Symbols

Our favorite **list-of-sym** program:

```
; eat-apples : list-of-sym -> list-of-sym
(define (eat-apples 1)
  (cond
  [(empty? 1) empty]
  [(cons? 1)
   (local [(define ate-rest (eat-apples (rest 1)))]
      (cond
        [(symbol=? (first 1) 'apple) ate-rest]
        [else (cons (first 1) ate-rest)]))]))
```

- How about **eat-bananas**?
- How about eat-non-apples?

Filtering Symbols

```
; filter-syms : (sym -> bool) list-of-sym
; -> list-of-sym
(define (filter-syms PRED 1)
  (cond
    [(empty? 1) empty]
    [(cons? 1)
     (local [(define r
               (filter-syms PRED (rest 1)))]
       (cond
         [(PRED (first 1))
          (cons (first l) r)]
         [else r]))]))
```

This looks really familiar

Last Time: Filtering Numbers

```
; filter-nums : (num -> bool) list-of-num
; -> list-of-num
(define (filter-nums PRED 1)
  (cond
    [(empty? 1) empty]
    [(cons? 1)
     (local [(define r
               (filter-nums PRED (rest 1)))]
       (cond
         [(PRED (first 1))
          (cons (first l) r)]
         [else r]))]))
```

How do we avoid cut and paste?

Filtering Lists

We know this function will work for both number and symbol lists:

```
; filter : ...
(define (filter PRED 1)
  (cond
    [(empty? 1) empty]
    [(cons? 1)
     (local [(define r
                (filter PRED (rest 1)))]
       (cond
         [(PRED (first 1))
          (cons (first l) r)]
         [else r]))]))
```

But what is its contract?

How about this?

```
(num-OR-sym -> bool) list-of-num-OR-list-of-sym
-> list-of-num-OR-list-of-sym
```

- ; A num-OR-sym is either
- ; num
- ; sym
- ; A list-of-num-OR-list-of-sym is either
- ; list-of-num
- ; list-of-sym

How about this?

```
(num-OR-sym -> bool) list-of-num-OR-list-of-sym
-> list-of-num-OR-list-of-sym
```

This contract is too weak to define **eat-apples**

```
; eat-apples : list-of-sym -> list-of-sym
(define (eat-apples 1)
  (filter not-apple? 1))
```

```
; not-apple? : sym -> bool
(define (not-apple? s)
    (not (symbol=? s 'apple)))
```

eat-apples must return a list-of-sym, but by its contract, filter might return a list-of-num

How about this?

```
(num-OR-sym -> bool) list-of-num-OR-list-of-sym
-> list-of-num-OR-list-of-sym
```

This contract is too weak to define **eat-apples**

```
; eat-apples : list-of-sym -> list-of-sym
(define (eat-apples 1)
  (filter not-apple? 1))
```

```
; not-apple? : sym -> bool
(define (not-apple? s)
    (not (symbol=? s 'apple)))
```

not-apple? only works on symbols, but by its contract filter
might give it a num

The reason **filter** works is that if we give it a **list-of-sym**, then it returns a **list-of-sym**

Also, if we give **filter** a **list-of-sym**, then it calls **PRED** with symbols only

A better contract:

```
filter :
((num -> bool) list-of-num
  -> list-of-num)
OR
((sym -> bool) list-of-sym
  -> list-of-sym)
```

But what about a list of **images**, **posns**, or **snakes**?

The True Contract of Filter

The real contract is

```
filter : ((X -> bool) list-of-X -> list-of-X)
```

where **x** stands for any type

- The caller of **filter** gets to pick a type for **x**
- All xs in the contract must be replaced with the same type

Data definitions need type variables, too:

- ; A list-of-X is either
- ; empty
- ; (cons X empty)

Using Filter

The filter function is so useful that it's built in

New solution for HW 4 that works in **Intermediate**:

```
(define (eat-apples 1)
  (local [(define (not-apple? s)
                    (not (symbol=? s 'apple)))]
        (filter not-apple? 1)))
```

Looking for Other Built-In Functions

```
Recall inflate-by-4%:
```

Is there a built-in function to help?

Yes: map

Using Map

```
(define (map CONV 1)
  (cond
    [(empty? 1) empty]
    [else (cons (CONV (first 1))
                (map CONV (rest 1)))]))
(define (inflate-by-4% 1)
  (local [(define (inflate-one n)
            (* n 1.04))]
    (map inflate-one l)))
; negate-colors : list-of-col -> list-of-col
(define (negate-colors 1)
  (map negate-color 1))
```

The Contract for Map

```
(define (map CONV 1)
 (cond
   [(empty? 1) empty]
   [else (cons (CONV (first 1))
                    (map CONV (rest 1)))]))
```

- The 1 argument must be a list of x
- The **CONV** argument must accept each **x**
- If **CONV** returns a new **x** each time, then the contract for **map** is

map : $(X \rightarrow X)$ list-of-X -> list-of-X

Posns and Distances

Another function from HW 4:

The **distances** function looks just like **map**, except that **distances-to-0** is

posn -> num

not

The True Contract of Map

Despite the contract mismatch, this works!

```
(define (distances 1)
  (map distance-to-0 1))
```

The true contract of **map** is

map : (X -> Y) list-of-X -> list-of-Y

The caller gets to pick both x and y independently

More Uses of Map

```
; modernize : list-of-pipe -> list-of-pipe
(define (modernize 1)
  ; replaces 4 lines:
  (map modern-pipe 1))
; modern-pipe : pipe -> pipe
: rob-train : list-of-car -> list-of-car
(define (rob-train 1)
  ; replaces 4 lines:
  (map rob-car 1))
; rob-car : car -> car
```

```
• • •
```

Folding a List

How about **sum**?

```
sum : list-of-num -> num
```

Doesn't return a list, so neither **filter** nor **map** help

```
But recall combine-nums...
```

```
; combine-nums : list-of-num num
; (num num -> num) -> num
(define (combine-nums l base-n COMB)
  (cond
    [(empty? l) base-n]
    [(cons? l)
    (COMB
    (first l)
    (combine-nums (rest l) base-n COMB))])) <sup>26-27</sup>
```

```
; foldr : (X Y -> Y) Y list-of-X -> Y
(define (foldr COMB base 1)
  (cond
    [(empty? 1) base]
    [(cons? 1)
      (COMB (first 1)
        (foldr COMB base (rest 1)))]))
```

The **sum** and **product** functions become trivial:

```
(define (sum 1) (foldr + 0 1))
(define (product 1) (foldr * 1 1))
```

```
; foldr : (X Y -> Y) Y list-of-X -> Y
(define (foldr COMB base 1)
  (cond
    [(empty? 1) base]
    [(cons? 1)
      (COMB (first 1)
        (foldr COMB base (rest 1)))]))
```

```
Useful for HW 5:
```

```
; total-blue : list-of-col -> num
(define (total-blue 1)
   (local [(define (add-blue c n)
                    (+ (color-blue c) n))]
   (foldr add-blue 0 1)))
```

```
; foldr : (X Y -> Y) Y list-of-X -> Y
(define (foldr COMB base 1)
  (cond
    [(empty? 1) base]
    [(cons? 1)
      (COMB (first 1)
        (foldr COMB base (rest 1)))]))
```

In fact,

```
(define (map f l)
 (local [(define (comb i r)
                         (cons (f i) r))]
                (foldr comb empty l)))
```

```
; foldr : (X Y -> Y) Y list-of-X -> Y
(define (foldr COMB base 1)
  (cond
    [(empty? 1) base]
    [(cons? 1)
      (COMB (first 1)
        (foldr COMB base (rest 1)))]))
```

```
Yes, filter too:
```

The Source of Foldr

How can **foldr** be so powerful?

The Source of Foldr

```
Template:
(define (func-for-loX 1)
  (cond
    [(empty? 1) ...]
    [(cons? 1) ... (first 1)
     ... (func-for-loX (rest 1)) ...]))
Fold:
     (define (foldr COMB base 1)
       (cond
          [(empty? 1) base]
          [(cons? 1)
           (COMB (first 1)
                 (foldr COMB base (rest 1)))]))
```

Other Built-In List Functions

More specializations of **foldr**:

```
ormap : (X -> bool) list-of-X -> bool
andmap : (X -> bool) list-of-X -> bool
Examples:
```

```
; got-milk? : list-of-sym -> bool
(define (got-milk? l)
  (local [(define (is-milk? s)
               (symbol=? s 'milk))]
  (ormap is-milk? s)))
```

```
; all-passed? : list-of-grade -> bool
(define (all-passed? 1)
  (andmap passing-grade? 1))
```

What about Non-Lists?

Since it's based on the template, the concept of fold is general

```
; fold-ftn : (sym num sym Z Z -> Z) Z ftn -> Z
(define (fold-ftn COMB base ftn)
 (cond
    [(empty? ftn) base]
    [(child? ftn)
     (COMB (child-name ftn) (child-date ftn) (child-eyes ftn)
           (fold-ftn COMB BASE (child-father ftn))
           (fold-ftn COMB BASE (child-mother ftn))))))
(define (count-persons ftn)
  (local [(define (add name date color c-f c-m)
            (+ 1 c-f c-m))
    (fold-ftn add 0 ftn)))
(define (in-family? who ftn)
  (local [(define (here? name date color in-f? in-m?)
            (or (symbol=? name who) in-f? in-m?))]
    (fold-ftn here? false ftn)))
```