

### $K$ -nearest-neighbors

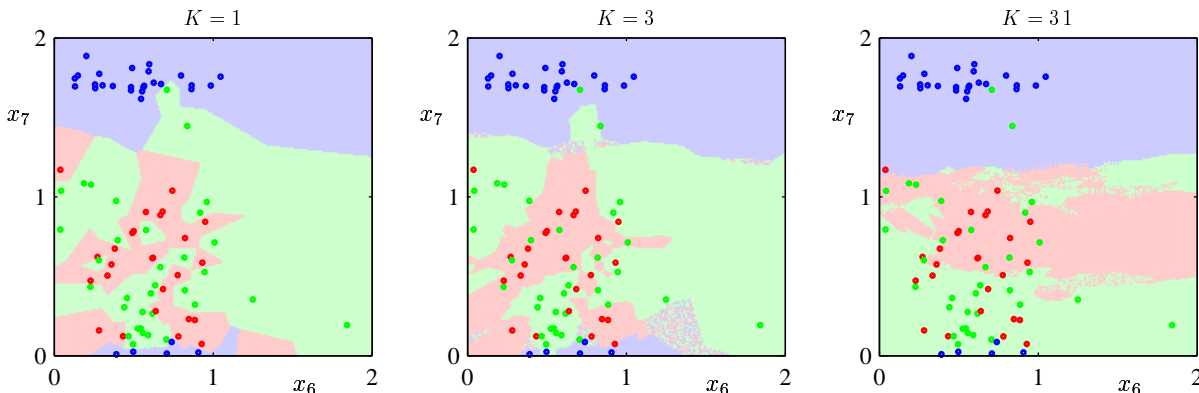
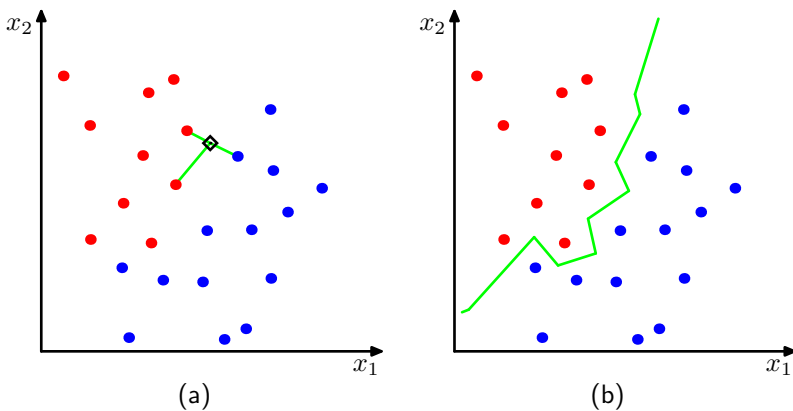
1NN—simple intuition: to classify a new data point, just return the class of the closest training point.

$k$ NN—instead of single closest point, average over the  $k$  nearest.

$\epsilon$ NN—instead of the  $k$  nearest, use as many as fit in a ball of radius  $\epsilon$ .

How does one train such an algorithm?

Despite its simplicity,  $k$ NN is a really really good classifier. (But very sensitive to irrelevant features.)



In general, as  $k$  (or  $\epsilon$ ) gets bigger, you are risking more underfitting. As  $k$  (or  $\epsilon$ ) gets smaller, you are risking more overfitting.

One can also give each of the  $k$  nearest neighbors a *vote* based on how far away they are. This vote is usually of the form  $1/d$  or  $e^{-d}$ , where  $d$  is the distance between the training point and the test point.

(Can be used also for regression, by averaging responses.)