lies in the training step that spends over 80% of the total compute time.

### 7 Limitation and Future Work

First, the detection performance of our method depends on the quality of manually labeled data. A reliable training dataset is necessary to guarantee good results.

Second, a classification step is pre-computed before we proceed to process a single model on a PC with 2.60GHz CPU and 128GB RAM. As shown in Table 5, the bottleneck lies in the training step that spends over 80% of the total compute time.

Finally, the current implementation of the training process is very time-consuming. In the future, we plan to explore parallelized implementations to reduce the time complexity and facilitate the application of our method in practice. Employing specialized hardware for deep networks (such as Tensor Processing Units) may be very helpful.

### 8 Conclusion

In this paper, we propose a novel supervised method for detecting POIs on 3D shapes based on deep learning techniques. The key idea is to predict a saliency map to encode the possibility of being a POI and then extract typical POIs by clustering. Our method is data-driven and able to predict POIs in a similar way as human observers. Extensive experimental results show that our method outperforms state-of-the-art approaches and reveals how the distribution of POIs depends on geometric features.

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### References


Data Engineering


