## Interpreter with Continuations

(define (eval-expression exp env cont)
(cases expression exp
(lit-exp (datum)
(apply-cont cont datum))
(var-exp (id)
(apply-cont cont (apply-env env id)))
(proc-exp (id body-exp)
(apply-cont cont

> (closure id body-exp env)))
...))
(define (apply-cont cont val)
(cases continuation cont
(done-cont () val)
...))

## Continuations and Gotos

(define (eval-expression exp env cont)
(cases exp
(proc-exp (id body-exp) (apply-cont cont
(closure id body-exp env)))
=>
; ; registers:
(define EXP ...) (define CONT ...) ...
(define (eval-expression) (cases EXP
(proc-exp (id body-exp) (set! VAL (closure id body-exp ENV))
; ; CONT stays the same (apply-cont)) ; "goto"

## Continuations and Gotos

(define (eval-expression exp env cont) (cases exp...
(app-exp (rator rand)
(eval-expression rator env
(app-arg-cont rand env cont)))
=>
(define (eval-expression)
(cases EXP
(app-exp (rator rand)
(set! EXP rator)
; ; ENV stays the same
(set! CONT (app-arg-cont rand ENV CONT))
(eval-expression)) ; "goto"

## Continuations and Gotos

- Registers and gotos explain why the following program never generates a stack overflow:

$$
\begin{aligned}
& \text { let } \mathbf{f}=\operatorname{proc}(\mathbf{f}) \operatorname{proc}(\mathbf{n})((\mathbf{f} \mathbf{f}) \mathbf{n}) \\
& \text { in }((\mathbf{f} \mathbf{f}) 0)
\end{aligned}
$$

- So, can we compute arbitrarily deep recursions?

```
let f= proc(f)
        proc(n)
    if n}\mathrm{ then +(1, ((f f) -(n, 1)))
        else 0
in ((f f) 1000000000)
```


## Allocation

- We've avoided stack allocation
- But we still have to allocate
- continuation records
- closures
- environment records


## Allocation

- Where do we call malloc?
(define (eval-expression)
(cases EXP
(proc-exp (id body-exp)
(set! VAL (closure id body-exp ENV))
;; CONT stays the same
(apply-cont))
(app-exp (rator rand)
(set! EXP rator)
;; ENV stays the same
(set! CONT (app-arg-cont rand ENV CONT))
(eval-expression))


## Allocation

- Where do we call malloc?
(define (eval-expression)
(cases EXP
(proc-exp (id body-exp)
(set! VAL (closure id body-exp ENV))
;; CONT stays the same
(apply-cont))
(app-exp (rator rand)
(set! EXP rator)
; ; ENV stays the same
(set! CONT (app-arg-cont rand ENV CONT)) (eval-expression))


## Exposing Allocation

(define (closure id body env)
(let ([v (malloc 4)])
(mem-set! v 0 closure-tag)
(mem-set! v 1 id)
(mem-set! v 2 body)
(mem-set! v 3 env)
v) )
(define (closure? v)
(= (mem-ref v 0) closure-tag))
(define (closure->id v) (mem-ref v 1))

## Memory Allocator

(define memory (make-vector 200))
(define allocated 0)
(define (malloc size)
(let ([result allocated])
(set! allocated (+ allocated size)) result))
(define (mem-set! a n v) (vector-set! memory (+ a n) v))
(define (mem-ref a $n$ ) (vector-ref memory (+ a n)))

## Exposing Allocation

- Use of malloc explains why the following program runs out of memory:

$$
\begin{aligned}
& \text { let } \mathbf{f}=\operatorname{proc}(\mathbf{f}) \\
& \quad \operatorname{proc}(\mathbf{n}) \\
& \quad \text { if } \mathbf{n} \text { then }+(1,((\mathbf{f} \mathbf{f})-(\mathbf{n}, 1))) \\
& \quad \text { else 0 } \\
& \text { in }((\mathbf{f} \mathbf{f}) 1000000000)
\end{aligned}
$$

- Each call to (ff) extends the continuation
- Eventually, the continuation fills all memory


## Exposing Allocation

- Does the following program run forever?

$$
\begin{aligned}
& \text { let } \mathbf{f}=\operatorname{proc}(\mathbf{f}) \operatorname{proc}(\mathbf{n})((\mathbf{f} \mathbf{f}) \mathbf{n}) \\
& \text { in }((\mathbf{f} \mathbf{f}) 0)
\end{aligned}
$$

- Each call to (f f)
- creates an extended environment
- creates a new closure

We need deallocation

## Deallocation

- Where do we call free?

```
(define (apply-cont)
    (cond
    [ (app-cont? CONT)
    (let ([rator (app-cont->rator CONT)]
                [old-cont (app-cont->cont CONT)])
        (set! EXP (closure->body rator))
        (set! ENV (extend-env
        (closure->id rator)
        VAL
        (closure->env rator)))
        (set! CONT old-cont))
    (eval-expression)]
```


## Deallocation

- Where do we call free?

```
(define (apply-cont)
    (cond
    [ (app-cont? CONT)
    (let ([rator (app-cont->rator CONT)]
                [old-cont (app-cont->cont CONT)])
    (set! EXP (closure->body rator))
    (set! ENV (extend-env
        (closure->id rator)
        VAL
        (closure->env rator)))
        (free CONT) ; ; unless letcc'd!
        (set! CONT old-cont))
        (eval-expression)]
```


## Deallocation

- Where do we call free?

```
(define (apply-cont)
    (cond
    [ (app-cont? CONT)
    (let ([rator (app-cont->rator CONT)]
                [old-cont (app-cont->cont CONT)])
    (set! EXP (closure->body rator))
    (free ENV) ; ; unless in a closure!
    (set! ENV (extend-env
    (closure->id rator)
        VAI
        (closure->env rator)))
        (set! CONT old-cont))
        (eval-expression)]
```


## Reference Counting

Reference counting: a way to know whether a record has other users

- Attatch a count to every record, start at 0
- When installing a pointer to a record (into a register, or another record), increment its count
- When replacing a pointer to a record, decrement its count
- When a count is decremented to 0 , decrement counts for other records referenced by the record, then free it


## Reference Counting



- Top boxes are the registers ENV, CONT, etc.
- Boxes in the blue area are allocated with malloc


## Reference Counting



- Adjust counts when a pointer is changed...


## Reference Counting



- ... freeing a record if its count goes to 0


## Reference Counting



- Same if the pointer is in a register


## Reference Counting



- Adjust counts after frees, too...


## Reference Counting



- ... which can trigger more frees

Reference Counting


- Another example


## Reference Counting



- Adding a reference increments a count


## Reference Counting



- Lower-left records are inaccessible, but not deallocated
- In general, cycles break reference counting


## Garbage Collection

Garbage collection: a way to know whether a record is accessible

- A record referenced by a register is live
- A record referenced by a live record is also live
- A program can only possibly use live records, because there is no way to get to other records
- A garbage collector frees all records that are not live
- We'll allocate until we run out of memory, then run a garbage collector to get more space


## Garbage Collection Algorithm

- Color all records white
- Color records referenced by registers gray
- Repeat until there are no gray records:
- Pick a gray record, $r$
- For each white record that $r$ points to, make it gray
- Color r black
- Deallocate all white records


## Garbage Collection



- All records are marked white


## Garbage Collection



- Mark records referenced by registers as gray


## Garbage Collection



- Need to pick a gray record
- Red arrow indicates the chosen record


## Garbage Collection



- Mark white records referenced by chosen record as gray


## Garbage Collection



- Mark chosen record black


## Garbage Collection



- Start again: pick a gray record


## Garbage Collection



- No referenced records; mark black


## Garbage Collection



- Start again: pick a gray record


## Garbage Collection



- Mark white records referenced by chosen record as gray


## Garbage Collection



- Mark chosen record black


## Garbage Collection



- Start again: pick a gray record


## Garbage Collection



- No referenced white records; mark black


## Garbage Collection



- No more gray records; deallocate white records
- Cycles do not break garbage collection


## Two-Space Copying Collectors

A two-space copying collector compacts memory as it collects, making allocation easier.

Allocator:

- Partitions memory into to-space and from-space
- Allocates only in to-space

Collector:

- Starts by swapping to-space and from-space
- Coloring gray => copy from from-space to to-space
- Choosing a gray record => walk once though the new to-space, update pointers


## Two-Space Collection



Left $=$ from-space
Right $=$ to-space


## Two-Space Collection

Mark gray = copy and leave forward address


## Two-Space Collection

Choose gray by walking through to-space


## Two-Space Collection

Mark referenced as gray


## Two-Space Collection



## Two-Space Collection

Nothing to color gray;


## Two-Space Collection

## Color referenced record gray



## Two-Space Collection



## Two-Space Collection



## Two-Space Collection



## Two-Space Collection

Right $=$ from-space Left = to-space


## Two-Space Collection on Vectors

- Everything is a number:
- Some numbers are immediate integers
- Some numbers are pointers
- An allocated record in memory starts with a tag, followed by a sequence of pointers and immediate integers
- The tag describes the shape


## Two-Space Vector Example

- 26-byte memory (13 bytes for each space), 2 registers
- Tag 1: one integer
- Tag 2: one pointer
- Tag 3: one integer, then one pointer

$$
\text { Register 1: } 7 \quad \text { Register 2: } 0
$$

From: $\begin{array}{lllllllllllll}1 & 75 & 2 & 0 & 3 & 2 & 10 & 3 & 2 & 2 & 3 & 1 & 4\end{array}$

## Two-Space Vector Example

- 26-byte memory (13 bytes for each space), 2 registers
- Tag 1: one integer
- Tag 2: one pointer
- Tag 3: one integer, then one pointer

$$
\text { Register 1: } 7 \quad \text { Register 2: } 0
$$

| From: | $\mathbf{1}$ | $\mathbf{7 5}$ | $\mathbf{2}$ | $\mathbf{0}$ | $\mathbf{3}$ | $\mathbf{2}$ | 10 | $\mathbf{3}$ | $\mathbf{2}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{1}$ | $\mathbf{4}$ |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Addr: | 00 | 01 | 02 | 03 | 04 | 05 | 06 | 07 | 08 | 09 | 10 | 11 | 12 |

## Two-Space Vector Example

- 26-byte memory (13 bytes for each space), 2 registers
- Tag 1: one integer
- Tag 2: one pointer
- Tag 3: one integer, then one pointer

Register 1:7 Register 2: 0
$\begin{array}{lrrrrrrrrrrrrr}\text { From: } & 1 & 75 & 2 & 0 & 3 & 2 & 10 & 3 & 2 & 2 & 3 & 1 & 4 \\ \text { Addr: } & 00 & 01 & 02 & 03 & 04 & 05 & 06 & 07 & 08 & 09 & 10 & 11 & 12\end{array}$

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| From: | $\mathbf{1}$ | $\mathbf{7 5}$ | $\mathbf{2}$ | $\mathbf{0}$ | $\mathbf{3}$ | $\mathbf{2}$ | 10 | $\mathbf{3}$ | $\mathbf{2}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{1}$ | $\mathbf{4}$ |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Addr: | 00 | 01 | 02 | 03 | 04 | 05 | 06 | 07 | 08 | 09 | 10 | 11 | 12 |
|  | $\wedge$ |  | $\wedge$ |  | $\wedge$ |  |  | $\wedge$ |  |  | $\wedge$ |  |  |
| To: | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

## Two-Space Vector Example

- 26-byte memory (13 bytes for each space), 2 registers
- Tag 1: one integer
- Tag 2: one pointer
- Tag 3: one integer, then one pointer

Register 1:0 Register 2: 0
$\begin{array}{lrrrrrrrrrrrrr}\text { From: } & \mathbf{1} & \mathbf{7 5} & \mathbf{2} & \mathbf{0} & \mathbf{3} & \mathbf{2} & \mathbf{1 0} & 99 & 0 & \mathbf{2} & \mathbf{3} & \mathbf{1} & \mathbf{4} \\ \text { Addr: } & 00 & 01 & 02 & 03 & 04 & 05 & 06 & 07 & 08 & 09 & 10 & 11 & 12 \\ & \wedge & & \wedge & & \wedge & & & \wedge & & & \wedge & & \\ \text { To: } & 3 & \mathbf{2} & \mathbf{2} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0\end{array}$

## Two-Space Vector Example

- 26-byte memory (13 bytes for each space), 2 registers
- Tag 1: one integer
- Tag 2: one pointer
- Tag 3: one integer, then one pointer

Register 1: $0 \quad$ Register 2: 3
$\begin{array}{lrrrrrrrrrrrrr}\text { From: } & 99 & 3 & \mathbf{2} & 0 & 3 & \mathbf{2} & 10 & 99 & 0 & 2 & 3 & 1 & 4 \\ \text { Addr: } & 00 & 01 & 02 & 03 & 04 & 05 & 06 & 07 & 08 & 09 & 10 & 11 & 12 \\ & \wedge & & \wedge & & \wedge & & & \wedge & & & \wedge & & \\ \text { To: } & 3 & 2 & 2 & 1 & 75 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0\end{array}$

## Two-Space Vector Example

- 26-byte memory (13 bytes for each space), 2 registers
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Register 1: $0 \quad$ Register 2: 3
$\begin{array}{lrrrrrrrrrrrrr}\text { From: } & 99 & 3 & 99 & 5 & 3 & 2 & 10 & 99 & 0 & 2 & 3 & 1 & 4 \\ \text { Addr: } & 00 & 01 & 02 & 03 & 04 & 05 & 06 & 07 & 08 & 09 & 10 & 11 & 12 \\ & \wedge & & \wedge & & \wedge & & & \wedge & & & \wedge & & \\ \text { To: } & 3 & 2 & 5 & 1 & 75 & 2 & 0 & 0 & 0 & 0 & 0 & 0 & 0\end{array}$

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- 26-byte memory (13 bytes for each space), 2 registers
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## Two-Space Vector Example

- 26-byte memory (13 bytes for each space), 2 registers
- Tag 1: one integer
- Tag 2: one pointer
- Tag 3: one integer, then one pointer

Register 1: $0 \quad$ Register 2: 3

| From: | 99 | 3 | 99 | 5 | 3 | 2 | 10 | 99 | 0 | 2 | 3 | 1 | 4 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Addr: | 00 | 01 | 02 | 03 | 04 | 05 | 06 | 07 | 08 | 09 | 10 | 11 | 12 |
|  | $\wedge$ |  | $\wedge$ |  | $\wedge$ |  |  | $\wedge$ |  |  | $\wedge$ |  |  |
| To: | 3 | 2 | 5 | 1 | 75 | 2 | 3 | 0 | 0 | 0 | 0 | 0 | 0 |

